

# 1 Optimum Solution to Global Warming Using a Greenhouse Gas-Albedo Hotspot Theorem

## 2 In the Control of Three Types of Forcing

3 Alec Feinberg

4 DfRSoft Research, email: dfrsoft@gmail.com

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6 **Key Words:** Albedo Solution, Global Warming Solution, Global Warming Re-radiation Model,, Hotspot Mitigation, UHI Global  
7 Warming Estimates, hydro-hotspots

### 9 Abstract

10 In this paper we suggest that a fundamental GHG-albedo hotspot surface theorem, when applied to the  
11 reality of today's climate challenges, appears to indicate that the albedo solution is the optimum and  
12 safest way to mitigate climate change. The theorem also indicates that CO<sub>2</sub> solutions have an associated  
13 risk in stopping climate change when considering three types of forcing described. The albedo-GHG  
14 factor is also detailed.

### 15 1. Introduction

16 Since GHGs need long wavelength radiation to work, then changing a hotspot surfaces albedo is  
17 associated with the greenhouse gas mechanism. Therefore, we can devise *a greenhouse gas (GHG)*  
18 *albedo hotspot surface theorem* stating:

- 19 • *Increasing the reflectivity of a hotspot surface has the same effect as reducing greenhouse gases*
- 20 • *Decreasing the reflectivity of a hotspot surface has the same effect as increasing greenhouse*  
21 *gases*
- 22 • *The inherent global warming change associated with a reflectivity hotspot change is given by the*  
23 *albedo-GHG radiation factor having an approximate value of 1.6.*

24 This fundamental theorem is important because it leads one to the reality that conservatively, the albedo  
25 solution [1-5] is our fastest and safest method to stop climate change. From the theorem we can deduce:

- 26 • CO<sub>2</sub> mitigation is not optimum in reducing hotspots effects and has no effect on hydro-hotspots
- 27 • The albedo solution is effective in reducing hotspots, hydro-hotspots and CO<sub>2</sub> effects

28 Here we assume three dominant types of forcing due to

- 29 • CO<sub>2</sub> (ignoring other GHGs)
- 30 • Hotspots
- 31 • Hydro-hotspots

32 Carbon climatologist apparently assume that hotspot forcing is negligible and little is known about hydro-  
33 hotspot forcing where

- 34 • UHI and other impermeable surfaces create hydro-hotspots [6] which contribute to global  
35 warming. However, the level of hydro-hotspot significance is currently unknown. A hydro-  
36 hotspot is a solar hot surface that creates atmospheric water vapor in the presence of precipitation.  
37 Such surfaces create excess moisture in the atmosphere promoting a local greenhouse effect. For

38 example, Zhao et al. [7] observed that UHI temperatures increase in daytime  $\Delta T$  by 3.0°C in  
 39 humid climates but decreasing  $\Delta T$  by 1.5°C in dry climates.

40

41 The assumption that hotspots do not contribute significantly to global warming has been contested by  
 42 many authors as it relates to UHIs. This is now fully described both with measurements [8-19] and more  
 43 recently in modeling [4,20]. Furthermore, humankind has a lack of hotspot controls in the construction of  
 44 UHIs and impermeable surfaces which are increasing with population [20] growth at an alarming rate. In  
 45 this view, we have three dominate forcing issues, hotspots, hydro-hotspots and CO<sub>2</sub>.

- 46 • Thus, maintaining the carbon climatologist's argument that hotspots and hydro-hotspots forcing  
 47 are not significant, so that CO<sub>2</sub> must dominates, promotes associated risk in climate change  
 48 mitigation

49 Finally, there is no well-established scientific proof that CO<sub>2</sub> plays such a dominate role. One could argue  
 50 that hydro-hotspot increases are possibly more dominant in terms of greenhouse gas changes since the  
 51 industrial revolution. Therefore, the only way to reduce this risk is by adopting, at least in parallel, *albedo*  
 52 *solutions since according to this theorem, it guarantee success in mitigating all three types of forcing.*

53 Furthermore, we have growing concerns regarding

- 54 • slow progress reported in CO<sub>2</sub> reduction
- 55 • the yearly increases in reports on large desertification and deforestation occurring [21]
- 56 • Lack of hotspot and hydro-hotspot control [6]

57 One aspect of this theorem of interest is to demonstrate the albedo-GHG radiation 1.6 factor [4, 20] and  
 58 its change since the pre-industrial revolution. This factor must take into account all GHG increases  
 59 including hydro-hotspot changes. Such values relates to the effective emissivity constant of the planetary  
 60 system  $\beta^4$ . Because of its importance as it relates to the albedo-GHG mechanism, it is a primary focus in  
 61 the rest of this paper.

## 62 2. Method: Albedo-GHG Radiation Global Warming Pre-Industrial Factor

63

64 When initial solar absorption occurs, part of the long wavelength radiation given off is re-radiated back to  
 65 Earth. In the absence of forcing we denote this fraction as  $f_1$ . This presents a simplistic but effective  
 66 model

67

$$68 \quad P_{Pre-Industrial} = P_{\alpha} + P_{GHG} = P_{\alpha} + f_1 P_{\alpha} = P_{\alpha} (1 + f_1) = \sigma T_s^4 \quad \text{where} \quad P_{\alpha} = \frac{S_0}{4} (1 - \alpha) \quad (1)$$

69

70 and  $T_s$  is the surface temperature. As one might suspect,  $f_1$  turns out to be exactly  $\beta^4$  in the absence of  
 71 forcing, so that  $f_1$  is a redefined variable taken from the effective emissivity constant of the planetary  
 72 system. We identify  $1+f_1=1.618034$  as the pre-industrial albedo-GHG radiation factor (Table 1).

73 We identify the re-radiation 2019 having a value of  $1+f_2=1.6276$  (Table 1). That is, in 2019, due to  
 74 increases in GHGs, an increase in the re-radiation fraction occurs

75

$$76 \quad f_2 = f_{2019} = f_1 + \Delta f = \beta_1^4 + \Delta f \approx \beta_2^4 + \Delta f \quad (2)$$

77

78 In this way  $f_{2019}=f_2$  is a function of  $f_1$ . The RHS of Eq. 2 indicates that  $\beta_1 \approx \beta_2$  (see varication results in Eq.  
 79 18 and 19). We find that  $\Delta f=0.0096$  is relatively small compared to  $(1+f_1)$  which we show can fairly  
 80 accurate be assessed in geoenineering.

81

## 82 2.1 Basic Re-radiation Model and Estimating $f_1$

83

84 In geoengineering, we are working with absorption and re-radiation, we define

$$85 \quad P_{Total} = \sigma T_S^4 = \sigma \left( \frac{T_e}{\beta} \right)^4 \quad \text{and} \quad P_\alpha = \sigma T_\alpha^4 = \sigma (\beta T_S)^4 \quad (3)$$

86 The definitions of  $T_\alpha=T_e$ ,  $T_S$  and  $\beta$  are the emission temperature, surface temperature and typically  $\beta \approx 0.887$ ,  
 87 respectively. Consider a time when there is **no forcing issues** causing warming trends. Then by conservation of  
 88 energy, the equivalent power re-radiated from GHGs in this model is dependent on  $P_\alpha$  with

89

$$90 \quad P_{GHG} = P_{Total} - P_\alpha = \sigma T_S^4 - \sigma T_\alpha^4 \quad (4)$$

91

92 To be consistent with  $T_\alpha=T_e$ , since typically  $T_\alpha \approx 255^\circ\text{K}$  and  $T_S \approx 288^\circ\text{K}$ , then in keeping with a common definition of  
 93 the global beta (the proportionality between surface temperature and emission temperature) for the moment  
 94  $\beta = T_\alpha/T_S = T_e/T_S$ .

95

96 This allows us to write the dependence

97

$$98 \quad P_{GHG} = \sigma T_S^4 - \sigma T_\alpha^4 = \frac{\sigma T_\alpha^4}{\beta^4} - \sigma T_\alpha^4 = \sigma T_\alpha^4 \left( \frac{1}{\beta^4} - 1 \right) = \sigma T_\alpha^4 \left( \frac{1}{f} - 1 \right) \quad (5)$$

99

100 Note that when  $\beta^4=1$ , there are no GHG contributions. We note that  $f$ , the re-radiation parameter equals  $\beta^4$   
 101 in the absence of forcing.

102

103 We can also define the blackbody re-radiated by GHGs given by some fraction  $f_1$  such that

104

$$105 \quad P_{GHG} = f_1 P_\alpha = f_1 \sigma T_\alpha^4 \quad (6)$$

106

107 Consider  $f=f_1$ , in this case according to Equations 5 and 6, it requires

108

$$109 \quad P_{GHG} = \sigma T_\alpha^4 \left( \frac{1}{f_1} - 1 \right) = f_1 \sigma T_\alpha^4 \quad (7)$$

110

111 This dependence leads us to the solution of the quadratic expression

112

$$113 \quad f_1^2 + f_1 - 1 = 0 \quad \text{yielding} \quad f_1 = 0.618034 = \beta^4, \quad \beta = (0.618034)^{1/4} = 0.886652 \quad (8)$$

114

115 This is very close to the common value estimated for  $\beta$  and this has been obtained through energy balance  
 116 in the planetary system providing a self-determining assessment. In geoengineering we can view the re-  
 117 radiation as part of the albedo effect. Consistency with the Planck parameter is shown in Section 3.1. We  
 118 note that the assumption  $f=f_1$  only works if planetary energy is in balance without forcing. In the next  
 119 section, we double check this model in another way by balancing energy in and out of our global system.

120

## 121 2.2 Balancing Pout and Pin in 1950

122

123 In equilibrium the radiation that leaves must balance  $P_\alpha$ , the energy absorbed, so that

124

$$125 \quad \begin{aligned} Energy_{out} &= (1-f_1)P_\alpha + (1-f_1)P_{Total} = (1-f_1)P_\alpha + (1-f_1)\{P_\alpha + f_1P_\alpha\} \\ &= 2P_\alpha - f_1P_\alpha - f_1^2P_\alpha = Energy_{in} = P_\alpha \end{aligned} \quad (9)$$

126

127 This is consistent, so that in 1950, Eq. 9 requires the same quadratic solution as Eq. 8. It is also apparent  
 128 that

129

$$130 \quad P_{\alpha} = f_1 P_{Total\_1950} = \beta_1^4 P_{Total\_1950} \quad (10)$$

131 since  
132

$$133 \quad P_{\alpha} = f_1(P_{\alpha} + f_1 P_{\alpha}) \text{ or } 1 = f_1(1 + f_1) \quad (11)$$

134 The RHS of Eq. 11 is Eq. 8. This illustrates  $f_1$  from another perspective as the fractional amount of total  
135 radiation in equilibrium. As a final check, the application in the next Section in Table 1, illustrate that  $f_1$   
136 provides reasonable results.  
137  
138

### 139 **2.3 Re-radiation Model Applied to 2019**

140 In 2019 due to global warming trends, to apply the model we assume that feedback can be applied as a  
141 separate term and we make use of some IPCC estimates for GHG forcing as a way to calibrate our model.  
142 In the traditional sense of forcing, we assume some small change to the albedo and most of the forcing  
143 due to IPCC estimates for GHGs where  
144

$$145 \quad P_{Total2019} = P_{\alpha'} + P_{GHG'} = P_{\alpha'}(1 + f_2) \quad (12)$$

146 Then we introduce feedback through an amplification factor  $A_F$  as follows  
147

$$148 \quad P_{Total2019\&Feedback} = P_{1950} + (\Delta P) A_F = P_{1950} + (P_{2019} - P_{1950}) A_F = \sigma T_S^4 \quad (13)$$

149 Here, we assume a small change in the albedo denoted as  $P_{\alpha}'$  and  $f_2$  is adjusted to the IPCC GHG forcing  
150 value estimated between 1950 and 2019 of  $2.38W/m^2$  [22]. Then the feedback amplification factor, is  
151 calibrated so that  $T_S=T_{2019}$  (see Table 1) yielding  $A_F=2.022$  [also see ref. 23]. The main difference in our  
152 model is that the forcing is about 6% higher than the IPCC for this period. Here, we take into account a  
153 small albedo decline of 0.15% that the author has estimated in another study due to likely issues from  
154 UHIs [20] and their coverage. We note that unlike  $f_1$ ,  $f_2$  is not a strict measure of the emissivity due the  
155 increase in GHGs.  
156

### 157 **3. Results Applied to 1950 and 2019 with an Estimate for $f_2$**

158 In 1950 we will simplify estimates by assuming the re-radiation parameter is fixed at the pre-industrial  
159 level of  $f_1=0.618034$ . Then, to obtain the average surface temperature  $T_{1950}=13.89^{\circ}C$  ( $287.04^{\circ}K$ ), the only  
160 adjustable parameter left in our basic model is the global albedo. This requires an albedo value of 0.3008  
161 (see Table 1) to obtain  $T_{1950}=287.04^{\circ}K$ . This albedo number is reasonable and similar to values cited in  
162 the literature [24].  
163

164 In 2019, the average temperature of the Earth is  $T_{2019}=14.84^{\circ}C$  ( $287.99^{\circ}K$ ) given in Eq. 15. We have  
165 assumed a small change in the Earth's albedo due to UHIs [20]. The  $f_2$  parameter is adjusted to 0.6276 to  
166 obtain the GHG forcing shown in Column 7 of  $2.38W/m^2$  [23]. Therefore the next to last row in Table 1 is  
167 a summary without feedback, and the last row incorporated the  $A_F=2.022$  feedback amplification factor.  
168

169 From Table 1 we now have identified the reverse forcing at the surface needed since  
170

$$171 \quad P_{Total2019\_Feedback\ Amp} = P_{1950} + (P_{2019} - P_{1950}) A_F = 384.927W / m^2 + (2.5337W / m^2) 2.022 = 390.05W / m^2 \quad (14)$$

172 and  
173

$$174 \quad \Delta T_S = T_{2019} - T_{1950} = (390.05 / \sigma)^{1/4} - 287.04^{\circ}K = 287.9899^{\circ}K - 287.04^{\circ}K = 0.95^{\circ}K \quad (15)$$

175 as modeled. We also note an estimate has now been obtained in Table 1 for  $f_2=0.6276$ ,  $A_F=2.022$ , and  
176  $\Delta P_{Total\_Feedback\_amp}=5.12W/m^2$ .  
177  
178  
179  
180  
181  
182

183

184

**Table 1 Model results**

Year	$T_s(^{\circ}K)$	$T_{\alpha}(^{\circ}K)$	$f_1, f_2$	$\alpha, \alpha'$	Power Absorbed $\frac{W}{m^2}$	$P_{GHG}$ $P_{GHG}$	$P_{Total}$ $\frac{W}{m^2}$
2019	287.5107	254.55	0.6276	30.03488	238.056	149.4041	387.4605
1950	287.04	254.51	0.6180	30.08	237.9028	147.024	384.9267
$\Delta_{2019-1950}$	0.471	0.041	0.0096	(0.15%)	0.15352	2.38	2.53
$\Delta_{Feedback}$ $A_F=2.022$	0.95	0.083	-	-	0.3104	4.81	5.12

185

186

**3.1 Model Consistency with the Planck Parameter**

188

189 As a measure of model consistency, the forcing change with feedback, and resulting temperatures  $T_{1950}$   
 190 and  $T_{2019}$ , should be in agreement with expected results using the Planck feedback parameter. From the  
 191 definition of the Planck parameter  $\lambda_o$  and results in Table 1, we estimate [25]

192

$$193 \quad \lambda_o = -4 \frac{\Delta R_{OLW}}{T_s} = -4 \left( \frac{237.9028 W / m^2}{287.041^{\circ}K} \right)_{1950} = -3.31524 W / m^2 / ^{\circ}K \quad (16)$$

194 and

$$195 \quad \lambda_o = -4 \frac{\Delta R_{OLW}}{T_s} = -4 \left( \frac{238.056 W / m^2}{287.99^{\circ}K} \right)_{2019} = -3.306 W / m^2 / ^{\circ}K \quad (17)$$

196

197 Here  $\Delta R_{OLW}$  is the outgoing long wave radiation change. We note these are very close in value showing  
 198 minor error and consistency with Planck parameter value, often taken as  $3.3 W/m^2/^{\circ}K$ .

199

200 Also note the Betas are very consistent with Eq. 8 for the two different time periods since from Table 1

201

$$202 \quad \beta_{1950} = \frac{T_{\alpha}}{T_s} = \frac{T_e}{T_s} = \frac{254.51}{287.041} = 0.88667 \text{ and } \beta_{1950}^4 = 0.6180785 \quad (18)$$

203

204 and

$$206 \quad \beta_{2019} = \frac{T_{\alpha}}{T_s} = \frac{T_e}{T_s} = \frac{254.55}{287.5107} = 0.88526 \text{ and } \beta_{2019}^4 = 0.6144 \quad (19)$$

207

**4 Summary**

209 In this paper we have devised a greenhouse gas albedo surface theorem. The theorem includes a re-  
 210 radiation factor which has been fully described and applied to two time periods. Results show that the re-  
 211 radiation factor for 1950 is taken as a pre-industrial value of 1.6181 while in present day the factor has  
 212 increase to 1.6276 due to the increase in GHGs.

213 We suggest the theorem, when applied to the reality of today's challenges, appears to indicate that the  
 214 albedo solution would be the safest and fastest way to mitigate climate change. Furthermore, the theorem  
 215 indicates that focusing solely on the CO2 solution is unrealistic and puts our planet at risk when three  
 216 types of forcing are considered.

**References**

- 218 1. Dunne D, (2018) Six ideas to limit global warming with solar geoengineering, CarbonBrief,  
 219 <https://www.carbonbrief.org/explainer-six-ideas-to-limit-global-warming-with-solar-geoengineering>

- 220 2. Cho A, (2016) To fight global warming, Senate calls for study of making Earth reflect more light, Science,  
 221 <https://www.sciencemag.org/news/2016/04/fight-global-warming-senate-calls-study-making-earth-reflect->  
 222 more-light
- 223 3. Levinson, R., Akbari, H. (2010) Potential benefits of cool roofs on commercial buildings: conserving energy,  
 224 saving money, and reducing emission of greenhouse gases and air pollutants. *Energy Efficiency* 3, 53–109.  
 225 <https://doi.org/10.1007/s12053-008-9038-2>
- 226 4. Feinberg A., On Geoengineering and Implementing an Albedo Solution with UHI GW and Cooling  
 227 Estimates vixra 2006.0198, DOI: 10.13140/RG.2.2.26006.37444/6 (Currently in Peer Review in the  
 228 J. Mitigation and Adaptation Strategies for Global Change)
- 229 5. Feinberg A., The Reflectivity (Albedo) Solution Urgently Needed to Stop Climate Change,  
 230 Youtube, August 2020
- 231 6. **Feinberg A** (2020) Review of Global Warming Urban Heat Island Forcing Issues Unaddressed by IPCC  
 232 Suggestions Including CO2 Doubling Estimates, viXra:2001.0415
- 233 7. Zhao L, Lee X, Smith RB, Oleson K (2014) Strong, contributions of local background climate to urban heat  
 234 islands, *Nature*. 10;511(7508):216-9. doi: 10.1038/nature13462
- 235 8. McKittrick R. and Michaels J. (2004) A Test of Corrections for Extraneous Signals in Gridded Surface  
 236 Temperature Data, *Climate Research*
- 237 9. McKittrick R., Michaels P. (2007) Quantifying the influence of anthropogenic surface processes and  
 238 inhomogeneities on gridded global climate data, *J. of Geophysical Research-Atmospheres*.
- 239 10. Schmidt GA, (2009) Spurious correlations between recent warming and indices of local economic activity,  
 240 *Int. J. of Climatology*
- 241 11. Zhao ZC (1991) Temperature change in China for the last 39 years and urban effects. *Meteorological*  
 242 *Monthly* (in Chinese), 17(4), 14-17.
- 243 12. Feddema JJ, Oleson KW, Bonan GB, Mearns LO, Buja LE, Meehl GA, and Washington WM (2005) The  
 244 importance of land-cover change in simulating future climates, *Science*, 310, 1674– 1678,  
 245 doi:10.1126/science.1118160
- 246 13. Ren G, Chu Z, Chen Z, Ren Y (2007) Implications of temporal change in urban heat island intensity observed  
 247 at Beijing and Wuhan stations. *Geophys. Res. Lett.* , 34, L05711,doi:10.1029/2006GL027927.
- 248 14. Ren, GY, Chu ZY, and Zhou JX (2008) Urbanization effects on observed surface air temperature in North  
 249 China. *J. Climate*, 21, 1333-1348
- 250 15. Jones PD, Lister DH, and Li QX, (2008) Urbanization effects in large-scale temperature records, with an  
 251 emphasis on China. *J. Geophys. Res.*, 113, D16122, doi: 10.1029/2008JD009916.
- 252 16. Stone B (2009) Land use as climate change mitigation, *Environ. Sci. Technol.*, 43( 24), 9052– 9056,  
 253 doi:10.1021/es902150g
- 254 17. Zhao, ZC (2011) Impacts of urbanization on climate change. in: 10,000 Scientific Difficult Problems: Earth  
 255 Science, 10,000 scientific difficult problems Earth Science Committee Eds., Science Press, 843-846. 30%
- 256 18. Yang X, Hou Y, Chen B (2011) Observed surface warming induced by urbanization in east China. *J.*  
 257 *Geophys. Res. Atmos*, 116, doi:10.1029/2010JD015452.
- 258 19. Huang Q, Lu Y (2015) Effect of Urban Heat Island on Climate Warming in the Yangtze River Delta Urban  
 259 Agglomeration in China, *Intern. J. of Environmental Research and Public Health* 12 (8): 8773 (30%)
- 260 20. Feinberg A, (2020) Urban Heat Island Amplification Estimates on Global Warming Using an Albedo Model,  
 261 Vixra 2003.0088, DOI: 10.13140/RG.2.2.32758.14402/15 (Currently under peer review in the journal SN  
 262 Applied Science)
- 263 21. Deforestation, Wikipedia, <https://en.wikipedia.org/wiki/Deforestation>
- 264 22. Butler JH, Montzka SA, (2020) The NOAA Annual Greenhouse Gas Index, Earth System Research Lab.  
 265 Global Monitoring Laboratory, <https://www.esrl.noaa.gov/gmd/aggi/aggi.html>
- 266 23. Dessler AE, Zhang Z, Yang P (2008) Water-vapor climate feedback inferred from climate fluctuations, 2003–  
 267 2008, *Geophysical Research Letters*, <https://doi.org/10.1029/2008GL035333>
- 268 24. [Stephens G, O'Brien D, Webster P, Pilewski P, Kato S, Li J](https://doi.org/10.1002/2014RG000449), (2015) The albedo of Earth, *Rev. of Geophysics*,  
 269 <https://doi.org/10.1002/2014RG000449>
- 270 25. Kimoto K (2006) On the Confusion of Planck Feedback Parameters, *Energy & Environment* (2009)
- 271