

A proof of Riemann Hypothesis.

Riemann Zeta-Function

$$\xi(s) = \sum_{n=1}^{\infty} \frac{1}{n^s} = \prod \frac{1}{1-p^s} \quad (s = a + bi)$$

Riemann Hypothesis: all the Non-trivial zero-point of Zeta-Function $Re(s) = 1/2$.

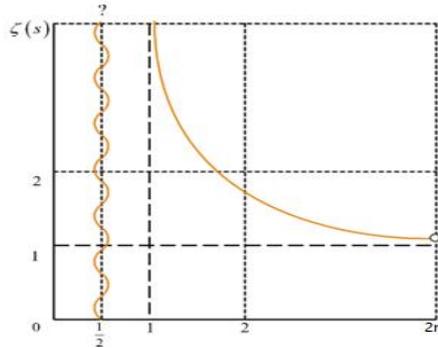


Figure.3. Riemann Hypothesis: all the non-trivial Zero points of Riemann zeta-function are on the $1/2$ axis.

We can get figure.3

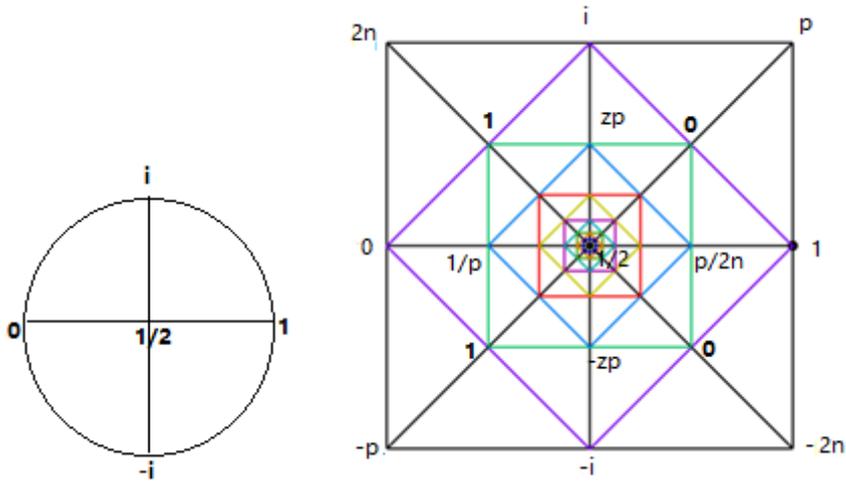


Fig.4. N-domain analytic continuation with $\frac{p}{2n} - \frac{1}{p}$ in $L^{1/2}_{(0\ 1/2\ 1)}$ space
 We have

$$1/2 = 1/2 \quad 0 = 1/2 - 1/2 \quad 1 = 1/2 + 1/2 \quad i^2 = -1$$

$$1/2 = (1/2 + 1/2 \cdot i) (1/2 - 1/2 \cdot i)$$

$$i^0 = 1 \quad i^1 = i \quad i^2 = -1 \quad i^3 = -i \quad i^4 = 1$$

So we can construct a space with a $1/2$ Fixed Point, we call it $L^{1/2}_{(0\ 1/2\ 1)}$
 We also have

$$\frac{1}{p} \rightarrow 0$$

$$\frac{p}{n} \rightarrow 1$$

$$zp = \frac{1}{2} + \frac{1}{2} \left(\frac{p}{n} - \frac{1}{p} \right) i$$

$$-zp = \frac{1}{2} - \frac{1}{2} \left(\frac{p}{n} - \frac{1}{p} \right) i$$

$$i^{2n} = \pm 1 \quad i^n = (i \quad -1 \quad -i \quad 1)$$

$$i^p = \pm i$$

$$1 + \begin{bmatrix} 2n & i & p \\ 0 & 1/2 & 1 \\ -p & -i & -2n \end{bmatrix} \begin{bmatrix} 1/2 & \dots & \frac{1}{2^n} [1 + (p/n - 1/p)i] \\ \dots & 1/2 & \dots \\ \frac{1}{2^n} [1 - (p/n - 1/p)i] & \dots & 1/2 \end{bmatrix} = 0$$

The $\text{tr}(A) = 1/2 * n$

This is the proof of Hilbert–Pólya conjecture. This is mean that all the non-trivial Zero points of Riemann zeta-function are on the 1/2 axis just show as Fig.3. So we give a proof of Riemann Hypothesis.

In fact, we have

$$1 + \frac{e^{ip\pi} - e^{i2N\pi}}{\sum \frac{1}{2^N}} = 0$$

$N \sim (0, 1, 2, 3, 4, \dots)$ all the natural numbers.

$p \sim (3, 5, 7, \dots)$ all the odd prime numbers.

This equation gives a structure of all N and p with a 1/2 fixed point.