

# Polynomials Generating Prime Numbers No.2

Yukihiro Sano

## Abstract

In the Ulam spiral, there are places where prime numbers appear continuously on line. Integers are arranged in a square spiral in the Ulam spiral. I thought that if integers are arranged differently, other continuous prime numbers would appear. Therefore, I arrange integers in the angles of 45, 90, 135, 180, 225, 270, 315, 153, 160 degrees, hexagonal arrangement etc.. Then, prime numbers appeared continuously on line.

Looking at the prime numbers vertical column of Euler's polynomial generating prime numbers, that I created in the hexagonal 90 degrees arrangement, I think how far the continuous numbers will continue if Euler prime numbers is selected to skip by 2 or skip by 3 etc., avoiding the value where the continuous prime number is interrupted, and I investigate. As a result, I found many polynomials generating 40 to 10 consecutive prime numbers.

## Contents

|          |   |          |
|----------|---|----------|
| <b>1</b> | <b>Introduction</b>                             | <b>2</b> |
| <b>2</b> | <b>Polynomials generating prime numbers</b>     | <b>3</b> |
| 2.1      | The Ulam spiral                                 | 3        |
| 2.2      | Polynomial generating prime numbers 1           | 3        |
| 2.3      | Polynomial generating prime numbers 2           | 3        |
| 2.4      | Polynomial generating prime numbers 3           | 4        |
| 2.5      | Euler's polynomial generating prime numbers     | 4        |
| <b>3</b> | <b>New polynomials generating prime numbers</b> | <b>4</b> |
| 3.1      | New polynomial generating prime numbers 1       | 5        |
| 3.2      | New polynomial generating prime numbers 2       | 6        |
| 3.3      | New polynomial generating prime numbers 3       | 7        |
| 3.4      | New polynomial generating prime numbers 4       | 7        |
| 3.5      | New polynomial generating prime numbers 5       | 8        |

|          |  |    |
|----------|--|----|
| 3.6      | New polynomial generating prime numbers 6                      | 9  |
| 3.7      | New polynomial generating prime numbers 7                      | 9  |
| 3.8      | New polynomial generating prime numbers 8                      | 9  |
| 3.9      | New polynomial generating prime numbers 9                      | 9  |
| 3.10     | New polynomial generating prime numbers 10                     | 10 |
| 3.11     | New polynomial generating prime numbers 11                     | 10 |
| 3.12     | Other new polynomials generating prime numbers                 | 10 |
| 3.13     | Skipping numbers and continuous prime numbers                  | 18 |
| <b>4</b> | <b>List of Figures</b>   |    |
| 4.1      | Figure 2.1 The Ulam Spiral                                     | 19 |
| 4.2      | Figure 2.2 180 degrees Arrangement Legendre Polynomial         | 20 |
| 4.3      | Figure 2.3 135 degrees Arrangement Brox Polynomial             | 21 |
| 4.4      | Figure 2.4 270 degrees Arrangement Frame Polynomial            | 22 |
| 4.5      | Figure 2.5 90 degrees Arrangement Euler's Polynomial           | 23 |
| 4.6      | Figure 2.6 Hexagonal 90 degrees Arrangement Euler's Polynomial | 24 |
| 4.7      | Figure 3.1 Hexagonal 90 degrees Arrangement Euler's Polynomial | 25 |
| <b>5</b> | <b>Consideration</b>   | 26 |
| <b>6</b> | <b>Acknowledgment</b>  | 26 |
|          | <b>References</b>  | 26 |

## 1 Introduction

I was interested in prime numbers looking at the Ulam spiral, I analyzed it myself. And I learned that Euler's polynomial generating prime numbers is simple and great. I thought that other polynomials generating prime numbers may be found in other arrangements, I investigate.

Looking at the prime numbers vertical column of Euler's polynomial generating prime numbers, that I created in the hexagonal 90 degrees arrangement, I think how far the continuous numbers will continue if Euler prime numbers is selected to skip by 2 or skip by 3 etc., avoiding the value where the continuous prime number is interrupted, and I investigate. As a result, I found many polynomials generating 40 to 10 consecutive prime numbers and I collect the results.

These algebraic polynomials have the property that for  $n = 0, 1, \dots, m-1$  value of the polynomial, eventually in module, are  $m$  primes.

## 2 Polynomials generating prime numbers

### 2.1 The Ulam spiral

In the Ulam spiral, there are places where prime numbers appear continuously on line. I noticed that there are places where prime numbers appear continuously in a certain pattern in the Ulam spiral, although they do not appear continuously on line. There are two polynomials,  $P(n) = 4n^2 + 2n + 41$  and  $P(n) = 4n^2 + 6n + 43$ , generates 20 primes, see Figure 2.1. Each value is a value obtained by skipping by 1 of Euler prime numbers. When the values of the two polynomials are inserted alternately, the values are the same as values of Euler prime numbers, see Figure 2.1.

### 2.2 Polynomial generating prime numbers 1

Integers are arranged in a square spiral in the Ulam spiral, but I thought that if integers are arranged differently, other continuous prime numbers would appear. Therefore, I arrange integers in the angles of 45, 90, 135, 180, 225, 270, 315, 153, 160 degrees, hexagonal arrangement etc., using a computer. Then, prime numbers appeared continuously on line.

In 180 degrees arrangement, see Figure 2.2, 29 prime numbers appear continuously. It was prime numbers of Legendre polynomial [1798],  $P(n) = 2n^2 + 29$ , generates 29 primes: 29, 31, 37, 47, 61, 79, 101, 127, 157, 191, 229, 271, 317, 367, 421, 479, 541, 607, 677, 751, 829, 911, 997, 1087, 1181, 1279, 1381, 1487, 1597 .

### 2.3 Polynomial generating prime numbers 2

In 135 degrees arrangement, see Figure 2.3, 29 prime numbers appear continuously. It was prime numbers of Brox polynomial [2006],  $P(n) = 6n^2 - 342n + 4903$  ( or  $6n^2 + 6n + 31$  ), generates 29 primes: 4903, 4567, 4243, 3931, 3631, 3343, 3067, 2803, 2551, 2311, 2083, 1867, 1663, 1471, 1291, 1123, 967, 823, 691, 571, 463, 367, 283, 211, 151, 103, 67, 43, 31 . Also, in Figure 2.3, prime numbers of polynomials,  $P(n) = 6n^2 + 6n + p$ ,  $p$  are lucky numbers  $p = 5, 7, 11, 17, 31$ , are clearly appeared. In addition, prime numbers of polynomials,  $P(n) = 6n^2 + p$ ,  $p$  are lucky numbers  $p = 5, 7, 13, 17$ , are clearly appeared.

## 2.4 Polynomial generating prime numbers 3

In 270 degrees arrangement, see Figure 2.4, 22 prime numbers appear continuously. It was prime numbers of Frame polynomial [2018],  $P(n) = 3n^2 + 3n + 23$ , generates 22 primes: 23, 29, 41, 59, 83, 113, 149, 191, 239, 293, 353, 419, 491, 569, 653, 743, 839, 941, 1049, 1163, 1283, 1409 .

## 2.5 Euler's polynomial generating prime numbers

In 90 degrees arrangement, see Figure 2.5 and the hexagonal 90 degrees arrangement, see Figure 2.6 (illustrated as a rectangle for simplification in Figure 2.6), 40 prime numbers appear continuously. It was prime numbers of Euler's polynomial [1772],  $P(n) = n^2 + n + 41$ , generates 40 primes: 41, 43, 47, 53, 61, 71, 83, 97, 113, 131, 151, 173, 197, 223, 251, 281, 313, 347, 383, 421, 461, 503, 547, 593, 641, 691, 743, 797, 853, 911, 971, 1033, 1097, 1163, 1231, 1301, 1373, 1447, 1523, 1601 .

Also, prime numbers of polynomial,  $P(n) = n^2 + n + p$ ,  $p$  are Euler's lucky numbers  $p = 3, 5, 11, 17, 41$ , are clearly appeared.

## 3 New polynomials generating prime numbers

Looking at the vertical column of  $n^2 + n + 17$  with the lucky number  $p = 17$  of Euler's polynomial generating prime numbers in Figure 2.6 that I created, this vertical column has many prime numbers, but they are not used much in the polynomial generating prime numbers. The last value of the continuous prime number of  $n^2 + n + 17$  is 257. I thought that if I selected 257, 359, 479 to skip by 2 in this column, I may have polynomials generating prime numbers with many consecutive numbers, because there are many prime numbers in this vertical column. With the spirit of "mottainai" in Japan, the intention is to make use of 257, 359, 479. Then, the polynomial of Section 3.12.10 was found. After that, since the vertical column of Euler's polynomial generating prime numbers ,  $n^2 + n + 41$  has many prime numbers, I think how far the continuous numbers will continue if Euler prime numbers is selected to skip by 2 or skip by 3 etc., avoiding the value of 1681, 1763, 2021 where the continuous prime number is interrupted, and I investigate. As a result, I found many polynomials generating 40 to 10 consecutive prime numbers and I collect the results.

### 3.1 New polynomial generating prime numbers 1

Figure 3.1 shows the same contents as Figure 2.6, but Figure 3.1 is easy to see the values. In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I avoid 1681, 1763, 2021 of non-prime numbers and I calculate polynomial including 1601, 1847, 2111 of 2 skipped numbers. 971, 1163, 1373, 1601, 1847, 2111 are prime numbers. Polynomial generating these prime numbers is calculated. The method of calculating polynomial is as follows.

|   |  |  |   |
|---|--|--|---|
| $\begin{array}{c} 971 \\ \quad \left[ \begin{array}{c} 192 \\ 1163 \\ \quad \left[ \begin{array}{c} 210 \\ 1373 \\ \quad \left[ \begin{array}{c} 228 \\ 1601 \\ \quad \left[ \begin{array}{c} 246 \\ 1847 \\ \quad \left[ \begin{array}{c} 264 \\ 2111 \end{array} \right] \end{array} \right] \end{array} \right] \end{array} \right] \end{array}$ | $\begin{array}{c} 971 \\ 18 \\ 18 \\ 18 \\ 18 \\ 18 \\ 2111 \end{array}$ | $\begin{array}{l} 1163 = 971 + 192 \\ \quad = 971 + 192 \times 1 \\ 1373 = (971 + 192) + (192 + 18) \\ \quad = 971 + 192 \times 2 + 18 \times 1 \\ 1601 = (971 + 192) + (192 + 18) + (192 + 18 + 18) \\ \quad = 971 + 192 \times 3 + 18 \times 3 \\ 1847 = (971 + 192) + (192 + 18) + (192 + 18 + 18) + (192 + 18 + 18 + 18) \\ \quad = 971 + 192 \times 4 + 18 \times 6 \\ 2111 = (971 + 192) + (192 + 18) + (192 + 18 + 18) + (192 + 18 + 18 + 18) + (192 + 18 + 18 + 18) = 971 + 192 \times 5 + 18 \times 10 \end{array}$ | $\begin{array}{c} n=0 \\ n=1 \\ n=2 \\ n=3 \\ n=4 \\ n=5 \end{array}$ |
|   |  | $f(n) = 971 + 192n + 18xn(n-1)/2 = 971 + 192n + 9n^2 - 9n = 9n^2 + 183n + 971$   |   |

It can be confirmed later that this polynomial is prime numbers even if  $n = -1$  to  $-23$ , so I insert  $n=n-23$ ,

$$\begin{aligned} f(n) &= 9(n-23)^2 + 183(n-23) + 971 = 9n^2 - 9x2x23n + 9x23x23 + 183n - 183x23 + 971 \\ &= 9n^2 - 414n + 4761 + 183n - 4209 + 971 = 9n^2 - 231n + 1523 \quad (n=0, 1, \dots, 28) \end{aligned}$$

And it can be confirmed later that this polynomial is prime numbers even if  $n = 29$  to  $39$ .

This is polynomial generating 40 prime numbers.

$P(n) = 9n^2 - 231n + 1523$ , generates 40 primes: 1523, 1301, 1097, 911, 743, 593, 461, 347, 251, 173, 113, 71, 47, 41, 53, 83, 131, 197, 281, 383, 503, 641, 797, 971, 1163, 1373, 1601, 1847, 2111, 2393, 2693, 3011, 3347, 3701, 4073, 4463, 4871, 5297, 5741, 6203 .

The values of 1523 to 47 in the first half of the above value and 41 to 1601 in the middle part are the values of Euler prime numbers skipped by 2, and the values in the latter half are prime numbers larger than the maximum Euler prime number 1601.

### 3.2 New polynomial generating prime numbers 2

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1163, 1523, 1933 of 4 skipped numbers. 383, 593, 853, 1163, 1523, 1933 are prime numbers. Polynomial generating these prime numbers is calculated. The method of calculating polynomial is as follows.

|   |  |   |  |
|---|--|---|--|
| $\begin{array}{c} 383 \\   \\ 210 \\   \\ 593 \\   \\ 260 \\   \\ 853 \\   \\ 310 \\   \\ 1163 \\   \\ 360 \\   \\ 1523 \\   \\ 410 \\   \\ 1933 \end{array}$ | $\begin{array}{c} 383 \\   \\ 50 \\   \\ 50 \\   \\ 50 \\   \\ 50 \\   \\ 50 \\   \\ 50 \\   \\ 50 \\   \\ 50 \end{array}$ | $\begin{aligned} & 383 \\ & 593 = 383 + 210 \\ & \quad = 383 + 210 \times 1 \\ & 853 = (383 + 210) + (210 + 50) \\ & \quad = 383 + 210 \times 2 + 50 \times 1 \\ & 1163 = (383 + 210) + (210 + 50) + (210 + 50 + 50) \\ & \quad = 383 + 210 \times 3 + 50 \times 3 \\ & 1523 = (383 + 210) + (210 + 50) + (210 + 50 + 50) + (210 + 50 + 50 + 50) \\ & \quad = 383 + 210 \times 4 + 50 \times 6 \\ & 1933 = (383 + 210) + (210 + 50) + (210 + 50 + 50) + (210 + 50 + 50 + 50) \\ & \quad \quad \quad + (210 + 50 + 50 + 50) = 383 + 210 \times 5 + 50 \times 10 \end{aligned}$ | $n=0$<br>$n=1$<br>$n=2$<br>$n=3$<br>$n=4$<br>$n=5$ |
|   |  | $\begin{aligned} f(n) &= 383 + 210n + 50xn(n-1)/2 = 383 + 210n + 25n^2 - 25n \\ &= 25n^2 + 185n + 383 \end{aligned}$  |  |

It can be confirmed later that this polynomial is prime numbers even if  $n = -1$  to  $-11$ , so I insert  $n=n-11$ ,

$$\begin{aligned} f(n) &= 25(n-11)^2 + 185(n-11) + 383 = 25n^2 - 25 \times 2 \times 11n + 25 \times 11 \times 11 + 185n - 185 \times 11 + 383 \\ &= 25n^2 - 550n + 3025 + 185n - 2035 + 383 = 25n^2 - 365n + 1373 \quad (n=0, 1, \dots, 16) \end{aligned}$$

And it can be confirmed later that this polynomial is prime numbers even if  $n = 17$  to  $31$ .

This is polynomial generating 32 prime numbers.

$P(n) = 25n^2 - 365n + 1373$ , generates 32 primes: 1373, 1033, 743, 503, 313, 173, 83, 43, 53, 113, 223, 383, 593, 853, 1163, 1523, 1933, 2393, 2903, 3463, 4073, 4733, 5443, 6203, 7013, 7873, 8783, 9743, 10753, 11813, 12923, 14083 .

### 3.3 New polynomial generating prime numbers 3

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1301, 1601, 1933 of 3 skipped numbers. 593, 797, 1033, 1301, 1601, 1933 are prime numbers. Polynomial generating these prime numbers is calculated. The method of calculating polynomial is as follows.

|   |   |  |
|---|---|--|
| 593<br>204<br>797<br>236<br>1033<br>268<br>1301<br>300<br>1601<br>332<br>1933 | 593<br><br>32 $797 = 593 + 204$<br>= $593 + 204 \times 1$<br><br>32 $1033 = (593 + 204) + (204 + 32)$<br>= $593 + 204 \times 2 + 32 \times 1$<br><br>32 $1301 = (593 + 204) + (204 + 32) + (204 + 32 + 32)$<br>= $593 + 204 \times 3 + 32 \times 3$<br><br>32 $1601 = (593 + 204) + (204 + 32) + (204 + 32 + 32) + (204 + 32 + 32 + 32)$<br>= $593 + 204 \times 4 + 32 \times 6$<br><br>1933 $1933 = (593 + 204) + (204 + 32) + (204 + 32 + 32) + (204 + 32 + 32 + 32)$<br>+ $(204 + 32 + 32 + 32) = 593 + 204 \times 5 + 32 \times 10$ | n=0<br><br>n=1<br><br>n=2<br><br>n=3<br><br>n=4<br><br>n=5 |
|   | $f(n) = 593 + 204n + 32xn(n-1)/2 = 593 + 204n + 16n^2 - 16n$<br>$= 16n^2 + 188n + 593$  |  |

It can be confirmed later that this polynomial is prime numbers even if  $n = -1$  to  $-15$ , so I

insert  $n = -15$ ,

$$\begin{aligned} f(n) &= 16(-15)^2 + 188(-15) + 593 = 16n^2 - 16x2x15n + 16x15x15 + 188n - 188x15 + 593 \\ &= 16n^2 - 480n + 3600 + 188n - 2820 + 593 = 16n^2 - 292n + 1373 \quad (n=0, 1, \dots, 20) \end{aligned}$$

And it can be confirmed later that this polynomial is prime numbers even if  $n = 21$  to  $30$ .

This is polynomial generating 31 prime numbers.

$P(n) = 16n^2 - 292n + 1373$ , generates 31 primes: 1373, 1097, 853, 641, 461, 313, 197, 113, 61, 41, 53, 97, 173, 281, 421, 593, 797, 1033, 1301, 1601, 1933, 2297, 2693, 3121, 3581, 4073, 4597, 5153, 5741, 6361, 7013 .

### 3.4 New polynomial generating prime numbers 4

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1231, 1523, 1847 of 3 skipped numbers. 547, 743,

971, 1231, 1523, 1847 are prime numbers. Polynomial generating these prime numbers is calculated. The method of calculating polynomial is as follows.

|      |     |   |       |
|------|-----|---|-------|
|      | 547 |   | $n=0$ |
|      | 196 |   |       |
| 743  | 32  | 743=547+196   | $n=1$ |
|      | 228 | =547+196x1  |       |
| 971  | 32  | 971=(547+196)+(196+32)  | $n=2$ |
|      | 260 | =547+196x2+32x1   |       |
| 1231 | 32  | 1231=(547+196)+(196+32)+(196+32+32)   | $n=3$ |
|      | 292 | =547+196x3+32x3   |       |
| 1523 | 32  | 1523=(547+196)+(196+32)+(196+32+32)+(196+32+32+32)                                    | $n=4$ |
|      | 324 | =547+196x4+32x6   |       |
| 1847 |     | 1847=(547+196)+(196+32)+(196+32+32)+(196+32+32+32)+<br>(196+32+32+32)=547+196x5+32x10 | $n=5$ |
|      |     | $f(n)=547+196n+32xn(n-1)/2=547+196n+16n^2-16n$  |       |
|      |     | $=16n^2+180n+547$   |       |

It can be confirmed later that this polynomial is prime numbers even if  $n = -1$  to  $-15$ , so I insert  $n=n-15$ ,

$$\begin{aligned} f(n) &= 16(n-15)^2 + 180(n-15) + 547 = 16n^2 - 16x2x15n + 16x15x15 + 180n - 180x15 + 547 \\ &= 16n^2 - 480n + 3600 + 180n - 2700 + 547 = 16n^2 - 300n + 1447 \quad (n=0, 1, \dots, 20) \end{aligned}$$

And it can be confirmed later that this polynomial is prime numbers even if  $n = 21$  to  $29$ .

This is polynomial generating 30 prime numbers.

$P(n) = 16n^2 - 300n + 1447$ , generates 30 primes: 1447, 1163, 911, 691, 503, 347, 223, 131, 71, 43, 47, 83, 151, 251, 383, 547, 743, 971, 1231, 1523, 1847, 2203, 2591, 3011, 3463, 3947, 4463, 5011, 5591, 6203 .

### 3.5 New polynomial generating prime numbers 5

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 691, 1231, 1933 of 8 skipped numbers. 43, 97, 313, 691, 1231, 1933 are prime numbers. Since the method of obtaining the polynomial is the same as the method described above, so I will omit below.

This is polynomial generating 28 prime numbers.

$P(n) = 81n^2 - 1323n + 5443$ , generates 28 primes: 5443, 4201, 3121, 2203, 1447, 853, 421, 151, 43, 97, 313, 691, 1231, 1933, 2797, 3823, 5011, 6361, 7873, 9547, 11383, 13381, 15541, 17863, 20347, 22993, 25801, 28771 .

### 3.6 New polynomial generating prime numbers 6

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 853, 1447, 2203 of 8 skipped numbers.

This is polynomial generating 28 prime numbers.

$P(n) = 81n^2 - 3051n + 28771$ , generates 28 primes: 28771, 25801, 22993, 20347, 17863, 15541, 13381, 11383, 9547, 7873, 6361, 5011, 3823, 2797, 1933, 1231, 691, 313, 97, 43, 151, 421, 853, 1447, 2203, 3121, 4201, 5443 .

Note that the above values are the same as in Section 3.5 and they will appear in reverse order, like mirror.

### 3.7 New polynomial generating prime numbers 7

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 911, 1373, 1933 of 6 skipped numbers.

This is polynomial generating 23 prime numbers.

$P(n) = 49n^2 - 469n + 1163$ , generates 23 primes: 1163, 743, 421, 197, 71, 43, 113, 281, 547, 911, 1373, 1933, 2591, 3347, 4201, 5153, 6203, 7351, 8597, 9941, 11383, 12923, 14561 .

### 3.8 New polynomial generating prime numbers 8

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 911, 1447, 2111 of 7 skipped numbers.

This is polynomial generating 23 prime numbers.

$P(n) = 64n^2 - 1192n + 5591$ , generates 23 primes: 5591, 4463, 3463, 2591, 1847, 1231, 743, 383, 151, 47, 71, 223, 503, 911, 1447, 2111, 2903, 3823, 4871, 6047, 7351, 8783, 10343 .

### 3.9 New polynomial generating prime numbers 9

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 743, 1231, 1847 of 7 skipped numbers.

This is polynomial generating 23 prime numbers.

$P(n) = 64n^2 - 1624n + 10343$ , generates 23 primes: 10343, 8783, 7351, 6047, 4871, 3823, 2903, 2111, 1447, 911, 503, 223, 71, 47, 151, 383, 743, 1231, 1847, 2591, 3463, 4463, 5591 .

Note that the above values are the same as in Section 3.8 and they will appear in reverse order, like mirror.

### 3.10 New polynomial generating prime numbers 10

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 971, 1373, 1847 of 5 skipped numbers.

This is polynomial generating 20 prime numbers.

$P(n) = 36n^2 - 426n + 1301$ , generates 20 primes: 1301, 911, 593, 347, 173, 71, 41, 83, 197, 383, 641, 971, 1373, 1847, 2393, 3011, 3701, 4463, 5297, 6203 .

### 3.11 New polynomial generating prime numbers 11

In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1163, 1601, 2111 of 5 skipped numbers.

This is polynomial generating 20 prime numbers.

$P(n) = 36n^2 - 462n + 1523$ , generates 20 primes: 1523, 1097, 743, 461, 251, 113, 47, 53, 131, 281, 503, 797, 1163, 1601, 2111, 2693, 3347, 4073, 4871, 5741 .

### 3.12 Other new polynomial generating prime numbers

**3.12.1** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 347, 853, 1601 of 10 skipped numbers.

This is polynomial generating 18 prime numbers.

$P(n) = 121n^2 - 1551n + 5011$ , generates 18 primes: 5011, 3581, 2393, 1447, 743, 281, 61, 83, 347, 853, 1601, 2591, 3823, 5297, 7013, 8971, 11171, 13613 .

**3.12.2** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 281, 743, 1447 of 10 skipped numbers.

This is polynomial generating 18 prime numbers.

$P(n) = 121n^2 - 2563n + 13613$ , generates 18 primes: 13613, 11171, 8971, 7013, 5297, 3823, 2591, 1601, 853, 347, 83, 61, 281, 743, 1447, 2393, 3581, 5011 .

**3.12.3** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 593, 1301, 2297 of 11 skipped numbers.

This is polynomial generating 18 prime numbers.

$P(n) = 144n^2 - 1740n + 5297$ , generates 18 primes: 5297, 3701, 2393, 1373, 641, 197, 41, 173, 593, 1301, 2297, 3581, 5153, 7013, 9161, 11597, 14321, 17333 .

**3.12.4** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 197, 641, 1373 of 11 skipped numbers.

This is polynomial generating 18 prime numbers.

$P(n) = 144n^2 - 3156n + 17333$ , generates 18 primes: 17333, 14321, 11597, 9161, 7013, 5153, 3581, 2297, 1301, 593, 173, 41, 197, 641, 1373, 2393, 3701, 5297 .

**3.12.5** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1097, 1601, 2203 of 6 skipped numbers.

This is polynomial generating 17 prime numbers.

$P(n) = 49n^2 - 525n + 1447$ , generates 17 primes: 1447, 971, 593, 313, 131, 47, 61, 173, 383, 691, 1097, 1601, 2203, 2903, 3701, 4597, 5591 .

**3.12.6** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 971, 1523, 2203 of 7 skipped numbers.

This is polynomial generating 17 prime numbers.

$P(n) = 64n^2 - 536n + 1163$ , generates 17 primes: 1163, 691, 347, 131, 43, 83, 251, 547, 971, 1523, 2203, 3011, 3947, 5011, 6203, 7523, 8971 .

**3.12.7** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 383, 853, 1523 of 9 skipped numbers.

This is polynomial generating 17 prime numbers.

$P(n) = 100n^2 - 630n + 1033$ , generates 17 primes: 1033, 503, 173, 43, 113, 383, 853, 1523, 2393, 3463, 4733, 6203, 7873, 9743, 11813, 14083, 16553 .

**3.12.8** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 593, 1163, 1933 of 9 skipped numbers.

This is polynomial generating 17 prime numbers.

$P(n) = 100n^2 - 930n + 2203$ , generates 17 primes: 2203, 1373, 743, 313, 83, 53, 223, 593, 1163, 1933, 2903, 4073, 5443, 7013, 8783, 10753, 12923 .

**3.12.9** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 743, 1373, 2203 of 9 skipped numbers.

This is polynomial generating 17 prime numbers.

$P(n) = 100n^2 - 2270n + 12923$ , generates 17 primes: 12923, 10753, 8783, 7013, 5443, 4073, 2903, 1933, 1163, 593, 223, 53, 83, 313, 743, 1373, 2203 .

**3.12.10** In Figure 3.1, in the  $n^2 + n + 17$  vertical column of Euler's polynomial generating prime with lucky number  $p = 17$ , I calculate polynomial including 257, 359, 479 of 2 skipped numbers.

This is polynomial generating 16 prime numbers.

$P(n) = 9n^2 - 87n + 227$ , generates 16 primes: 227, 149, 89, 47, 23, 17, 29, 59, 107, 173, 257, 359, 479, 617, 773, 947 .

**3.12.11** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1097, 1447, 1847 of 4 skipped numbers.

This is polynomial generating 16 prime numbers.

$P(n) = 25n^2 + 25n + 47$ , generates 16 primes: 47, 97, 197, 347, 547, 797, 1097, 1447, 1847, 2297, 2797, 3347, 3947, 4597, 5297, 6047 .

This polynomial generating prime number produces the same prime number even if  $n = -1$  to  $-16$ .

**3.12.12** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 797, 1301, 1933 of 7 skipped numbers.

This is polynomial generating 16 prime numbers.

$P(n) = 64n^2 - 584n + 1373$ , generates 16 primes: 1373, 853, 461, 197, 61, 53, 173, 421, 797, 1301, 1933, 2693, 3581, 4597, 5741, 7013 .

**3.12.13** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 797, 1447, 2297 of 9 skipped numbers.

This is polynomial generating 16 prime numbers.

$P(n) = 100n^2 - 1450n + 5297$ , generates 16 primes: 5297, 3947, 2797, 1847, 1097, 547, 197, 47, 97, 347, 797, 1447, 2297, 3347, 4597, 6047 .

**3.12.14** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 461, 1033, 1847 of 10 skipped numbers. This is polynomial generating 16 prime numbers.

$P(n) = 121n^2 - 1001n + 2111$ , generates 16 primes: 2111, 1231, 593, 197, 43, 131, 461, 1033, 1847, 2903, 4201, 5741, 7523, 9547, 11813, 14321 .

**3.12.15** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 593, 1231, 2111 of 10 skipped numbers. This is polynomial generating 16 prime numbers.

$P(n) = 121n^2 - 2629n + 14321$ , generates 16 primes: 14321, 11813, 9547, 7523, 5741, 4201, 2903, 1847, 1033, 461, 131, 43, 197, 593, 1231, 2111 .

**3.12.16** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 503, 1163, 2111 of 11 skipped numbers. This is polynomial generating 16 prime numbers.

$P(n) = 144n^2 - 2652n + 12251$ , generates 16 primes: 12251, 9743, 7523, 5591, 3947, 2591, 1523, 743, 251, 47, 131, 503, 1163, 2111, 3347, 4871 .

**3.12.17** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 197, 691, 1523 of 12 skipped numbers. This is polynomial generating 16 prime numbers.

$P(n) = 169n^2 - 1365n + 2797$ , generates 16 primes: 2797, 1601, 743, 223, 41, 197, 691, 1523, 2693, 4201, 6047, 8231, 10753, 13613, 16811, 20347 .

**3.12.18** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 223, 743, 1601 of 12 skipped numbers. This is polynomial generating 16 prime numbers.

$P(n) = 169n^2 - 3705n + 20347$ , generates 16 primes: 20347, 16811, 13613, 10753, 8231, 6047, 4201, 2693, 1523, 691, 197, 41, 223, 743, 1601, 2797 .

**3.12.19** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 593, 1033, 1601 of 7 skipped numbers. This is polynomial generating 15 prime numbers.

$P(n) = 64n^2 - 520n + 1097$ , generates 15 primes: 1097, 641, 313, 113, 41, 97, 281, 593, 1033, 1601, 2297, 3121, 4073, 5153, 6361 .

**3.12.20** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 911, 1523, 2297 of 8 skipped numbers. This is polynomial generating 15 prime numbers.

$P(n) = 81n^2 - 855n + 2297$ , generates 15 primes: 2297, 1523, 911, 461, 173, 47, 83, 281, 641, 1163, 1847, 2693, 3701, 4871, 6203 .

**3.12.21** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 911, 1523, 2297 of 8 skipped numbers. This is polynomial generating 15 prime numbers.

$P(n) = 81n^2 - 1413n + 6203$ , generates 15 primes: 6203, 4871, 3701, 2693, 1847, 1163, 641, 281, 83, 47, 173, 461, 911, 1523, 2297 .

**3.12.22** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 547, 1097, 1847 of 9 skipped numbers. This is polynomial generating 15 prime numbers.

$P(n) = 100n^2 - 1550n + 6047$ , generates 15 primes: 6047, 4597, 3347, 2297, 1447, 797, 347, 97, 47, 197, 547, 1097, 1847, 2797, 3947 .

**3.12.23** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 461, 1163, 2203 of 12 skipped numbers. This is polynomial generating 15 prime numbers.

$P(n) = 169n^2 - 819n + 1033$ , generates 15 primes: 1033, 383, 71, 97, 461, 1163, 2203, 3581, 5297, 7351, 9743, 12473, 15541, 18947, 22691 .

**3.12.24** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1033, 1447, 1933 of 5 skipped numbers. This is polynomial generating 14 prime numbers.

$P(n) = 36n^2 - 414n + 1231$ , generates 14 primes: 1231, 853, 547, 313, 151, 61, 43, 97, 223, 421, 691, 1033, 1447, 1933 .

**3.12.25** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 641, 1301, 2203 of 10 skipped numbers. This is polynomial generating 14 prime numbers.

$P(n) = 121n^2 - 671n + 971$ , generates 14 primes: 971, 421, 113, 47, 223, 641, 1301, 2203, 3347, 4733, 6361, 8231, 10343, 12697 .

**3.12.26** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 503, 1231, 2297 of 12 skipped numbers. This is polynomial generating 14 prime numbers.

$P(n) = 169n^2 - 1131n + 1933$ , generates 14 primes: 1933, 971, 347, 61, 113, 503, 1231, 2297, 3701, 5443, 7523, 9941, 12697, 15791 .

**3.12.27** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 347, 971, 1933 of 12 skipped numbers. This is polynomial generating 14 prime numbers.

$P(n) = 169n^2 - 3263n + 15791$ , generates 14 primes: 15791, 12697, 9941, 7523, 5443, 3701, 2297, 1231, 503, 113, 61, 347, 971, 1933 .

**3.12.28** In Figure 3.1, in the  $n^2 + n + 17$  vertical column of Euler's polynomial generating prime with lucky number  $p = 17$ , I calculate polynomial including 773, 1009, 1277 of 3 skipped numbers.

This is polynomial generating 13 prime numbers.

$P(n) = 16n^2 - 100n + 173$ , generates 13 primes: 173, 89, 37, 17, 29, 73, 149, 257, 397, 569, 773, 1009, 1277 .

**3.12.29** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 503, 971, 1601 of 8 skipped numbers. This is polynomial generating 13 prime numbers.

$P(n) = 81n^2 - 585n + 1097$ , generates 13 primes: 1097, 593, 251, 71, 53, 197, 503, 971, 1601, 2393, 3347, 4463, 5741 .

**3.12.30** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 797, 1373, 2111 of 8 skipped numbers. This is polynomial generating 13 prime numbers.

$P(n) = 81n^2 - 639n + 1301$ , generates 13 primes: 1301, 743, 347, 113, 41, 131, 383, 797, 1373, 2111, 3011, 4073, 5297 .

**3.12.31** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 1033, 1523, 2111 of 6 skipped numbers.

This is polynomial generating 12 prime numbers.

$P(n) = 49n^2 + 49n + 53$ , generates 126 primes: 53, 151, 347, 641, 1033, 1523, 2111, 2797, 3581, 4463, 5443, 6521 .

This polynomial generating prime number produces the same prime number even if  $n = -1$  to  $-12$ .

**3.12.32** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 853, 1301, 1847 of 6 skipped numbers.

This is polynomial generating 12 prime numbers.

$P(n) = 49n^2 - 483n + 1231$ , generates 12 primes: 1231, 797, 461, 223, 83, 41, 97, 251, 503, 853, 1301, 1847 .

**3.12.33** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 131, 547, 1301 of 12 skipped numbers.

This is polynomial generating 12 prime numbers.

$P(n) = 169n^2 - 1781n + 4733$ , generates 12 primes: 4733, 3121, 1847, 911, 313, 53, 131, 547, 1301, 2393, 3823, 5591 .

**3.12.34** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 313, 911, 1847 of 12 skipped numbers.

This is polynomial generating 12 prime numbers.

$P(n) = 169n^2 - 1937n + 5591$ , generates 12 primes: 5591, 3823, 2393, 1301, 547, 131, 53, 313, 911, 1847, 3121, 4733 .

**3.12.35** In Figure 3.1, in the  $n^2 + n + 17$  vertical column of Euler's polynomial generating prime with lucky number  $p = 17$ , I calculate polynomial including 479, 887, 1423 of 7 skipped numbers.

This is polynomial generating 11 prime numbers.

$P(n) = 64n^2 - 424n + 719$ , generates 11 primes: 719, 359, 127, 23, 47, 199, 479, 887, 1423, 2087, 2879 .

**3.12.36** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 691, 1373, 2297 of 10 skipped numbers.

This is polynomial generating 11 prime numbers.

$P(n) = 121n^2 - 649n + 911$ , generates 11 primes: 911, 383, 97, 53, 251, 691, 1373, 2297, 3463, 4871, 6521 .

**3.12.37** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 383, 971, 1847 of 11 skipped numbers. This is polynomial generating 11 prime numbers.

$P(n) = 144n^2 - 708n + 911$ , generates 11 primes: 911, 347, 71, 83, 383, 971, 1847, 3011, 4463, 6203, 8231 .

**3.12.38** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 691, 1301, 2111 of 9 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 100n^2 - 690n + 1231$ , generates 10 primes: 1231, 641, 251, 61, 71, 281, 691, 1301, 2111, 3121 .

**3.12.39** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 421, 1033, 1933 of 11 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 144n^2 - 684n + 853$ , generates 10 primes: 853, 313, 61, 97, 421, 1033, 1933, 3121, 4597, 6361 .

**3.12.40** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 281, 797, 1601 of 11 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 144n^2 - 780n + 1097$ , generates 10 primes: 1097, 461, 113, 53, 281, 797, 1601, 2693, 4073, 5741 .

**3.12.41** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 547, 1231, 2203 of 11 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 144n^2 - 900n + 1447$ , generates 10 primes: 1447, 691, 223, 43, 151, 547, 1231, 2203, 3463, 5011 .

**3.12.42** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 251, 743, 1523 of 11 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 144n^2 - 1668n + 4871$ , generates 10 primes: 4871, 3347, 2111, 1163, 503, 131, 47, 251, 743, 1523 .

**3.12.43** In Figure 3.1, in the  $n^2 + n + 41$  vertical columns of Euler's polynomial generating prime, I calculate polynomial including 223, 691, 1447 of 11 skipped numbers. This is polynomial generating 10 prime numbers.

$P(n) = 144n^2 + 1692n + 5011$ , generates 10 primes: 5011, 3463, 2203, 1231, 547, 151, 43, 223, 691, 1447 .

### 3.13 Skipping numbers and continuous prime numbers

I summarize continuous prime numbers for each skipping numbers in the vertical column of Euler's polynomial generating prime numbers  $n^2 + n + 41$  in Figure 3.1. If skipping numbers are small, continuous primes numbers are large, but even if skipping number are large, continuous primes numbers are large unexpectedly.

| <u>Skipping numbers</u> | <u>Continuous prime numbers</u>      |
|-------------------------|--------------------------------------|
| 2                       | 40                                   |
| 3                       | 31, 30                               |
| 4                       | 32, 16                               |
| 5                       | 20, 20, 14                           |
| 6                       | 23, 17, 12, 12                       |
| 7                       | 23, 23, 17, 16, 15                   |
| 8                       | 28, 28, 15, 15, 13, 13               |
| 9                       | 17, 17, 17, 16, 15, 10, 3            |
| 10                      | 18, 18, 16, 16, 14, 11, 9, 4         |
| 11                      | 18, 18, 16, 11, 10, 10, 10, 10, 10   |
| 12                      | 16, 16, 15, 14, 14, 12, 12, 8, 6, 6, |

Figure 2.1: The Ulam Spiral

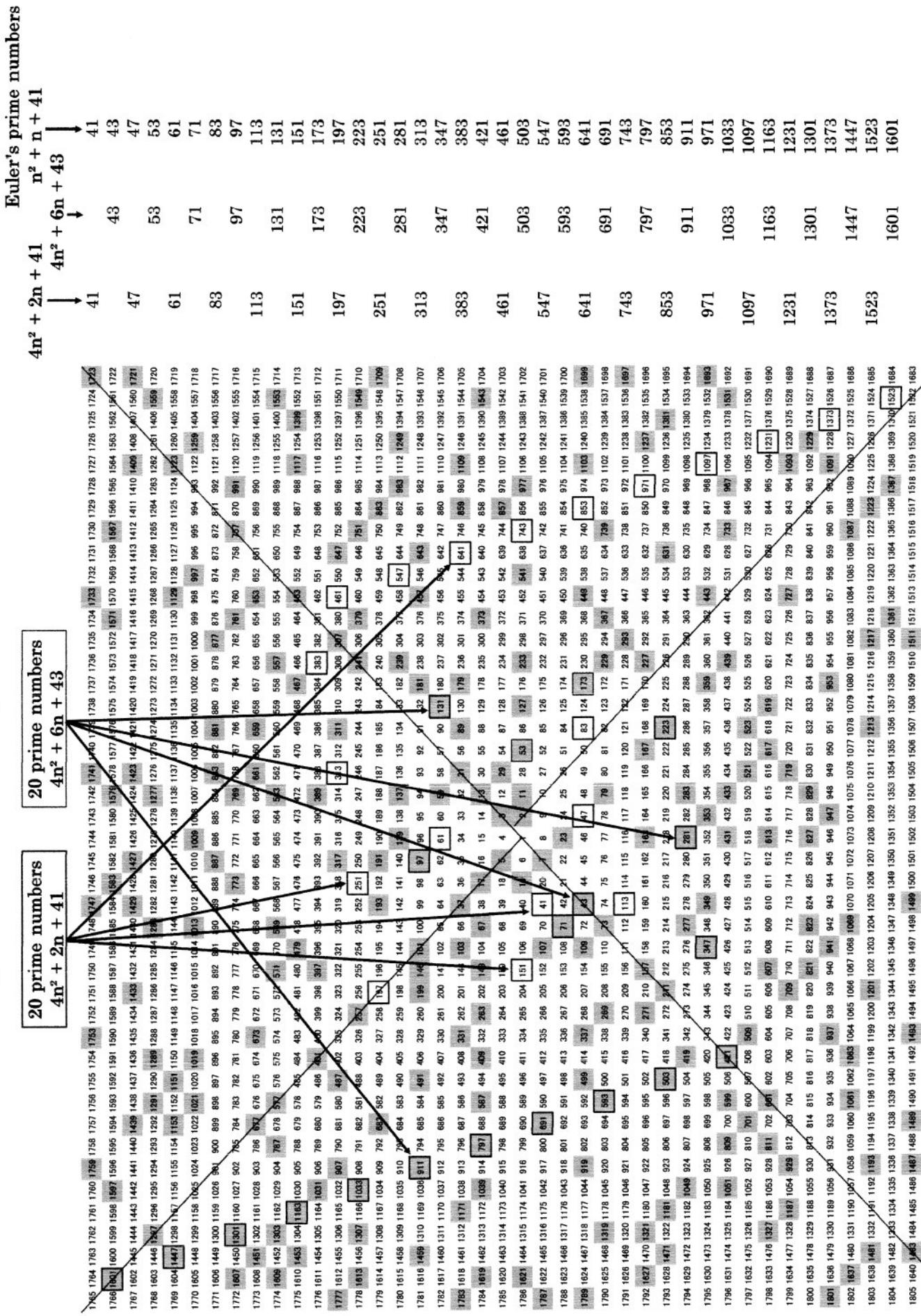


Figure 2.2: 180 degrees Arrangement Legendre Polynomial

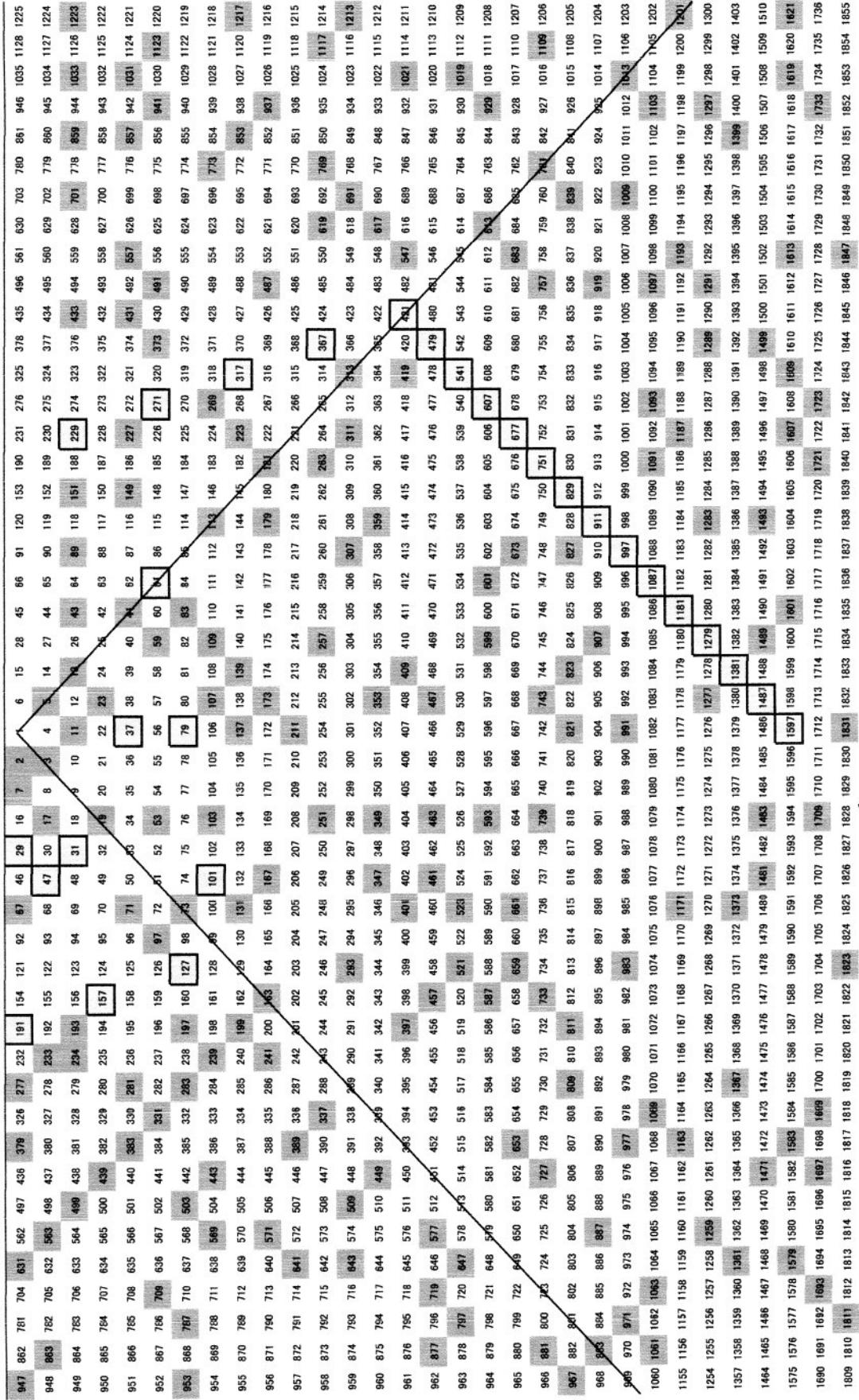


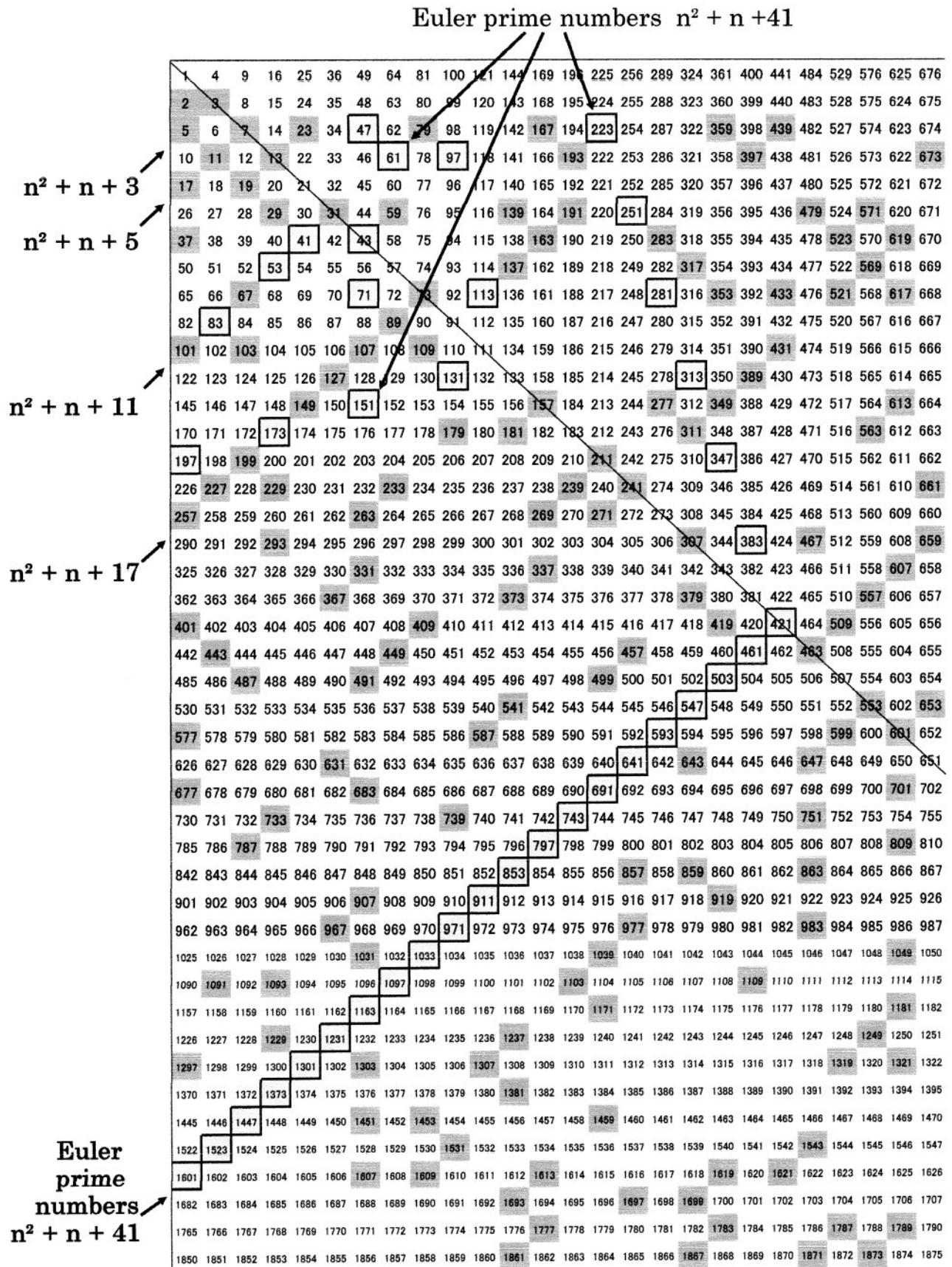
Figure 2.3: 135 degrees Arrangement Brox Polynomial

Figure 2.4: 270 degrees Arrangement Frame Polynomial

Frame polynomial  $3n^2 + 3n + 23$

|      |      |      |      |      |      |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
|------|------|------|------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 280  | 279  | 278  | 277  | 276  | 275  | 274 | 273 | 272 | 271 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 225  | 224  | 223  | 222  | 221  | 220  | 219 | 218 | 217 | 270 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 176  | 175  | 174  | 173  | 172  | 171  | 170 | 169 | 216 | 269 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 133  | 132  | 131  | 130  | 129  | 128  | 127 | 168 | 215 | 268 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 96   | 95   | 94   | 93   | 92   | 91   | 126 | 167 | 214 | 267 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 65   | 64   | 63   | 62   | 61   | 90   | 125 | 166 | 213 | 266 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 40   | 39   | 38   | 37   | 60   | 89   | 124 | 165 | 212 | 265 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 21   | 20   | 19   | 36   | 59   | 88   | 123 | 164 | 211 | 264 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 8    | 7    | 18   | 35   | 58   | 87   | 122 | 163 | 210 | 263 |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| 1681 | 1542 | 1409 | 1282 | 1161 | 1046 | 937 | 834 | 737 | 646 | 561 | 482 | 409 | 342 | 281 | 226 | 177 | 134 | 97  | 66  | 41  | 22  | 9   | 2   | 1   | 6   | 17  | 34  | 57  | 86  | 121 | 162 | 209 | 262 |
| 1682 | 1543 | 1410 | 1283 | 1162 | 1047 | 938 | 835 | 738 | 647 | 562 | 483 | 410 | 343 | 282 | 227 | 178 | 135 | 98  | 67  | 42  | 23  | 10  | 3   | 4   | 5   | 16  | 33  | 56  | 85  | 120 | 161 | 208 | 261 |
| 1683 | 1544 | 1411 | 1284 | 1163 | 1048 | 939 | 836 | 739 | 648 | 563 | 484 | 411 | 344 | 283 | 228 | 179 | 136 | 99  | 68  | 43  | 24  | 11  | 12  | 13  | 14  | 15  | 32  | 55  | 84  | 119 | 160 | 207 | 260 |
| 1684 | 1545 | 1412 | 1285 | 1164 | 1049 | 940 | 837 | 740 | 649 | 564 | 485 | 412 | 345 | 284 | 229 | 180 | 137 | 100 | 69  | 44  | 25  | 26  | 27  | 28  | 29  | 30  | 31  | 54  | 83  | 118 | 159 | 206 | 259 |
| 1685 | 1546 | 1413 | 1286 | 1165 | 1050 | 941 | 838 | 741 | 650 | 565 | 486 | 413 | 346 | 285 | 230 | 181 | 138 | 101 | 70  | 45  | 46  | 47  | 48  | 49  | 50  | 51  | 52  | 53  | 82  | 117 | 158 | 205 | 258 |
| 1686 | 1547 | 1414 | 1287 | 1166 | 1051 | 942 | 839 | 742 | 651 | 566 | 487 | 414 | 347 | 286 | 231 | 182 | 139 | 102 | 71  | 72  | 73  | 74  | 75  | 76  | 77  | 78  | 79  | 80  | 81  | 116 | 157 | 204 | 257 |
| 1687 | 1548 | 1415 | 1288 | 1167 | 1052 | 943 | 840 | 743 | 652 | 567 | 488 | 415 | 348 | 287 | 232 | 183 | 140 | 103 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 156 | 203 | 256 |
| 1688 | 1549 | 1416 | 1289 | 1168 | 1053 | 944 | 841 | 744 | 653 | 568 | 489 | 416 | 349 | 288 | 233 | 184 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 | 151 | 152 | 153 | 154 | 155 | 202 | 255 |
| 1689 | 1550 | 1417 | 1290 | 1169 | 1054 | 945 | 842 | 745 | 654 | 569 | 490 | 417 | 350 | 289 | 234 | 185 | 186 | 187 | 188 | 189 | 190 | 191 | 192 | 193 | 194 | 195 | 196 | 197 | 198 | 199 | 200 | 201 | 254 |
| 1690 | 1551 | 1418 | 1291 | 1170 | 1055 | 946 | 843 | 746 | 655 | 570 | 491 | 418 | 351 | 290 | 235 | 236 | 237 | 238 | 239 | 240 | 241 | 242 | 243 | 244 | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 252 | 253 |
| 1691 | 1552 | 1419 | 1292 | 1171 | 1056 | 947 | 844 | 747 | 656 | 571 | 492 | 419 | 352 | 291 | 292 | 293 | 294 | 295 | 296 | 297 | 298 | 299 | 300 | 301 | 302 | 303 | 304 | 305 | 306 | 307 | 308 | 309 | 310 |
| 1692 | 1553 | 1420 | 1293 | 1172 | 1057 | 948 | 845 | 748 | 657 | 572 | 493 | 420 | 353 | 354 | 355 | 356 | 357 | 358 | 359 | 360 | 361 | 362 | 363 | 364 | 365 | 366 | 367 | 368 | 369 | 370 | 371 | 372 | 373 |
| 1693 | 1554 | 1421 | 1294 | 1173 | 1058 | 949 | 846 | 749 | 658 | 573 | 494 | 421 | 422 | 423 | 424 | 425 | 426 | 427 | 428 | 429 | 430 | 431 | 432 | 433 | 434 | 435 | 436 | 437 | 438 | 439 | 440 | 441 | 442 |
| 1694 | 1555 | 1422 | 1295 | 1174 | 1059 | 950 | 847 | 750 | 659 | 574 | 495 | 496 | 497 | 498 | 499 | 500 | 501 | 502 | 503 | 504 | 505 | 506 | 507 | 508 | 509 | 510 | 511 | 512 | 513 | 514 | 515 | 516 | 517 |
| 1695 | 1556 | 1423 | 1296 | 1175 | 1060 | 951 | 848 | 751 | 660 | 575 | 576 | 577 | 578 | 579 | 580 | 581 | 582 | 583 | 584 | 585 | 586 | 587 | 588 | 589 | 590 | 591 | 592 | 593 | 594 | 595 | 596 | 597 | 598 |

Figure 2.5: 90 degrees Arrangement Euler's Polynomial



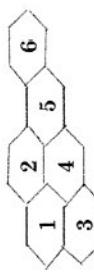
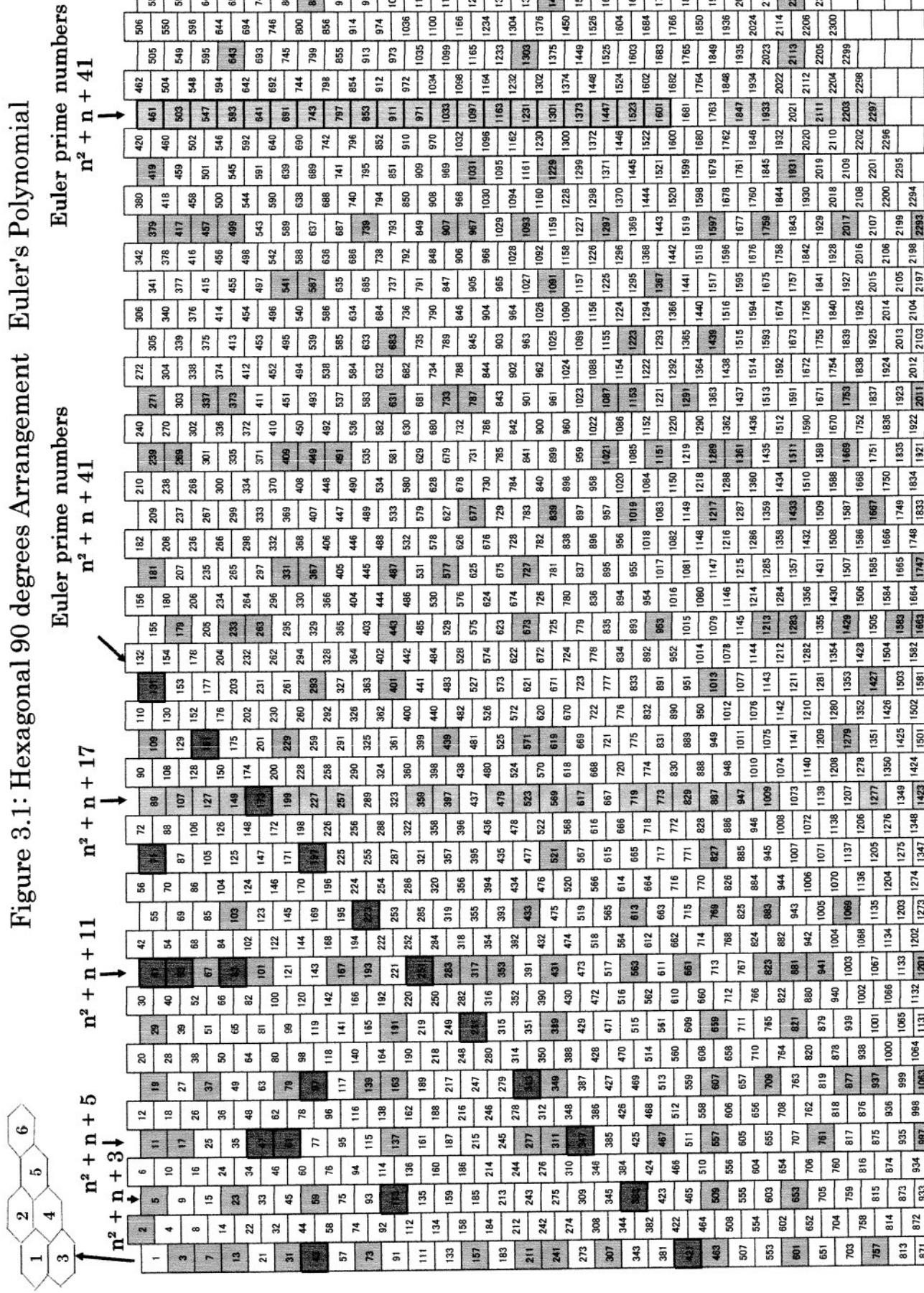


Figure 2.6: Hexagonal 90 degrees Arrangement Euler's Polynomial

| Euler prime numbers |     |     |                |      |      | Euler prime numbers |      |      |               |      |      |
|---------------------|-----|-----|----------------|------|------|---------------------|------|------|---------------|------|------|
| $n^2 + n + 41$      |     |     | $n^2 + n + 17$ |      |      | $n^2 + n + 11$      |      |      | $n^2 + n + 5$ |      |      |
| 2                   | 5   | 11  | 18             | 28   | 30   | 42                  | 55   | 62   | 72            | 90   | 109  |
| 4                   | 10  | 18  | 27             | 39   | 54   | 70                  | 88   | 107  | 129           | 155  | 181  |
| 3                   | 9   | 17  | 26             | 38   | 69   | 86                  | 106  | 128  | 152           | 180  | 193  |
| 7                   | 15  | 25  | 37             | 51   | 67   | 85                  | 105  | 126  | 150           | 178  | 207  |
| 14                  | 24  | 36  | 50             | 66   | 84   | 104                 | 126  | 152  | 177           | 205  | 235  |
| 13                  | 23  | 35  | 49             | 65   | 84   | 103                 | 125  | 149  | 175           | 204  | 234  |
| 12                  | 22  | 34  | 48             | 62   | 82   | 102                 | 124  | 148  | 174           | 202  | 233  |
| 21                  | 33  | 46  | 63             | 81   | 101  | 123                 | 147  | 175  | 201           | 231  | 263  |
| 32                  | 32  | 46  | 62             | 80   | 100  | 122                 | 146  | 172  | 200           | 230  | 262  |
| 31                  | 45  | 60  | 78             | 96   | 119  | 121                 | 144  | 170  | 198           | 228  | 259  |
| 44                  | 56  | 77  | 96             | 118  | 142  | 168                 | 196  | 226  | 257           | 286  | 329  |
| 58                  | 76  | 96  | 117            | 141  | 167  | 195                 | 225  | 257  | 291           | 327  | 366  |
| 57                  | 75  | 95  | 116            | 140  | 166  | 194                 | 224  | 256  | 290           | 326  | 364  |
| 73                  | 93  | 115 | 139            | 165  | 193  | 212                 | 248  | 289  | 325           | 363  | 403  |
| 91                  | 114 | 138 | 164            | 192  | 221  | 253                 | 287  | 323  | 361           | 401  | 442  |
| 112                 | 136 | 162 | 190            | 220  | 252  | 286                 | 322  | 360  | 400           | 442  | 486  |
| 111                 | 135 | 161 | 188            | 219  | 251  | 285                 | 321  | 359  | 399           | 441  | 485  |
| 134                 | 159 | 187 | 217            | 249  | 283  | 318                 | 356  | 396  | 438           | 483  | 529  |
| 133                 | 158 | 186 | 216            | 248  | 282  | 317                 | 355  | 395  | 437           | 481  | 527  |
| 157                 | 185 | 215 | 247            | 280  | 316  | 354                 | 394  | 436  | 480           | 526  | 574  |
| 184                 | 214 | 246 | 279            | 315  | 353  | 393                 | 435  | 479  | 525           | 573  | 623  |
| 183                 | 213 | 245 | 278            | 314  | 352  | 392                 | 434  | 478  | 524           | 572  | 622  |
| 212                 | 244 | 277 | 312            | 350  | 391  | 431                 | 476  | 522  | 571           | 621  | 673  |
| 211                 | 242 | 276 | 311            | 349  | 389  | 430                 | 474  | 520  | 568           | 619  | 672  |
| 241                 | 275 | 310 | 348            | 388  | 430  | 473                 | 519  | 567  | 617           | 670  | 725  |
| 273                 | 309 | 349 | 387            | 428  | 466  | 506                 | 546  | 586  | 626           | 676  | 729  |
| 308                 | 346 | 386 | 428            | 468  | 504  | 542                 | 578  | 616  | 656           | 704  | 758  |
| 307                 | 345 | 385 | 427            | 467  | 503  | 543                 | 577  | 615  | 655           | 703  | 757  |
| 343                 | 384 | 425 | 469            | 515  | 563  | 613                 | 665  | 719  | 774           | 832  | 893  |
| 382                 | 424 | 468 | 514            | 562  | 612  | 664                 | 718  | 774  | 831           | 891  | 953  |
| 381                 | 423 | 467 | 513            | 561  | 611  | 663                 | 717  | 773  | 831           | 890  | 952  |
| 422                 | 466 | 512 | 560            | 610  | 662  | 716                 | 772  | 830  | 890           | 951  | 1016 |
| 441                 | 485 | 511 | 559            | 609  | 661  | 715                 | 771  | 829  | 888           | 951  | 1015 |
| 464                 | 510 | 558 | 608            | 660  | 714  | 770                 | 828  | 887  | 949           | 1008 | 1080 |
| 463                 | 508 | 556 | 606            | 656  | 713  | 768                 | 826  | 886  | 948           | 1007 | 1073 |
| 507                 | 555 | 605 | 657            | 711  | 767  | 825                 | 885  | 947  | 1011          | 1077 | 1145 |
| 553                 | 554 | 604 | 656            | 710  | 766  | 824                 | 884  | 946  | 1010          | 1076 | 1144 |
| 553                 | 603 | 655 | 709            | 755  | 818  | 878                 | 940  | 1004 | 1070          | 1138 | 1208 |
| 602                 | 654 | 708 | 756            | 817  | 877  | 939                 | 1003 | 1068 | 1137          | 1207 | 1278 |
| 601                 | 653 | 707 | 753            | 811  | 876  | 938                 | 1002 | 1068 | 1136          | 1206 | 1277 |
| 652                 | 706 | 752 | 810            | 860  | 881  | 937                 | 1001 | 1067 | 1135          | 1204 | 1276 |
| 651                 | 705 | 751 | 809            | 859  | 880  | 936                 | 1000 | 1066 | 1134          | 1203 | 1275 |
| 704                 | 700 | 750 | 808            | 858  | 878  | 935                 | 1004 | 1064 | 1131          | 1201 | 1273 |
| 703                 | 759 | 817 | 877            | 939  | 1003 | 1068                | 1137 | 1207 | 1278          | 1349 | 1424 |
| 758                 | 816 | 876 | 938            | 1002 | 1067 | 1136                | 1206 | 1277 | 1345          | 1422 | 1504 |
| 757                 | 815 | 875 | 937            | 1001 | 1066 | 1135                | 1205 | 1276 | 1344          | 1421 | 1503 |
| 813                 | 873 | 936 | 995            | 1065 | 1133 | 1203                | 1275 | 1349 | 1425          | 1503 | 1583 |
| 871                 | 933 | 987 | 998            | 1064 | 1131 | 1201                | 1273 | 1347 | 1423          | 1501 | 1581 |



## 5 Consideration

I am very lucky that I found many polynomials generating prime numbers only to skip the values of column of Euler prime numbers.

It is expected that polynomial of many continuous prime numbers can be found by skipping successfully the values of polynomials containing many prime numbers.

## 6. Acknowledgment

The author would like to thank the Darkside Communication Group of the mathematics circle in japan and the people involved in research and teaching in this research work.

## References

- [1] Graphic Science MAGAZINE Newton (Japan) 2013.4
- [2] Various Arithmetic Functions and their Applications  
Octavian Cira and Florentin Smarandache March 29,2016  
arXiv:1603.08456v1 [math.GM] 28 Mar 2016
- [3] PRIME NUMBERS The Most Mysterious Figures in Math: David Wells
- [4] Prime-Generating Polynomial Wolfram MathWorld