

# ELECTRON AND ELECTRONS SYSTEM

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ABSTRACT. This article try to unified the four basic forces by Maxwell equations, the only experimental theory. Self-consistent Maxwell equations with the e-current coming from matter current is proposed, and is solved to electrons and the structures of particles and atomic nucleus. The static properties and decay are reasoned, all meet experimental data. The equation of general relativity sheerly with electromagnetic field is discussed as the base of this theory. In the end the conformation elementarily between this theory and QED and weak theory is discussed.

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## 1. BOUND DIMENSIONS

A rebuilding of units and physical dimensions is needed. Time  $s$  is fundamental.

We can define:

The unit of time:  $s$  (second)

The unit of length:  $cs$  ( $c$  is the velocity of light)

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*Date:* Jun 16, 2021.

*Key words and phrases.* Maxwell equations; Decay; Electron function; Recursive re-substitution.

The unit of energy:  $\hbar/s$  ( $\hbar$  is Plank constant)

The unit dielectric constant  $\epsilon$  is

$$[\epsilon] = \frac{[Q]^2}{[E][L]} = \frac{[Q]^2}{\hbar c}$$

The unit of magnetic permeability  $\mu$  is

$$[\mu] = \frac{[E][T]^2}{[Q]^2[L]} = \frac{\hbar}{c[Q]^2}$$

The unit of  $Q$  (charge) is defined as

$$c[\epsilon] = c[\mu] = 1$$

then

$$[Q] = \sqrt{\hbar}$$

$$\sqrt{\hbar} = (1.0546 \times 10^{-34})^{1/2} C$$

$C$  is charge's SI unit Coulomb.

For convenience, new base units by unit-free constants are defined,

$$c = 1, \hbar = 1, [Q] = \sqrt{\hbar} = [1]$$

then the units are reduced.

Define

$$\text{UnitiveElectricalCharge} : \sigma = \sqrt{\hbar}$$

$$\sigma = 1.027 \times 10^{-17} C \approx 64e$$

$$e_{/\sigma} = e/\sigma = 1.5602 \times 10^{-2} \approx 1/64$$

It's defined that

$$\beta := m/e = 1, \quad m := |k_e| \approx m_e$$

Then all units are power  $\sigma^n$ . This unit system is called *bound dimension* or *bound unit*. We always take the definition latter in this article

$$\beta = 1, \quad \sigma = 1$$

We always take them as a standard unit.

Define a *measure*  $\sigma/z$ ,  $[z] = 1$ :

$$\sigma = z \quad \sigma/z = 1$$

## 2. INNER FIELD OF ELECTRON

Try the self-consistent Maxwell equation for the inner electromagnetic (EM) field of electrons

$$(2.1) \quad \partial^l \partial_l A^\nu = i A_\mu^* \partial_\nu A^\mu / 2 + cc. = \mu J^\nu \quad m = 1$$

$$\partial^\nu \cdot A_\nu = 0$$

with definition

$$[W := \langle A | A_\mu^* \partial_\nu A^\mu \rangle] = \sigma^4, \quad [A] = \sigma^2$$

$$(A^i) := (V, \mathbf{A}), (A_i) := (V, -\mathbf{A})$$

$$(J^i) = (\rho, \mathbf{J}), (J_i) = (\rho, -\mathbf{J})$$

$$\partial := (\partial_i) := (\partial_t, \partial_{x_1}, \partial_{x_2}, \partial_{x_3})$$

$$\partial' := (\partial^i) := (\partial_t, -\partial_{x_1}, -\partial_{x_2}, -\partial_{x_3})$$

$$g_{ij} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

This equation has the symmetry  $CPT$ .

### 3. GENERAL ELECTROMAGNETIC FIELD

We find

$$(x', t') := (x, t - r) \\ \partial_x^2 - \partial_t^2 = \partial_{x'}^2 =: \nabla'^2$$

The following is the energy of a piece of field  $A$ :

$$(3.1) \quad \varepsilon := \frac{1}{2} (\langle E, D \rangle + \langle H, B \rangle)$$

The time-variant part is neglected, as a convention for energy calculation. If the field has Fourier transformation then this *electromagnetic (EM) energy* becomes

$$(3.2) \quad \varepsilon = \frac{1}{2} \langle A_\nu | \partial_t^2 - \nabla^2 | A^\nu \rangle$$

under Lorentz gauge.

### 4. SOLUTION OF ELECTRON

The solution by *recursive re-substitution* (RRS) for the two sides of the equation is proposed. For the equation

$$\hat{P}'B = \hat{P}B$$

Its algorithm is that (It's approximate, the exact solution needs a rate on the start state in the re-substitution for the normalization condition)

$$\hat{P}' \left( \sum_{k \leq n} B_k + B_{n+1} \right) = \hat{P} \sum_{k \leq n} B_k$$

A function is initially set and is corrected by RRS of the equation 2.1. Here is the start state

$$A_i = A_r e^{-ikt}, \partial_\mu \partial^\mu A_i = 0$$

The fields' correction  $A_n$  with  $n$  degrees of  $A_i$  is called the  $n$  degrees correction.

Firstly

$$\nabla^2 \phi = -k^2 \phi$$

is solved. Exactly, it's solved in spherical coordinate

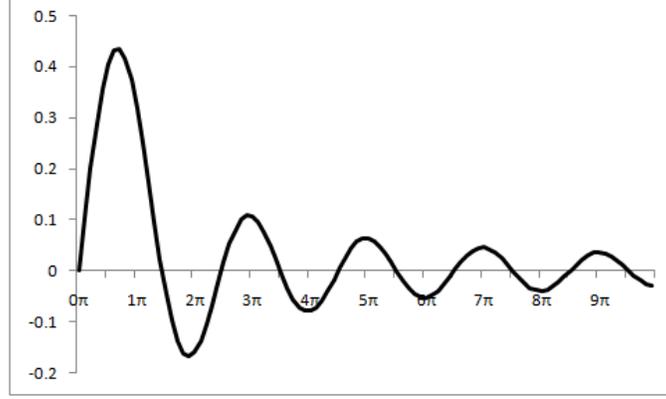
$$-k^2 = \nabla^2 = \frac{1}{r^2} \partial_r (r^2 \partial_r) + \frac{1}{r^2 \sin \theta} \partial_\theta (\sin \theta \partial_\theta) + \frac{1}{r^2 \sin^2 \theta} (\partial_\varphi)^2$$

Its solution is

$$\Omega_k := \Omega_{klm} = k j_l(kr) Y_{lm}(\theta, \varphi) e^{-ikt} \\ \phi_k := k \phi_{klm} e^{-ikt} := k h_l(kr) Y_{lm}(\theta, \varphi) e^{-ikt} \\ \omega_k := k j_1(kr) Y_{11}(\theta, \varphi) e^{-ikt}$$

After normalization it's in effect

$$h = \frac{e^{\pm ir}}{r}, \quad j = \frac{\cos r, \sin r}{r}$$

FIGURE 1. The function of  $j_1$ 

In fact, it has to be re-defined in the *smooth truncation* that keeps Fourier form

$$\Omega^\beta(x) = \Omega(x)e^{-\beta r}, \quad \beta \rightarrow 0^+$$

The similar is for  $\phi$ .

We use the following definition

$$\omega_k := e^{-\beta r} \cdot \sum_{\hat{\mathbf{k}}} \mathbf{F}(\hat{\mathbf{k}}) e^{i\mathbf{k}x - ikt}, \quad \hat{\mathbf{k}} = \frac{\mathbf{k}}{|\mathbf{k}|}, \quad |\mathbf{k}| = k$$

There are calculations:

$$\begin{aligned} (\partial_t^2 - \nabla^2)u &= -\nabla'^2 u = \delta(x')\delta(t') = \delta(x)\delta(t), \\ u &:= \frac{\delta(t-r)}{4\pi r} = \frac{\delta(t')}{4\pi r'}, \\ \nabla^2 &= \sum_{\mathbf{k}} -\mathbf{k}^2 e^{i\mathbf{k}x*} \end{aligned}$$

$$(4.1) \quad (k\Omega_k(x) | * | k\Omega_k(-x)) = \sigma k^2 \frac{\delta^3(kx)}{\sigma^3 \delta^3(0)} \quad \sigma = 1$$

Its smooth truncation is considered.

$$\delta(0) := \delta(\sigma t)|_{t=0}$$

$$\int_I dx (\Omega(x) * \Omega(x))^n = \left( \int_I dx \Omega(x) * \Omega(x) \right)^n$$

In the frequencies of  $\Omega(x) \cdot \Omega(x)$  the zero frequency is with the highest degrees of infinity. This principle is quite extensive in fact.

To avoid singularity it's calculated like

$$(e^{-\beta r} e^{ir} | * \nabla^2 | e^{-\beta r} e^{ir}) = (\nabla_\nu e^{-\beta r} e^{ir} | * | \nabla_\nu e^{-\beta r} e^{ir})$$

It's found that

$$\begin{aligned} &\langle e^{-\beta r} \frac{e^{i(r+\varphi)}}{r} \sin \theta | * | e^{-\beta r} \frac{e^{i(r+\varphi)}}{r} \sin \theta \rangle \\ &= - \langle e^{-\beta r} \frac{e^{i(r-\varphi)}}{r} \sin \theta | * | e^{-\beta r} \frac{e^{i(r-\varphi)}}{r} \sin \theta \rangle \end{aligned}$$

$$\begin{aligned}
&= - \left\langle e^{-\beta r} \frac{e^{i(-r+\varphi)}}{r} \sin \theta \right| * \left| e^{-\beta r} \frac{e^{i(-r+\varphi)}}{r} \sin \theta \right\rangle \\
&\quad \left\langle e^{-\beta r} \frac{\cos r e^{i\varphi}}{r} \sin \theta \right| * \left| e^{-\beta r} \frac{\cos r e^{i\varphi}}{r} \sin \theta \right\rangle \\
&= - \left\langle e^{-\beta r} \frac{\cos r e^{-i\varphi}}{r} \sin \theta \right| * \left| e^{-\beta r} \frac{\cos r e^{-i\varphi}}{r} \sin \theta \right\rangle
\end{aligned}$$

These also can be proved in Fourier space.

## 5. ELECTRONS

It's the start electron function for the RRS of the equation 2.1:

$$A_i^\nu := i\lambda\partial^\nu\omega_k(x,t)/\sqrt{2}, \quad \lambda \approx 1$$

Some states are defined as the core of the electron, which's the start function  $A_i(x,t)$  for the RRS of the equation 2.1 to get the whole electron function of field  $A$ :  $e$

$$\begin{aligned}
e_r^+ &: \omega_m(\varphi, t), & e_l^- &: \omega_m(-\varphi, -t) \\
e_l^+ &: \omega_m(-\varphi, t), & e_r^- &: \omega_m(\varphi, -t) \\
e_r^+ &\rightarrow e_l^+ : (x, y, z) \rightarrow (x, -y, -z)
\end{aligned}$$

The electron function is normalized with charge as

$$e = \langle A^\mu | i\partial_t | A_\mu \rangle / 2 + cc.$$

The MDM (Magnetic Dipole Moment) of electron is calculated as the second degree proximation

$$\begin{aligned}
\mu_z &= \langle A_{i\nu} | -i\partial_\varphi | A_i^\nu \rangle \cdot \hat{z} / 4 + cc. \\
&= \frac{e}{2m}
\end{aligned}$$

The spin is

$$S_z = \mu_z k_e / e = \hat{k}_e / 2$$

The correction in RRS of the equation 2.1 is calculated as

$$A - A_i = \frac{(A_i^* \cdot i\partial A_i / 2 + cc.) *_4 u}{1 - i\partial(A_i - A_i^*) / 2 *_4 u}$$

The function of  $e_r^+$  is decoupled with  $e_l^+$

$$\langle (e_r^+)^\nu | i\partial_t | (e_l^+)_\nu \rangle / 2 + \langle (e_l^+)^\nu | i\partial_t | (e_r^+)_\nu \rangle / 2 + cc. = 0$$

The following is the increment of the energy  $\varepsilon$  on the coupling of  $e_r^+, e_r^-$ , mainly between  $A_1$  and  $A_3$

$$\begin{aligned}
\varepsilon_e &= \langle (e_r^+)^\nu | i\partial_t | (e_r^-)_\nu \rangle / 2 + \langle (e_r^-)^\nu | i\partial_t | (e_r^+)_\nu \rangle / 2 + cc. \quad m = 1 \\
&\approx -2e_{/\sigma}^3 m = -\frac{1}{1.66 \times 10^{-16} s}
\end{aligned}$$

Their smooth truncation are considered. Its algorithm is

$$-\frac{2}{2} \cdot \frac{2 \cdot 2^2}{2^2}$$

The following is the increment of the energy  $\varepsilon$  on the coupling of  $e_r^+, e_l^-$ , mainly between  $A_1$  and  $A_7$ .

$$\varepsilon_x = \langle (e_r^+)^\nu | i\partial_t | (e_l^-)_\nu \rangle / 2 + \langle (e_l^-)^\nu | i\partial_t | (e_r^+)_\nu \rangle / 2 + cc. \quad m = 1$$

$$\approx -\frac{1}{2}e^7/\sigma m = -\frac{1}{1.145 \times 10^{-8}s}$$

Its algorithm is

$$-\frac{2}{.4 \cdot 4} \cdot \frac{2 \cdot 2^7}{2^6}$$

and

$$\begin{aligned} & \langle \cos^5(r - \phi) | \cos(r + \phi) \rangle, \quad \phi = t - \varphi \\ & = \langle \cos(2r) \cos^2 \phi (\cos^4 r \cos^4 \phi - \sin^4 r \sin^4 \phi) \rangle \\ & = -\frac{1}{4} \cdot \frac{1}{4} \cdot N \end{aligned}$$

These calculations of the integral product are applied:

$$(5.1) \quad \phi = Y_{11} \frac{e^{ir}}{r}, \quad -i\nabla\phi = Y_{11} \frac{e^{ir}}{r} \hat{r}$$

Normalization is considered.

## 6. SYSTEM AND TSS OF ELECTRONS

Wave functions are the scalar representation of the group of parallel motions.

The movement of electron makes an EM field denoted by  $A$ , the unit of which is verified by interactions:

$$A := f *_3 \sum_i e_i = N \sum_X f(X, T) \delta(x - X, t - T) *_4 \sum_i e_i(x, t)$$

The following are naked stable particles:

<i>particle</i>	<i>electron</i>	<i>photon</i>	<i>neutino</i>
<i>notation</i>	$e_r^+$	$\gamma_r$	$\nu_r$
<i>structure</i>	$e_r^+$	$(e_r^+ + e_r^-)$	$(e_r^+ + e_l^-)$

The following is the system of particle  $x$  with the initial state

$$A_0 := e_x \sum_c e_c,$$

There are two *base transforms*

$$\begin{aligned} e_c & := *e, \pm e, \quad d := (r, l) \\ \Phi * e_x ** e & := (\Phi * e_x)^*(x, -t) * e(x, t) \\ \Phi * e_x * -e & := \Phi(-x, -t) * e_x(-x, -t) * e(-x, -t) \\ [f\Phi] ** e & := (f\Phi)^*(x, -t) * e(x, t) \\ [f\Phi] * -e & := (f\Phi)(-x, -t) * e(-x, -t) \end{aligned}$$

The second one transfers an incoming wave to an outgoing wave, with which we can shift a particle from the left to the right in the reaction formula, with its meaning (decay energy, charge) unchanged.

$e_x, \Phi$  meet normalization (including dimensions):

$$(6.1) \quad \langle e^{-\beta r} \cdot \Phi * e_x | e^{-\beta r} \cdot \Phi * e_x \rangle = 1, \quad \langle e^{-\beta r} \cdot e_x | e^{-\beta r} \cdot e_x \rangle = 1 \quad \beta \rightarrow 0^+$$

$$\sigma[\langle \Phi * e_x * e | \Phi * e_x * e \rangle] = 1$$

The normalization is invariant under the two base transforms.

Its dense of charge of stably moving particle  $x$  is

$$\rho = (e^{-\beta r} \cdot \Phi * e_{xc} * e_c | e^{-\beta r} \cdot \Phi * e_{xc} * i\partial_t e_c) / 2 + cc. \quad \beta \rightarrow 0^+$$

$$= (e^{-\beta r} \cdot \Phi * e_{xc} * e_c |e^{-\beta r} \cdot [i\partial_t \Phi] * e_{xc} * i\partial_t e_c)/2 + cc. \quad k_\Phi = 1 \quad \beta \rightarrow 0^+$$

The momentum dense of the system is

$$p = (e^{-\beta r} \cdot \Phi * e_{xc} * e_c |i\partial|e^{-\beta r} \cdot \Phi * e_{xc} * e_c)/2 + cc. \quad \beta \rightarrow 0^+$$

$$= (e^{-\beta r} \cdot \Phi * e_{xc} * e_c |i\partial|e^{-\beta r} \cdot [i\partial_t \Phi] * e_{xc} * e_c)/2 + cc. \quad k_\Phi = 1 \quad \beta \rightarrow 0^+$$

Its observed e-current is

$$J = (e^{-\beta r} \cdot \Phi * e_{xc} * e_c |i\partial|e^{-\beta r} \cdot i\partial_t \Phi * e_{xc} * i\partial_t e_c)/2 + cc. \quad \beta \rightarrow 0^+$$

These are compared to the latter calculation of charge conservation and the 2-degree correction of electron.

*In the latter the factors  $e^{-\beta r}$  will be concealed.*

Try the action of isolated system for square of static mass with the zero-border condition

$$\delta < e_x | \partial_t^2 - \nabla^2 | e_x >_4 = 0$$

$e_{xc}$  here is without truncation. As its singularity is cut-off the function is quite normal (smooth process at the singularity), and the limit of  $\beta$  is go first of  $\delta$  or the both can commute (that's a fact). So that the initial  $A_0$  is found that

$$(\partial_t^2 - \nabla^2)e_x = 0$$

$$e_x := k_x \Omega_{k_x}(x) \quad \sigma = 1$$

This state  $A_0$  is considered as a (Transient) Steady State (TSS),  $e_x$  here is called a Light State (LS).

With the static charge conservation, after all electrons off-couple and become isolated electrons,

$$< e_x * \sum_c (e_c)^\mu | e_x * i\partial_t \sum_c (e_c)_\mu > /2 + cc.$$

$$= \sum_\nu < \phi_{k_\nu} * (e_c)^\mu | \phi_{k_\nu} * i\partial_t (e_c)_\mu > /2 + cc., \quad k_\nu \rightarrow 0$$

then it's found that

$$|k_x| = \left| \frac{n_x}{Q_x/e} \right| \quad \sigma = 1, \quad n_x := < \sum_c e_{xc} | \sum_c e_{xc} >, \quad k_\nu \rightarrow 0$$

Smooth truncation is used. It's right at least for proton and muon.

*About the conditions of the parities  $P(d)$ , I think the coupling of  $d$  on an electron is the results of coupling of MDM or EDM. In some case if an E-field is put on to uncouple them, the gravitational mass of them would become negative (see the latter).*

## 7. MUON

$$\mu^- : e_{\mu l} * (e_r^- - e_r^+ - e_l^-), \quad e_\mu = e_x(k_x = -3\sigma)$$

$\mu$  is approximately with mass  $3m/e/\sigma = 3 \times 64m$  [3.2][1] (The data in bracket is experimental by the referenced lab), spin  $S_e$  (electron spin), MDM  $\mu_B m/k_\mu$ .

The main channel of decay is

$$\mu^- \rightarrow e_r^- - \nu_r, \quad e_r^- \rightarrow -e_l^+ + \nu_l$$

$$e_\mu * e_r^- - e_\mu * \nu_r \rightarrow e_\mu * e_r^- - \phi * \nu_r$$

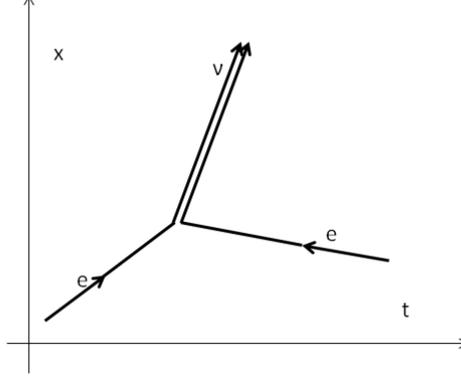


FIGURE 2. neutrino radiation

The isolated system conserves momentum in mass-center frame. We consider the reaction is without torsion.

Its main life is

$$\begin{aligned} \varepsilon_\mu &:= \langle (e_\mu^*(-x, -t) * e_\mu) \cdot ((e_r^+)^{\mu*}(-x, -t) * i\partial_t(e_l^-)_\mu) \rangle |_{t=0} + cc. \quad m = 1 \\ &= -\frac{m\varepsilon_x}{k_\mu} = -\frac{1}{2.2015 \times 10^{-6}s} \quad [2.1970 \times 10^{-6}s] \end{aligned}$$

Smooth truncation is applied. The charge conservation on neutrino is applied.

## 8. PION

The initial of pion perhaps is

$$\pi^- : e_\pi * (e_l^+ - e_l^- + *e_r^-) = e_\pi * (e_l^+ - e_l^-) + e_\pi * *e_r^-$$

Decay Channels:

$$\pi^- \rightarrow -e_l^+ + \nu_l, \quad e_l^+ \rightarrow -e_r^- + \nu_l$$

The mean life approximately is

$$-\varepsilon_x/2 = \frac{1}{2.3 \times 10^{-8}s} \quad [(2.603 \times 10^{-8}s)[1]]$$

The precise result is calculated with successive decays.

## 9. PION NEUTRAL

The initial of pion neutral is perhaps like an atom

$$\pi^0 : (e_r^+ + e_l^+, e_r^- + e_l^-)$$

It's the main decay mode as

$$\pi^0 \rightarrow \gamma_r + \gamma_l$$

The mean life is

$$-2\varepsilon_e = \frac{1}{8.3 \times 10^{-17}s} \quad [8.4 \times 10^{-17}s][1]$$

## 10. PROTON

The initial of proton may be like

$$p^+ : e_{pl} * (4e_r^- - 2e_l^+ - *3e_r^+), \quad e_p = e_x(k_x = 29\sigma)$$

The mass is  $29 \times 64m$  [29][1] that's very close to the real mass. The MDM is calculated as  $3\mu_N$  (mainly by track), spin is  $S_e$ . The proton thus designed is eternal.

## 11. NEUTRON

Neutron is the atom of a proton and a muon

$$n = (p^+, \mu^-)$$

The muon take the first track, with the decay process

$$\Phi * \mu^- = \Phi * e_\mu * (e_r^- - e_r^+ - e_l^-) \rightarrow \Phi * e_\mu * e_r^- - \nu_r$$

Make some normalization to fit 6.1. Calculate the variation of the action of the open system, the energy of system subtracting the affection,

$$(11.1) \quad i\partial_t \Phi + \frac{1}{2} \nabla^2 \Phi = -\frac{\alpha}{r} \Phi \quad m_\mu = 1$$

$$\alpha = \frac{e^2}{4\pi\epsilon\hbar c} \approx 1/137$$

One of the terms of EM energy is neglected, and its domain is cut off  $O$ . It's resolved to

$$\Phi = N e^{-r/r_0} e^{-iE_1 t}$$

$$E_1 = E_B \frac{\sigma^2}{m_\mu^2} \cdot \frac{m_\mu}{m}$$

$$E_B = -13.6eV$$

It's approximately the decay life of muon in the track that

$$\varepsilon_n = -\frac{\sigma^2}{m_\mu^2} \cdot \frac{E_B}{m} e^3 / \sigma \varepsilon_x = -\frac{1}{1019s}$$

## 12. ATOMIC NUCLEUS

We can find the equation for the fields of  $Z'$  ones of proton:  $\Phi_i$ , and the fields of  $n$  ones of muon:  $\Phi_{j:j>Z'} = \phi_i$ :

$$\Phi = \sum_i \Phi_i, \quad \phi = \sum_i \phi_i$$

$$\varphi_\nu := \Phi_\nu * (p/\mu)_l, \quad \varphi^\nu := \Phi_\nu * (p/\mu)^l$$

We have

$$I = \sum_\mu \langle \varphi^\mu | \frac{1}{2} \partial^\nu \partial_\nu | \varphi_\mu \rangle_4 / 2 - \sum_\nu \langle \varphi^\nu | \frac{1}{2} \partial^\nu \partial_\nu | \sum_{i \neq \nu} \varphi_i \rangle_4 / 2 + cc.$$

The third-level waves must catch independent tracks, or involve in strong effects. Strong effects (interactions) are omitted. Make the variation of this action on  $\Phi_i, \phi_i$

$$\delta I = 0$$

to find

$$\begin{aligned}\frac{1}{2}\partial_t^2\Phi + ik_p\partial_t\Phi + \frac{1}{2}\nabla^2\Phi &= (Z' + 2)\frac{\alpha\sigma^2}{r} * \Phi - n\frac{\alpha\sigma^4}{r} * \phi \\ \frac{1}{2}\partial_t^2\phi + ik_\mu\partial_t\phi + \frac{1}{2}\nabla^2\phi &= -Z'\frac{\alpha\sigma^2}{r} * \Phi + (n - 2)\frac{\alpha\sigma^4}{r} * \phi\end{aligned}$$

If  $E$  is known (which does exist undoubtedly and invariantly) the second equation is rendered to

$$\frac{1}{2}\partial_t^2\phi + ik_p\partial_t\phi + \frac{1}{2}\nabla^2\phi = -Z'\frac{\alpha\sigma^2}{r} * \Phi + (n - 2)\frac{\alpha\sigma^4}{r} * \phi$$

Make

$$\begin{aligned}\zeta &= \Phi + \phi\eta \\ (Z' + 2) - \eta Z' &= -n/\eta + (n - 2) =: N \\ \eta &= \frac{(Z' - n + 4) \pm \sqrt{(Z' - n + 4)^2 + 4Z'n}}{2Z'}\end{aligned}$$

then

$$\begin{aligned}-(E^2/2 + Ek_p)\nabla^2\zeta + \frac{1}{2}\nabla^4\zeta + 4\pi\alpha\sigma^2N\zeta &= 0 \\ \zeta e^{-ikt} &= \sum C_{lm}\Omega_{klm}\end{aligned}$$

So that the first approximation from  $\nabla^2(= -k^2) = -k_p^2$ :

$$E = -k_p - \sqrt{8\pi\alpha\sigma^2N}$$

$$(12.1) \quad N(Z', n) = \frac{1}{2}(Z' + n - \sqrt{(Z' + n)^2 + 8(Z' - n) + 16})$$

$$\approx -2\chi \quad \chi := \frac{Z' - n}{Z' + n}$$

$$E \approx -k_p - E_g, \quad E_g =: 10MeV, \quad \chi = 1/3$$

These states are TSS and LS obviously:  $|k| = |E|$ , hence

$$E^4 + E^3 + 8\pi\alpha\sigma^2N = 0 \quad k_p = 1$$

Every single muon or proton has third-level wave

$$\Phi_i = \sum C'_{lm}\Omega_{Elm}, \quad \phi_i = \sum C''_{lm}\Omega_{Elm}$$

**12.1. Decay Energy.** Make some normalization to fit 6.1. The life-involved energy of proton or muon under the solved wave  $\Phi_i$  is

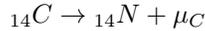
$$\begin{aligned}\varepsilon &= \langle \Phi_i * (p, \mu)^l | i\partial_t | \Phi_i * (p, \mu)_l \rangle / 2 + cc. \quad m = 1 \\ &= (-3/29 - \frac{2}{|E|}, \quad -1/3 + \frac{4}{|E|})e_{/\sigma}^{11}\end{aligned}$$

Smooth truncation is on  $\Phi_\nu$ . The measure change the calculation a few.

$$\Delta_E\varepsilon = E_\Delta(2, -4) \quad m = 1$$

$$E_\Delta \approx \frac{1}{4s}, \quad \Delta E = E_g$$

The decay



is with zero energy decrease unless the neglected weak crossing is considered.

12.2.  **$\beta$ -stable and Neutron Hide.** In the solutions when a proton combine with a muon the both have the same wave function:

$$\Phi_\mu = \phi_\mu$$

then this terms will quit from the interactional terms of the previous equations, which change to

$$(Z'_x, n_x) \rightarrow (Z'_x - 1, n_x - 1)$$

This will change the *flag energy*  $\Delta E$ . If a  $\beta$ -decay can't happen then a dismiss of this *neutron hide* will help. Out of the hidden nucleons ( $\geq 2z$ ), the ratio  $2 : 1 = Z' : n$  between protons and muons causes the most stable state. So that if

$$-N(Z' + \max(z) + z, n + \max(z) + z) \leq -N(Z' - z, n)$$

$$(12.2) \quad \frac{Z + \kappa - h}{3(Z + \kappa) + 2 \max(z) + 2z} \leq \frac{Z + \kappa - h - z}{3(Z + \kappa) - z}, \quad 8h := 3\kappa^2 + 8\kappa - 16$$

then  $\beta$ -decay wouldn't happen for the reversed process can happen. The sign of the coefficient (minus here) of the gross decay energy is also noticed.

It's found a critic point

$$\kappa \approx -8 : \quad h \approx 14$$

and

$$Z \approx 29$$

hence  $N$  of  $\max(z) = 0$  is calculated near to  $-2/3$  through parameter  $\kappa$ . By the following result 12.3, conditions  $\chi = 1/3$  and  $\max(z) = 0$  are specific for this critical point, for the other  $Z$  or  $\kappa$ , the both of which are incompatible.

The condition 12.2 is solved to

$$2(z + \max(z))z < 2 \max(z)(Z + \kappa) - (2 \max(z) + z)h$$

hence as

$$(12.3) \quad \frac{1}{4} < \chi \leq \frac{1}{3}, \quad z \leq \max(z) = ((Z + \kappa) - 1.5h)/2$$

The reaction is very weak.

It's the *Average Binding Mass Per Nucleon* according to charge number that

$$\varepsilon_M(Z) = X \cdot \sigma \Delta_0^Z \sqrt{-8\pi\alpha N}$$

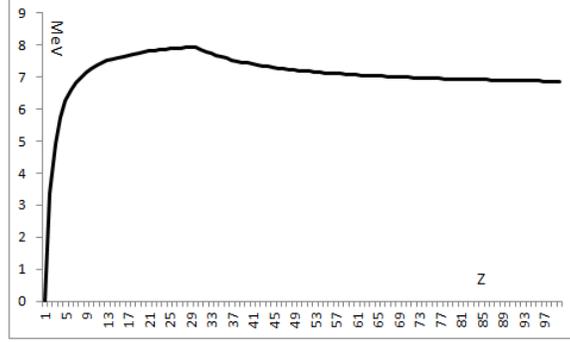
$$X = (Z \leq 29) + (Z > 29) \frac{2.0}{2.5 - 10.5/(Z - 8)}$$

The EM energy is gravitational mass by the discussions in the section 14, for proton

$$m_p = \langle \varphi_\nu | \frac{1}{2} \partial_\mu \partial^\mu | \varphi_\nu \rangle \approx k_p$$

Smooth truncation is on  $\Phi_\nu$ . By the motion  $\Phi_\nu$  to find its mechanical energy

$$M_p = -E/m_p \quad m_p = 1$$

FIGURE 3. Average Binding Mass:  $\varepsilon_M(0) - \varepsilon_M(Z)$ 

### 13. BASIC RESULTS FOR INTERACTION

For decay

$$(13.1) \quad \begin{aligned} W(t) &= \Gamma e^{-\Gamma t} \\ \Gamma &= \langle A_\nu | i\partial_t | A^\nu \rangle_{\infty}^{t=0} / 2 + cc., \quad m = 1 \\ \int_0^{\infty} W(t) dt &= 1 \end{aligned}$$

$\Gamma$  is the gross mechanical energy of electrons. It leads to the result between decay life and this mechanical emission. To prove this result with the condition 2.1, vary the measure from  $\sigma = 1$  to set this equation, at last  $m = 1$ . As varying, every atomic term is affected including the parts that out of unit variation.

The distribution shape of decay can be explain as

$$A_0 e^{-\Gamma t/2 - ik_x t}, \quad 0 < t < \Delta$$

It's the real wave of the particle  $x$  near the initial time and expanded in that time span

$$\approx \sum_k \frac{C e^{-ikt}}{k - k_x - i\Gamma/2}$$

### 14. GRAND UNIFICATION

The General Theory of Relativity is

$$(14.1) \quad R_{ij} - \frac{1}{2} R g_{ij} = -8\pi G T_{ij} / c^4$$

Firstly the unit second is redefined as  $S$  to simplify the equation 14.1

$$R_{ij} - \frac{1}{2} R g_{ij} = -T_{ij}$$

Then

$$R_{ij} - \frac{1}{2} R g_{ij} = \frac{1}{\mu} (F_{i\mu}^* F_j^\mu - g_{ij} F_{\mu\nu}^* F^{\mu\nu} / 4)$$

$F$  is conjugate and antisymmetric. We observe that the co-variant curvature is

$$R_{ij} = \frac{1}{\mu} (F_{i\mu}^* F_j^\mu + g_{ij} F_{\mu\nu}^* F^{\mu\nu} / 8)$$

## 15. CONCLUSION

Fortunately, this model explained all the effects in the known world: strong, weak and electromagnetic effects, and even subclassify them further if not being to add new ones. In this model the only field is electromagnetic field, and this stands for the philosophical that the unified world is from an unique source, all that depend on the hypothesis: in electron the movements of charge and mass are the same.

My description of particles is compatible with QED elementarily and depends on momentum quantification formula, and only contributes to it with theory of consonance state in fact. In some way, the electron function is a good promotion for the experimental models of proton and electron that went up very early.

Underlining my calculations a fact is that the electrons have the same phase (electrons consonance), which the BIG BANG theory would explain, all electrons are generated in the same time and place, the same source.

## REFERENCES

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