

# On Geoengineering and Implementing an Albedo Solution with Urban Heat Islands Global Warming and Cooling Estimates

**Key Words:** Albedo Solution, Global Warming Solution, Global Warming Re-radiation Model, Albedo Modeling, Hotspot Mitigation, UHI Global Warming Estimates

## Abstract

Surface albedo geoengineering is vital in Global Warming (GW) as results can reverse trends and reduce the probability of a tipping point. Although an albedo solution is reasonably practical, work in this area appears stagnant and even implementing Urban Heat Island (UHI) cool roofs on a global level has not yet been widely adopted. This paper provides basic modeling and motivation by illustrating the potential impact of reverse forcing. We provide insights into “Earthly areas” that might be utilized to increase the opportunity for reducing warming. Modeling shows that by solar geoengineering select hotspots with aspects like large heat capacities, such as UHIs, and possibly mountain regions, the effective area could be roughly 11 times smaller than nominal non-hotspot regions in influencing global warming. We find that between 0.2% and 1% of the Earth would require modification to resolve most of global warming. This represents about a 1.5% global albedo change. Results are highly dependent on modeling aspects like heat capacity, irradiance, and albedo changes of the area selected. The versatile model was also used to provide UHIs global warming and cooling estimates illustrating their importance.

## 1.0 Introduction

When we consider climate change solutions, in the race against time, it is advantageous to look at the practical aspects of implementing an albedo solution. Given the slow progress reported with greenhouse gas reduction, and the continual increase in the Earth’s average yearly temperature, it is important to revisit the alternate albedo solution. Unlike geoengineering solutions, Greenhouse Gas (GHG) reduction is highly difficult to result in reversing climate change, especially with reports on large desertification and deforestation occurring [1].

Implementation is a key focus on geoengineering an albedo surface solution. There have been a number of geoengineering solutions proposed [2-4] that are either atmospheric or surface-based. In this study, we focus on targeting surface regions and present practical engineering formulas and values.

The target areas that have the highest impacts are likely ones with:

- high solar irradiance
- large heat capacities
- low albedo
- ability to amplify nature’s albedo

To clarify the last target area, we infer that cooling down certain areas may cause natural compounding albedo changes to occur, such as increases in snowfall and ice formations. We can term hotspot regions as Solar Amplified Areas (SAA) relative to Nominal Land Albedo (NLA) areas (approximately 25% albedo, see Sec. 5.2).

Although the task is highly challenging, it is easier to do geoengineering of surface reflectivity compared with building cities. Often, UHIs and impermeable surfaces are haphazardly constructed in terms of solar absorption considerations. While numerous authors [5-17] have found probable significance that UHIs with their coverage contribute to GW (see supportive results in Section 5.2), the only motivated work in this area is a result of health concerns. Therefore, albedo cool roof solutions and other UHI mitigations have not received adequate attention compared to GHG efforts. This oversight is unfortunate and makes the business of an albedo solar solution and its financing less desirable. It is important that not just scientists understand the importance of the albedo solution. There is a lack of knowledge when it comes to the word albedo and its potential contribution. We cannot expect architects, road engineers, car designers, city planners, politicians and so forth, to incorporate environmental considerations and solutions, if these concepts are not widely understood. Therefore, a key strategy employed in this study is to demonstrate the advantages, feasibility and importance of cooling solar amplified areas made by man (and possibly nature). We provide simple geoengineering equations that can aid designers. We need to recognize that the whole is equal to the sum of the parts in global warming; humankind’s resolve to greenhouse gas and albedo improvements, both need to be addressed for a realistic solution.

## 63 2. Outline for Geoengineering and Implementing an Albedo Solution

64

65 We present a brief outline to overview and clarify our modeling objectives and motivate interests.

66

67 **Section 3:** In this section we first identify a key Planck-albedo parameter

68

$$69 \gamma_{\% \Delta \alpha \Delta T} \approx 1W / m^2 / \Delta \% \alpha \quad (1)$$

70

71 The parameter multiplied by  $\% \Delta \alpha$  (albedo percent albedo change) converts to  $\Delta P_T$ , the reverse forcing from the  
72 target area, where the total reverse forcing  $\Delta P_{Rev\_S}(\gamma_{\% \Delta \alpha \Delta T}, \% \Delta \alpha, \Delta P_T)$  is described

73

74 **Section 4:** In this section an Albedo model is developed to use the  $\Delta P_T$  goal where

75

$$76 \Delta P_T = \frac{A_T}{A_E} \frac{S_o}{4} 0.33 H_{T-N} [(\alpha'_T - \alpha_T)] \quad (2)$$

77

78 Here  $S_o=1360W/m^2$ , the factor,  $H_{T-N}$  is the hotspot irradiance sensible heat storage potential. This is a function of the  
79 heat capacity, mass, temperature storage, and solar irradiance by comparison to a nominal area (see Appendix B and  
80 C). Here  $\alpha_T$  is the initial target albedo,  $\alpha'_T$  is the modified target albedo, and 0.33 is the estimate fraction of time the  
81 target area is not covered by clouds. Then the final goal relative to fraction of Earth's area,  $A_E$ , needing modification  
82 is

- 83 •  $A_T / A_E$ , where  $A_T$  is the target area

84

85 **Section 5:** In this section, we provide examples on implementation of these models for different target areas  
86 including UHIs yielding their warming and cooling estimates.

87

88 Therefore, our task is to essentially find reasonable values for  $\Delta P_{Rev\_S}$ ,  $f_2$ ,  $H_{T-N}$ ,  $\gamma_{\% \Delta \alpha \Delta T}$ ,  $A_F$ ,  $\Delta P_T$ ,  $\% \Delta \alpha$ , in order to  
89 estimate a geoengineering GW solution by modifying the select fractional target area  $A_T/A_E$  of the Earth.

90

### 91 3.0 Geoengineering a Reverse Forcing Solution

92

93 In this section, we present and describe a simple solar geoengineering formula needed for a reverse forcing estimates  
94 due to a percent global albedo change from a target area given by

95

$$96 \Delta P_{Rev\_S} = -\gamma_{\% \Delta \alpha \Delta T} \% \Delta \alpha (1 + f_Y) A_F = \Delta P_T (1 + f_Y) A_F \quad (3)$$

97 Here we define

98

99  $\Delta P_{Rev\_S}$  is the reverse power per unit area change

100  $\% \Delta \alpha$  is the percent global albedo change due to modification of a target area

101  $\gamma_{\% \Delta \alpha \Delta T}$  = Planck-albedo parameter, 1Watt/m<sup>2</sup>/%ΔAlbedo

102  $1+f_Y$ = the albedo-GHG re-radiation parameter with  $f_Y$  about 0.63 for year Y=2019 (see Appendix A)

103  $A_F$  is an estimate of the anticipated GW feedback amplification reduction factor (Appendix A.4)

104  $\Delta P_T = \gamma_{\% \Delta \alpha \Delta T} \% \Delta \alpha$  is the reverse forcing change from the target area T

105

106 The Planck-albedo parameter is so named as it relates to blackbody ( $P_\alpha$ ) absorption. Its value can be estimated when  
107 considering an albedo change from two different time periods, having a global albedo change from  $\alpha_1$  to  $\alpha_2$  or we  
108 can simplify it as follows [5]

109

$$110 \gamma_{\% \Delta \alpha} = \frac{(\Delta E_o)_\alpha}{\alpha_1 - \alpha_2} \frac{1}{100} = \frac{E_o (\alpha_1 - \alpha_2)}{\alpha_1 - \alpha_2} \frac{1}{100} = E_o \alpha_1 / 100 \approx 1W / m^2 / \% \Delta \text{albedo} \quad (4)$$

111

112 Here the incoming solar radiation at the top of the atmosphere is  $E_o=1360W/m^2/4=340W/m^2$  and when  $\alpha_1$  is  
113 0.294118, the value is  $1.000W/m^2/\Delta \% \text{albedo}$ . We note the value 29.4118% ( $100W/m^2/340W/m^2$ ) and  $E_o$  are given in  
114 AR5 [18] in their energy budget diagram.

115

116 As an example, in Appendix A, an analysis of the warming was estimated from 1950 to 2019, and results are  
117 presented in Table A-1. The change in the long wavelength radiation  $\Delta P_\alpha$  is estimated as  $0.15352W/m^2$  due to an  
118 albedo percent change of 0.15% (from 1950 to 2019) so that

119

$$\gamma_{\% \Delta \alpha} = \Delta P_{\alpha} / \% \Delta \text{albedo} = 1.023 W / m^2 / \% \Delta \text{albedo} \quad (5)$$

120  
121  
122 This parameter can provide a relatively simple and reasonable estimate of the reverse forcing that occurs due to a  
123 global percent albedo change from a target area change of the Earth. Then the corresponding estimated power  
124 reduction  $\Delta P_T$  in long wavelength radiation due to an albedo target area reverse forcing is

$$\Delta P_T = -\gamma_{\% \Delta \alpha \Delta T} \% \Delta \alpha \quad (6)$$

127  
128 However, there is also a reduction in the re-radiation from GHG. This factor is  $1+f_Y$ . Here  $f_Y$  is the fraction of re-  
129 radiation that occurs from GHG where Y represents the estimated value for that year. This value can reasonably be  
130 assessed and its value found in Appendix A is  $f_Y=f_{2019} \approx 0.6276$  for 2019.

131  
132 Lastly we have included an allowance for anticipated feedback amplification reduction denoted as  $A_F$  (see example  
133 in the next Section),

134  
135 The effect of the target change results can be quantified as

$$\text{Effect} = \frac{\Delta P_{\text{Rev}_S}}{\Delta P_{\text{Total\_Feedback\_amp}}} \quad (7)$$

138  
139 Here  $\Delta P_{\text{Total+Feedback\_amp}}$  is the total forcing with feedback amplification that has occurred.

### 141 **3.1 Example of a Reverse Forcing Goal**

142  
143 In this section, we consider a goal of 1.5% geoengineering albedo change, with  $f_v=0.6276$  and a decrease in water-  
144 vapor feedback anticipated, we might use a value of  $A_F \approx 2.0$  [20]. According to Appendix A, Eq. A-12 this is  
145 estimated as 2.022. Then from Eq. 3

$$\Delta P_{\text{Rev}_S} = -1 W/m^2 / \% \times 1.5\% \times (1+f_2) \times 2.022 = -1.5 W/m^2 \times (1+0.6276) \times 2.022 = -4.94 \text{ Watt/m}^2 \quad (8)$$

148  
149 This estimate can be compared with the re-radiation model results in Table A-1 showing a forcing with feedback  
150 amplification yield  $5.12 W/m^2$  since 1950. This would indicate a significant resolution to the current warming trend  
151 since 1950, where  $\Delta T_s=0.95^\circ K$  that occurred by the end of 2019 (see Eq. A-13). Then the relative effect from Eq. 7  
152 is

$$\text{Effect} = \frac{4.94 W / m^2}{5.12 W / m^2} = 96.4\% \quad (9)$$

155  
156 for this particular geoengineering solution (Table A-1). The temperature reduction can be estimated from Eq. 9 as

$$\Delta T_{\text{Rev}_S} = -0.964 \times \Delta T_s = -0.926^\circ K \quad (10)$$

159  
160 As one might suspect, a 1.5% albedo change requires a lot of modified area. Feasibility is discussed in the rest of  
161 this paper. We note a number of solar geoengineering solutions have been proposed [2-4].

### 163 **4.0 Converting the Reverse Forcing Goal to a Target Area**

164  
165 We can write the short wavelength solar absorption as

$$P = \frac{Q}{A} = \frac{S_o}{4} \sum_i \frac{A'_i}{A_E} (1-\alpha_i) + \frac{S_o}{4} H_{T-N} \frac{A'_T}{A_E} (1-\alpha_T) + \frac{S_o}{4} \frac{A_C}{A_E} (1-\alpha_C) \quad (11)$$

168  
169 Here  $A'_i$  is the  $i^{\text{th}}$  effective area having an albedo  $\alpha_i$ ,  $S_o=1360 W/m^2$  and  $A_E$  is the surface area of the Earth and  $A_C$  is  
170 effective cloud coverage. We consider a change to a hotspot target effective area  $A_T$  with albedo  $\alpha_T$ . In addition,  
171 because we select a particularly problematic solar absorbing target compared to a nominal area (N), it has hotspot  
172 irradiance sensible heat storage potential  $H_{T-N}$ , a function of the heat capacity, mass, temperature storage, and solar  
173 irradiance. Essentially this has the effect of amplifying the target area.  $H_{T-N}$  is described and enumerated in  
174 Appendix B and C. As an example, many UHIs, due to their large heat capacity act like large heat sink. This is just

175 one of the many reasons that UHI are often hotter at night than during the day resulting from solar energy stored up  
 176 during the daytime (see Appendix C).

177

178 The overall equation prior to changing the albedo is subject to the area constraint

179

$$180 \quad A_E = A_{EU} + A_{EC} = \left( \sum_i A'_i + A_T \right) + A_C = 0.33 \left( \sum_i A_i + A_T \right) + A_C \quad (12)$$

181 and

$$182 \quad A_{EU} = 0.33 \left( \sum_i A_i + A_T \right), \quad A_{EC} = A_C \quad (13)$$

183

184 Here we have denoted the portion of the Earth covered from direct sunlight by clouds as  $A_{EC}=A_C= 67\%A_E$  [21].  
 185 Then the uncovered portion of the Earth is  $A_{EU}=33\%A_E$ . This is likely conservative as clouds do let some sunlight  
 186 through. However, that means that roughly on average only 33% of the time areas on the Earth receive direct sun  
 187 during daylight hours.

188

189 We now alter the target albedo  $\alpha_T$  to  $\alpha'_T$  of a SAA so that

190

$$191 \quad P' = \frac{Q'}{A} = \frac{S_o}{4} \sum_i \frac{0.33A_i}{A_E} (1 - \alpha_i) + \frac{S_o}{4} \frac{0.33A_T}{A_E} H_{T-N} (1 - \alpha'_T) + \frac{S_o}{4} \frac{A_C}{A_E} (1 - \alpha_C) \quad (14)$$

192

193 Note the 0.33 cloud factor is now added. The change in heat absorbed is just a function of the target change where  
 194 from Eq. 14

195

$$196 \quad \left( dP'_T \right)_\alpha = \frac{S_o}{4} \frac{0.33A_T H_{T-N}}{A_E} (-d\alpha_T) \quad (15)$$

197

198 where the subscript  $\alpha$  indicates all other Earth albedo components are held constant. Using the example goal of the  
 199 target area  $\Delta P_T = 1.5W/m^2$  in Eq. 3 and 8, Equation 15 is just

200

$$201 \quad \Delta P_T = P - P' = -\frac{S_o}{4} \frac{0.33A_T H_{T-N}}{A_E} [(\alpha'_T - \alpha_T)] = -1.5W / m^2 \quad (16)$$

202

203 However, the same results can be obtained by changing the albedo of a nominal area; so in this case  $H_{T-N} = 1$  (see  
 204 Appendix B). The equivalent change for the NLA is

205

$$206 \quad \Delta P_{T-N} = -\frac{S_o}{4} \frac{0.33A_N}{A_E} \{(\alpha'_N - \alpha_N)\} = -1.5W / m^2 \quad (17)$$

## 207 5.0 Area Estimates

208

209 Comparing the target SAA to the NLA, we have

210

$$211 \quad \frac{\Delta P_T}{\Delta P_{T-N}} \approx \frac{A_T H_{T-N} [(\alpha'_T - \alpha_T)]}{A_N [(\alpha'_N - \alpha_N)]} = 1 \quad (18)$$

212

213 As an example, assume  $H_{T-N} \approx 9$  (see Appendix B),  $\alpha_N = 0.25$  (see Sec. 5.2),  $\alpha_T = 0.12$  [22], and for  $\alpha'_N = \alpha'_T = 0.9$ , we  
 214 obtain

$$215 \quad \frac{A_N}{A_T} = \frac{H_{T-N} [(\alpha'_T - \alpha_T)]}{[(\alpha'_N - \alpha_N)]} = \frac{9[(0.9 - 0.12)]}{[(0.9 - 0.25)]} = 10.8 \quad (19)$$

216

217 This indicates that the nominal area would have to be about 11 times larger than the target area for equivalent  
 218 results.

219

220 In assessing our goal, we have from Eq. 16

$$221 \Delta P_T = \frac{S_o}{4} \frac{0.33 A_T H_{T-N}}{A_E} [(\alpha'_T - \alpha_T)] = -1.5W / m^2 \quad (20)$$

223 For  $H_{T-N}=1$ ,  $\alpha'_T=0.9$ , and  $\alpha_T=0.12$  then

$$224 \Delta P_T = -340 \frac{A_T}{A_E} [0.78] \times 0.33 = -1.5W / m^2 \quad (21)$$

225 and

$$226 \frac{A_T}{A_E} = 1.71\% \text{ of Earth} \quad (22)$$

227 For  $H_{T-N}=10$ ,  $\alpha'_T=0.9$ , and  $\alpha_T=0.12$  then

$$228 \frac{A_T}{A_E} = 0.171\% \text{ of Earth} \quad (23)$$

229 Recall that the goal for a  $1.5W/m^2$  corresponded to a 1.5% albedo change (see Sec. 3.1). We can check this results  
230 for  $A_T/A=1.71\%$  when  $H_{T-N}=1$ , using a related expression to Eq. 20. This is given by

$$231 \Delta \alpha\% = 0.33 \frac{A_T}{A_E} \frac{[(\alpha'_T - \alpha_T)]}{\alpha} = 0.33(1.71\%) \frac{[(0.9 - 0.12)]}{0.294118} = 1.5\% \quad (24)$$

232 as expected where the global albedo is taken as  $\alpha=0.294118$  which is indicated in AR5's energy budget figure [18].

### 233 5.1 Cooling Estimates Compared to Urban Heat Island Areas

234 Since UHI are likely good target areas, we can compare these results to the total global urbanized area. Such  
235 estimates of urbanization unfortunately vary widely partly due to the confusing definition of what is urban.  
236 However, two studies are of interest. A Schneider study [23] on 2000 data estimated that 0.148% of the Earth was  
237 covered by UHI and the associated surrounding urban areas. Due to city growth, this extrapolates to 0.188% [5] in  
238 2019. Similarly, another study from GRUMP [24] found global urbanization with a larger value in 2000 of 0.783%  
239 extrapolates to 0.953% [5] of the Earth's area in 2019. These extrapolations are based on an average yearly  
240 urbanization growth rates between 1.3% and 1.6% [5]. It is interesting that the IPCC (Satterthwaite et. al. [25]) AR5  
241 report references this Schneider et al. [23] results in urban coverage. Lastly, note that UHIs have their own hotspot  
242 amplification factors assessed in Appendix C [5] with two estimates provided of 3.1 and 8.4. These are listed in  
243 Table 2 for  $H_{T-N}$ . Therefore, compared to these 2019 estimates for urban heat island and surrounding areas, the  
244 required area changes for different  $H_{T-N}$  values (discussed in Appendix C) are summarized in Table 2.

245 **Table 2** Cooling required areas relative to UHI areas

$H_{T-N}$	$A_T/A$ (% of Earth)	Schneider Factor ( $A_T/A$ )/0.188%	GRUMP Factor ( $A_T/A$ )/0.953
	$\alpha'_T = 0.9$ ( $\alpha'_T = 0.5$ )	$\alpha'_T = 0.9$ ( $\alpha'_T = 0.5$ )	$\alpha'_T = 0.9$ ( $\alpha'_T = 0.5$ )
1	1.714 (3.52)	9.12 (18.7)	1.80 (3.69)
3.1	0.553 (1.13)	2.94 (6.03)	0.58 (1.19)
8.4	0.204 (0.419)	1.08 (2.23)	0.21 (0.44)
9	0.190 (0.39)	1.01 (2.08)	0.20 (0.41)

\* $A_T/A$  represent 96% of the solution (see Sec. 5.1)

256 Table 2 results are highly dependent on target albedo change and  $H_{T-N}$  which is overviewed in Appendix B and C.  
257 Results in Column 2 suggest that 0.2% to 1.1% of the Earth would require modification to resolve 96% of global  
258 warming depending on the target values for alpha and  $H_{T-N}$ . This is roughly a factor of 6 to 1 times the Schneider's  
259

261 UHI size estimate. It is important to develop better estimates for both  $H_{T-N}$  and urbanization sizes than estimated  
 262 here. Other important factors may exist such as hydro-hotspots.

263

- 264 • UHI surfaces create hydro-hotspots [26] which may contribute to higher values of  $H_{T-N}$ . A hydro-hotspot is  
 265 a hot surface that creates moisture in the presence of precipitation. Such surfaces create excess moisture in  
 266 the atmosphere promoting a local greenhouse effect. Zhao et al. [28] observed that UHI temperatures  
 267 increase in daytime  $\Delta T$  by 3.0°C in humid climates but decreasing  $\Delta T$  by 1.5°C in dry climates. Therefore,  
 268 UHI in humid climates could be prioritized.

269

270 We see that  $H_{T-N}$  is a highly complex factor for UHIs. We note that the 0.12 albedo value applies to UHI [22], may  
 271 be a good upper value when looking for hotspot targets. The albedo and two  $H_{T-N}$  values cited here have been  
 272 studied by the author [5]. These assessments for  $H_{T-N}$  applicable to UHIs are also provided to aid the reader in  
 273 Appendix C. Results in Table 2 illustrate feasibility and the probable geoengineering challenges.

274

275 A worldwide effort would provide motivation from a number of key benefits; resolving much of global warming,  
 276 providing assurance against a tipping point, and local health benefits by cooling off cities. UHIs pose a number of  
 277 challenges in trying to cool off their areas. The Schneider results in Row 2 and 3 indicate that the potential area  
 278 needed may be 2.2-6 times their current size while the GRUMP results are a factor of about 5 smaller. Therefore, if  
 279 the Schneider estimate was proven to be the most accurate, supplementary target areas would be required to reach  
 280 the 96% objective. Note in these estimates we used the target albedo goal of  $\alpha_T'=0.5$ , as it is unrealistic to realize an  
 281 UHI albedo goal of 0.9 due to their complex nature.

282

283 Generally, UHIs meet a lot of the requirements for good targets having high heat capacity with large hotspot areas  
 284 and massive sensible heat storage. One helpful aspect to note is that cool roof and building implementation also  
 285 allows for more stable albedo maintenance over time compared to other areas like mountain regions. However, the  
 286 complex nature of cities also makes it highly challenging.

287

## 288 *5.2 Warming Estimates Due to Urban Heat Islands*

289

290 We can use this same model to estimate the global warming contributions due to UHIs. In this case, instead of  
 291  $\alpha_T'=0.9$  or 0.5, we evaluate by restoring the UHIs to their original estimated albedo value of  $\alpha_T'=0.25$  (pre-UHI era).  
 292 This albedo value is based on a study by He et al. [29] which found that land albedo varies from 0.1 to 0.4 with an  
 293 average of 0.25. Then using the  $H_{T-N}$  values in Section 5.1 (also see Appendix C), we estimate the percent of the  
 294 Earth needed to obtain a 96% solution and compare results to the known UHI coverage areas.

295

296 For  $H_{T-N}=3.1$ ,  $\alpha_T'=0.25$ , and  $\alpha_T=0.12$  then from Eq. 20

297

$$298 \Delta P_T = -340W / m^2 \frac{A_T}{A_E} x 3.1x[(0.25 - 0.12)]x0.33 = -1.5W / m^2 \quad (25)$$

299 and

$$300 \frac{A_T}{A_E} = 3.31\% \quad (26)$$

301

302 of the Earth. Similarly for  $H_{T-N}=8.4$ ,  $\alpha_T'=0.25$ , and  $\alpha_T=0.12$  then

303

$$304 \frac{A_T}{A_E} = 1.22 \% \text{ of Earth} \quad (27)$$

305 Table 3 summarized the warming trend results. Results in Column 5 and 6 are reasonably comparable to Feinberg  
 306 2020 [5] (finding between 5% and 44% of GW could be due to UHIs and their coverage). This model shows that  
 307 between 6% and 81% of global warming could be due to UHIs and their coverage. Note that this is fairly  
 308 independent of the GHG parameter  $f_2$  compared with results if  $f_1$  were used we would see very little difference. This  
 309 indicates the relative possible importance of UHIs. We note these large variations are mainly due to the difficulty in  
 310 estimating  $H_{T-N}$  and a knowledge of UHI area coverages (i.e., Schneider vs. GRUMP study). However, the model  
 311 provides a reasonable way to make estimates which can be further refined once better values are known.

312

**Table 3** UHI Warming estimates

$H_{T-N}$	$A_T/A$ (% of Earth)	Schneider Factor ( $A_T/A$ )/0.188% (Conservative)	GRUMP Factor ( $A_T/A$ )/ 0.953	GW% 1/Schneider Factor / 0.964*	GW% 1/GRUMP Factor / 0.964*
3.1	3.31	17.61	3.47	6	30
8.4	1.22	6.49	1.28	16	81

313

\* $A_T/A$  GW represent 96.4% of the solution (see Sec. 3.1), and are adjusted to 100% in Column 5 & 6

314

315 Furthermore, we note the cooling potential in Table 2 is about a factor of 3 to 6 times compared to the warming  
316 shown in Table 3. For example in Table 2 and 3, the area warming to cooling ratio 17.6/2.94 yields an effective  
317 potential factor of 6 for  $\alpha'_T=0.9$ , and a factor of 2.9 (17.6/6.03) for  $\alpha'_T=0.5$ . As stated above, obtaining the full  
318 cooling potential ( $\alpha'_T=0.9$ ) for UHIs and their impermeable surfaces is likely unobtainable due to the complex  
319 nature of cities therefore the value  $\alpha'_T=0.5$  is a better guide.

320

### 321 5.3 Some Hotspot Target Areas

322

323 There are many hotspots that provide likely target areas. Deserts would be highly difficult to maintain any albedo  
324 change. However, mountains, UHI cool roofs in cities, and impermeable surface such as roads might be logical  
325 target areas. Some interesting known hotspots include

326

- 327 • Flaming Mountains, China
- 328 • Bangkok, Thailand (planet's hottest city)
- 329 • Death Valley California
- 330 • Titat Zvi, Israel
- 331 • Badlands of Australia
- 332 • Urban Heat Islands & all Impermeable surfaces, humid cities
- 333 • Oceans [2]

334

335 We note that mountain areas (while certainly environmentally unfriendly) in cool regions should not be excluded;  
336 natural compounding albedo effects may occur from increases in snow-fall and ice formations. Albedo changes  
337 could be performed in summer months and then in winter months compounding effects assessed.

338

339 As a summary, Equations 3 and 20 can be combined to provide a resulting solar geoengineering equation for reverse  
340 forcing obtained in this study where

341

$$342 \quad \Delta P_{Rev\_S} = -\gamma_{\% \Delta \alpha \Delta T} \% \Delta \alpha (1+f) A_R = - \left\{ \frac{S_o}{4} 0.33 H_{T-N} \frac{A_T}{A_E} [(\alpha'_T - \alpha_T)] \right\} (1+f) A_R \quad (28)$$

343

344 with suggested values  $H_{T-N}=6$ ,  $\alpha'_T=0.5-0.9$ ,  $\alpha_T=0.12$ ,  $\Delta P_{Rev\_S}=4.9W/m^2$ , and  $f=0.63$ .

345

## 346 6. Conclusions

347

348 The albedo solution is vital in mitigating global warming. Today, technology has numerous advances that include  
349 improvements in materials, drone capability, and artificial intelligence, which could be helpful in geoengineering  
350 surfaces. Humankind has addressed many technological challenges successfully. It is not illogical to consider a  
351 global albedo solution while time permits before a potential tipping point.

352

353 In this paper we have provided a number of important estimates that include:

354

- 355 • A reverse forcing albedo reduction goal of  $-1.5W/m^2$  that can result in  $-4.9W/m^2$  of reverse forcing with  
356 feedback representing a 96% global warming solution.
- 357 • The target area required is about 0.2% to 1% (Table 2) of the Earth, if proper hotspots are cooled with  
358 highly reflective surfaces
- 359 • Changing the albedo has a 1.63 benefit factor due to less GHG re-radiation

- 360 • Selecting proper hotspots can reduce the required target area by an estimated factor of 11 compared to non-
- 361 hotspots areas. Likely target areas may include problematic hotspots such as UHIs and impermeable
- 362 surfaces. While certainly environmentally unfriendly, we may have to consider mountains regions and
- 363 ocean areas [2]
- 364 • The global cooling potential of UHIs is about a factor of three to six times higher than their warming
- 365 contribution if highly reflective surfaces can be realized
- 366 • UHIs and their coverage likely contribute significantly to global warming. This is in agreement with other
- 367 studies [5-17]. This suggests a reasonable risk exists that major greenhouse gas reduction goals [30], may
- 368 fall short of global warming mitigation expectations
- 369 • UHI estimates are highly dependent on  $H_{T-N}$  and urbanization estimates
- 370 • UHI in humid climates should be prioritized.

371  
372 Finally, we suggest:

- 373
- 374 • Tasking agencies worldwide, such as NASA, to work full time on solar geoengineering, which at this late
- 375 time should be one of our highest priorities
- 376 • Worldwide albedo guidelines for both UHIs and impermeable surfaces similar to on-going CO<sub>2</sub> efforts
- 377 • Worldwide guidelines for future albedo design considerations of cities
- 378 • Changing impermeable surfaces of buildings, roads, sidewalks, driveways, parking lots, industrial areas
- 379 such as airports, distribution centers, and roof tops to reflective surfaces. We note that their cooling
- 380 potential can be much larger compared to their warming contribution, and a full review should be
- 381 performed
- 382 • Manufacturing cars to be more reflective including reducing their internal solar heating. Although,
- 383 worldwide cool vehicles (e.g., silver or white) may not contribute significantly to global warming
- 384 mitigation, recommending them could. It would help raise badly needed albedo awareness similar to
- 385 electric automobiles that help improve CO<sub>2</sub> emissions. It could increase interest in similar projects thereby
- 386 promoting other related changes by city planners and architects for cool roofs, reflective building designs,
- 387 and road engineers for pavement color changes and so forth.

## 388 Appendix A: Re-radiation Global Warming Model Introduction

389  
390 When initial solar absorption occurs, part of the long wavelength radiation given off is re-radiated back to Earth. In  
391 the absence of feedback we denote this fraction as  $f_1$ . This presents a simplistic but effective model

$$392 P_{Pre-Industrial} = P_{\alpha}(1 + f_1) = \sigma T_s^4, \text{ where } P_{\alpha} = \frac{S_o}{4}(1 - \alpha) \quad (A-1)$$

393  
394 where  $T_s$  is the surface temperature. As one might suspect,  $f_1$  turns out to be exactly  $\beta^4$  in the absence of feedback,  
395 so that  $f_1$  is a redefined variable taken from the effective emissivity constant of the planetary system. We identify  
396 this as 0.618034 here. One of the main goals in this appendix is to find the re-radiation  $f_2$  for 2019. That is, in 2019,  
397 due to increases in GHGs, we anticipate an increase in the re-radiation fraction so that

$$398 f_2 = f_{2019} = f_1 + \Delta f = \beta_1^4 + \Delta f \approx \beta_2^4 + \Delta f \quad (A-2)$$

399  
400 In this way  $f_{2019} = f_2$  is a function of  $f_1$ . The RHS of Eq. A-2 indicates that  $\beta_1 \approx \beta_2$  (see varication results in Eq. A-16  
401 and A-17). Estimating  $\Delta f$  will not cause much error since it is relatively small compared to  $(1+f_1)$  which is fairly  
402 accurate in geoengineering.

### 403 A.1 Basic Re-radiation Model and Estimating $f_1$

404  
405 In geoengineering, we are working with absorption and re-radiation, we define

$$406 P_{Total} = \sigma T_s^4 = \sigma \left( \frac{T_e}{\beta} \right)^4 \text{ and } P_{\alpha} = \sigma T_{\alpha}^4 = \sigma (\beta T_s)^4 \quad (A-3)$$

407  
408 The definitions of  $T_{\alpha} = T_e$ ,  $T_s$  and  $\beta$  are the emission temperature, surface temperature and typically  $\beta \approx 0.887$ ,  
409 respectively. Consider a time when there is **no feedback issues** causing warming trends. Then by conservation of  
410 energy, the equivalent power re-radiated from GHGs in this model is dependent on  $P_{\alpha}$  with

$$411 P_{GHG} = P_{Total} - P_{\alpha} = \sigma T_s^4 - \sigma T_{\alpha}^4 \quad (A-4)$$

412  
413  
414  
415

416 To be consistent with  $T_\alpha = T_e$ , since typically  $T_\alpha \approx 255^\circ\text{K}$  and  $T_s \approx 288^\circ\text{K}$ , then in keeping with a common definition of  
 417 the global beta (the proportionality between surface temperature and emission temperature) for the moment  
 418  $\beta = T_\alpha / T_s = T_e / T_s$ .

419  
 420 This allows us to write the dependence  
 421

$$422 \quad P_{GHG} = \sigma T_s^4 - \sigma T_\alpha^4 = \frac{\sigma T_\alpha^4}{\beta^4} - \sigma T_\alpha^4 = \sigma T_\alpha^4 \left( \frac{1}{\beta^4} - 1 \right) = \sigma T_\alpha^4 \left( \frac{1}{f} - 1 \right) \quad (\text{A-5})$$

423  
 424 Note that when  $\beta^4 = 1$ , there are no GHG contributions. We note that  $f$ , the re-radiation parameter equals  $\beta^4$  in the  
 425 absence of forcing.

426  
 427 We can also define the blackbody re-radiated by GHGs given by some fraction  $f_1$  such that

$$428 \quad P_{GHG} = f_1 P_\alpha = f_1 \sigma T_\alpha^4 \quad (\text{A-6})$$

429  
 430 Consider  $f = f_1$ , in this case according to Equations A-5 and A-6, it requires

$$431 \quad P_{GHG} = \sigma T_\alpha^4 \left( \frac{1}{f_1} - 1 \right) = f_1 \sigma T_\alpha^4 \quad (\text{A-7})$$

432  
 433 This dependence leads us to the solution of the quadratic expression

$$434 \quad f_1^2 + f_1 - 1 = 0 \text{ yielding } f_1 = 0.618034 = \beta^4, \beta = (0.618034)^{1/4} = 0.886652 \quad (\text{A-8})$$

435  
 436 This is very close to the common value estimated for  $\beta$  and this has been obtained through energy balance in the  
 437 planetary system providing a self-determining assessment. In geoengineering we can view the re-radiation as part of  
 438 the albedo effect. In Section A.4, we apply the model to demonstrate its capability. Consistency with the Planck  
 439 parameter is shown in A.5. We note that the assumption  $f = f_1$  only works if planetary energy is in balance without  
 440 feedbacks. In Appendix A.6, we double check this model in another way by balancing energy in and out of our  
 441 global system.

## 442 *A.2 Re-radiation Model Applied to 1950 and 2019*

443  
 444 Global warming can be exemplified by looking at two different time periods. The model applied for 1950 needs to  
 445 be consistent with Eq. A-3 and A-5. Here we will

- 446 • assume no forcing issues causing a warming trend in 1950 so that from our model

$$447 \quad P_{Total, 1950} = P_\alpha + P_{GHG} = P_\alpha + f_1 P_\alpha = P_\alpha (1 + f_1) = 1.618 P_\alpha \quad (\text{A-9})$$

448  
 449 where  $P_\alpha = S_o \{0.25x(1 - Albedo)\}$  and  $S_o = 1360 \text{W/m}^2$ . Although 1950 is not truly pre-industrial, we proceed under  
 450 the assumption of no changes in GHG and feedback issues at this time to establish our baseline, since  
 451 geoengineering a solution to earlier dates would pose even higher challenges. Under this assumption,  $1 + f = 1.618$   
 452 becomes the 1950 albedo-GHG reference value.

## 453 *A.3 Re-radiation Model Applied to 2019*

454  
 455 In 2019 due to global warming trends, to apply the model we assume that feedback can be applied as a separate term  
 456 and we make use of some IPCC estimates for GHG forcing as a way to calibrate our model. In the traditional sense  
 457 of forcing, we assume some small change to the albedo and most of the forcing due to IPCC estimates for GHGs  
 458 where

$$459 \quad P_{Total 2019} = P_{\alpha'} + P_{GHG'} = P_{\alpha'} (1 + f_2) \quad (\text{A-10})$$

460  
 461 Then we introduce feedback through an amplification factor  $A_F$  as follows

$$462 \quad P_{Total 2019 \& Feedback} = P_{1950} + (\Delta P) A_F = P_{1950} + (P_{2019} - P_{1950}) A_F = \sigma T_s^4 \quad (\text{A-11})$$

463  
 464  
 465  
 466  
 467  
 468  
 469  
 470  
 471  
 472

473 Here, we assume a small change in the albedo denoted as  $P_{\alpha'}$  and  $f_2$  is adjusted to the IPCC GHG forcing value  
 474 estimated between 1950 and 2019 of  $2.38W/m^2$  [39]. Then the feedback amplification factor, is calibrated so that  
 475  $T_S=T_{2019}$  (see Table A-1) yielding  $A_F=2.022$  [also see ref. 20]. The main difference in our model is that the forcing  
 476 is about 6% higher than the IPCC for this period. Here, we take into account a small albedo decline of 0.15% that  
 477 the author has estimated in another study due to likely issues from UHIs [5] and their coverage. We note that unlike  
 478  $f_1, f_2$  is not a strict measure of the emissivity due the increase in GHGs.  
 479

#### 480 *A.4 Results Applied to 1950 and 2019 and an Estimate for $f_2$*

481  
 482 Since the re-radiation parameter is fixed for  $f_1=0.618034$ , to obtain the average surface temperature  $T_{1950}=13.89^\circ C$   
 483 ( $287.038^\circ K$ ), the only adjustable parameter left in our basic model is the global albedo. This requires an albedo  
 484 value of 0.3008 (see Table 1) to obtain  $T_{1950}=287.0385^\circ K$ . This albedo number is reasonable and similar to values  
 485 cited in the literature [31].  
 486

487 In 2019, the average temperature of the Earth is  $T_{2019}=14.84^\circ C$  ( $287.99^\circ K$ ) given in Eq. A-13. We have assumed a  
 488 small change in the Earth's albedo due to UHIs [5]. The  $f_2$  parameter is adjusted to 0.6276 to obtain the GHG  
 489 forcing shown in Column 7 of  $2.38W/m^2$  [39]. Therefore the next to last row in Table A-1 is a summary without  
 490 feedback, and the last row incorporated the  $A_F=2.022$  feedback amplification factor.  
 491  
 492

**Table A-1** Model results

Year	$T_S(^{\circ}K)$	$T_a(^{\circ}K)$	$f_1, f_2$	$\alpha, \alpha'$	$P_{\alpha}, P_{\alpha'}$ ( $W/m^2$ )	$P_{GHG+feedback}$ $P_{GHG}$ ( $W/m^2$ )	$P_{Total}$ ( $W/m^2$ )
2019	287.5107	254.55	0.6276	30.03488	238.056	149.404	387.460
1950	287.0410	254.51	0.6180	30.08	237.9028	147.024	384.9348
<b><math>\Delta 2019-1950</math></b>	<b>0.471</b>	<b>0.41</b>	<b>0.96%</b>	<b>(0.15%)</b>	<b>0.15352</b>	<b>2.38</b>	<b>2.5337</b>
<b>Feedback <math>A_F=2.022</math></b>	<b>0.95</b>	<b>0.41</b>	<b>0.96%</b>	<b>0.15</b>	<b>0.3104</b>	<b>4.812</b>	<b>5.12</b>

493  
 494 From Table A-1 we now have identified the reverse forcing at the surface needed since  
 495

$$496 P_{Total\ 2019\_Feedback\ Amp} = P_{1950} + (P_{2019} - P_{1950}) A_F = 384.927W / m^2 + (2.5337W / m^2) 2.022 = 390.05W / m^2 \quad (A=12)$$

497  
 498 and

$$499 \Delta T_S = T_{2019} - T_{1950} = (390.05 / \sigma)^{1/4} - 287.0385^\circ K = 287.9899^\circ K - 287.0385^\circ K = 0.95^\circ K \quad (A-13)$$

500  
 501 as modeled. We also note an estimate has now been obtained in Table A-1 for  $f_2=0.6276$  and  $A_F=2.022$ .  
 502

#### 503 *A.5 Model Consistency with the Planck Parameter*

504  
 505 As a measure of model consistency, the forcing change with feedback, and resulting temperatures  $T_{1950}$  and  $T_{2019}$ ,  
 506 should be in agreement with expected results using the Planck feedback parameter. From the definition of the Planck  
 507 parameter  $\lambda_o$  and results in Table A-1, we estimate [19]  
 508

$$509 \lambda_o = -4 \frac{\Delta R_{OLW}}{T_S} = -4 \left( \frac{237.9028W / m^2}{287.041^\circ K} \right)_{1950} = -3.31524W / m^2 / ^\circ K \quad (A-14)$$

510 and

$$511 \lambda_o = -4 \frac{\Delta R_{OLW}}{T_S} = -4 \left( \frac{238.056W / m^2}{287.99^\circ K} \right)_{2019} = -3.306W / m^2 / ^\circ K \quad (A-15)$$

512  
 513 Here  $\Delta R_{OLW}$  is the outgoing long wave radiation change. We note these are very close in value showing minor error  
 514 and consistency with Planck parameter value, often taken as  $3.3W/m^2/^\circ K$ .  
 515

516 Also note the Betas are very consistent with Eq. A-8 for the two different time periods since from Table A-1  
 517

$$518 \beta_{1950} = \frac{T_{\alpha}}{T_S} = \frac{T_e}{T_S} = \frac{254.51}{287.041} = 0.88667 \text{ and } \beta_{1950}^4 = 0.6180785 \quad (A-16)$$

519  
 520 and  
 521

$$\beta_{2019} = \frac{T_\alpha}{T_S} = \frac{T_e}{T_S} = \frac{254.55}{287.5107} = 0.88526 \text{ and } \beta_{2019}^4 = 0.6144 \quad (\text{A-17})$$

523

524 **A.6 Balancing  $P_{out}$  and  $P_{in}$  in 1950**

525

526 In equilibrium the radiation that leaves must balance  $P_\alpha$ , from the energy absorbed, so that

527

$$\begin{aligned} \text{Energy}_{Out} &= (1-f_1)P_\alpha + (1-f_1)P_{Total} = (1-f_1)P_\alpha + (1-f_1)\{P_\alpha + f_1P_\alpha\} \\ &= 2P_\alpha - f_1P_\alpha - f_1^2P_\alpha = \text{Energy}_{In} = P_\alpha \end{aligned} \quad (\text{A-18})$$

529

530 This is consistent, so that in 1950, Eq. A-18 requires the same quadratic solution as Eq. A-8. It is also apparent that

531

$$P_\alpha = f_1^4 P_{Total\_1950} = \beta_1^4 P_{Total\_1950} \quad (\text{A-19})$$

533

534 since

535

$$P_\alpha = f_1(P_\alpha + f_1P_\alpha) \text{ or } 1 = f_1(1+f_1) \quad (\text{A-20})$$

537

538 The RHS of Eq. A-20 is Eq. A-8. This illustrates  $f_1$  from another perspective as the fractional amount of total  
539 radiation in equilibrium. As a final check, the application in Section A.4, Table A-1, illustrate that  $f_1$  provides  
540 reasonable results.

541

542 **Appendix B: Estimating the Potential for Hotspot Irradiance Sensible Heat Storage  $H_{T-N}$** 

543

544 A candidate hotspot irradiance sensible heat storage  $H_{T-N}$  was described in Section 6. Here we provide a preliminary  
545 suggested model to clarify and enumerate this factor. We note other models may be more appropriate. For example,  
546 an alternate method for  $H_{T-N}$  applied to UHIs is described in Appendix C. Other more rigorous models can be  
547 developed. Such solutions are outside the scope of this paper.

548

549 In this example model, we consider a ratio for a target (T) area relative to a nominal (N) area defined in Sec. 5.  
550 Consider a target area with sensible heat storage  $q$ , due to a mass  $m$ , having specific heat capacity  $C_p$  experiencing a  
551 day-night  $\Delta T$  change in time  $\tau$ , and then the suggested potential for sensible hotspot heat storage  $H_{T-N}$  has the form

552

$$H_{T-N} = \frac{q_T}{q_N} \times \frac{I_T}{I_N} = \frac{m_T C_{pT} \Delta T_T}{m_N C_{pN} \Delta T_N} \times \frac{I_T}{I_N} \approx \frac{\tau_T C_{pT} \Delta T_T}{\tau_N C_{pN} \Delta T_N} \times \frac{I_T}{I_N} \quad (\text{B-1})$$

554

555 Here we provide the option of using temperature change in time  $\tau$  in place of mass. For example, the time to 63%  
556 change in  $\Delta T$  might be useful (similar to a time constant). We also consider that the irradiance (I) term is needed  
557 since not all solar absorption energy is stored.

558

559 As a numeric example, first consider a 90% irradiance target area (compared to the equator) with nominal mid-  
560 latitudes (45°) roughly 70%, compared to say the Arctic and Antarctic Circles at approximately 40% [31]. Then the  
561 irradiance ratio is

$$\frac{I\%_T}{I\%_N} = \frac{90\%_T}{70\%_N} = 1.3 \quad (\text{B-2})$$

563

564 For the sensible heat numeric portion, consider a rocky area as the target (such as Flaming Mountains). This can be  
565 compared with a nominal vegetative land area. As a rule of thumb, most rocks have a density of 2.65 g/cm<sup>3</sup>, about  
566 50% difference compared to a nominal soil area of 1.33 g/cm<sup>3</sup> [33]. The heat capacity of rocks compared with  
567 vegetated land is 2000 to 830J/Kg<sup>o</sup>K [34]. Then  $\Delta T$  is estimated from tables for a day-night cycle [34, 35]. The  
568 estimate is

$$\frac{q_T}{q_N} = \frac{m_T C_{pT} \Delta T_T}{m_N C_{pN} \Delta T_N} = \frac{\rho_T C_{pT} \Delta T_T}{\rho_N C_{pN} \Delta T_N} = \left( \frac{2.65}{1.33} \right)_\rho \left( \frac{2000}{830} \right)_{C_p} \left( \frac{10^\circ\text{C}}{6.9^\circ\text{C}} \right) = 2 \times 2.4 \times 1.45 = 6.96 \quad (\text{B-3})$$

570

571 Then including irradiance

572

$$H_{T-N} \approx 9 \quad (\text{B-4})$$

## 573 Appendix C: UHI Amplification Factors

574

575 An analysis of UHI amplification effects that can be applied to  $H_{T-N}$  was originally provided by the author [5] and  
576 this work is added here to aid the reader.

### 577 C.1 UHI Area Amplification Factor

578

579 To estimate  $H_{T-N}$  for UHI amplification effects, it is logical to first look at UHI footprint (FP) studies as they provide  
580 some measurement information. Zhang et al. [36] found the ecological FP of urban land cover extends beyond the  
581 perimeter of urban areas, and the FP of urban climates on vegetation phenology was 2.4 times the size of the actual  
582 urban land cover. A more recent study by Zhou et al. [37], looked at day-night cycles using temperature difference  
583 measurements in China. This study found UHI effect decayed exponentially toward rural areas for the majority of  
584 the 32 Chinese cities. Their comprehensive study spanned from 2003 to 2012. Zhou et al. describes China as an  
585 ideal area to study as it has experienced the most rapid urbanization in the world during the decade evaluated.  
586 Findings state that the FP of UHI effect, including urban areas, was 2.3 and 3.9 times that of urban size for the day  
587 and nights, respectively. We note that the average day-night amplification footprint coverage factor is 3.1.

588 The UHI Amplification Factor (AF) is highly complex, making it difficult to assess from first principles as it would  
589 be some function of

$$590 AF_{UHI \text{ for } 2019} = f\left(\overline{Build}_{Area} \times \overline{Build}_{C_p} \times \overline{R}_{wind} \times \overline{LossE}_{vtr} \times \overline{Hy} \times \overline{S}_{canyon}\right) \quad (C-1)$$

591 were

592  $\overline{Build}_{Area}$  = Average building solar area593  $\overline{Build}_{C_p}$  = Average building heat capacity594  $\overline{R}_{wind}$  = Average city wind resistance595  $\overline{LossE}_{vtr}$  = Average loss of evapotranspiration to natural cooling & loss of wetland596  $\overline{Hy}$  = Average humidity effect due to hydro-hotspot597  $\overline{S}_{canyon}$  = Average solar canyon effect

598

599 To provide some estimate of this factor, we note that Zhou et al. [36] found the FP physical area (km<sup>2</sup>), correlated  
600 tightly and positively with actual urban size having a correlation coefficients higher than 79%. This correlation can  
601 be used to provide an initial estimate of this complex factor. Therefore, as a model assumption, it seems reasonable  
602 to use area ratios for this estimate.

$$603 AF_{UHI \text{ for } 2019} = \frac{\sum(UHI \text{ Area})_{2019}}{\sum(UHI \text{ Area})_{1950}} \quad (C-2)$$

604

605 Area estimates have been obtained in the Feinberg [5] yielding the following results for the Schneider et al. [23] and  
606 the GRUMP [24] extrapolated area results:

$$607 AF_{UHI \text{ for } 2019} = \frac{(Urban \text{ Size})_{2019}}{(Urban \text{ Size})_{1950}} \approx \begin{cases} \left( \frac{[0.188]_{2019}}{[0.059]_{1950}} \right)_{Schneider} = 3.19 \\ \left( \frac{[0.952]_{2019}}{[0.316]_{1950}} \right)_{GRUMP} = 3.0 \end{cases} \quad (C-3)$$

608 Between the two studies, the UHI area amplification factor average is 3.1. Coincidentally, this factor is the same  
609 observed in the Zhou et al. [37] study for the average footprint. This factor may seem high. However, it is likely  
610 conservative as other effects would be difficult to assess: increases in global drought due to loss of wet-lands,  
611 deforestation effects due to urbanization, and drought related fires. It could also be important to factor in changes of  
612 other impermeable surfaces since 1950, such as highways, parking lots, event centers, and so forth.

613

614 The area amplification value of 3.1 is then considered as one of our model assumptions for  $H_{T-N}$ .

615

616

617

## 618 **C.2 Alternate Method Using the UHI's Dome Extent**

619

620 An alternate approach to check the estimate of Equation C-3, is to look at the UHI's dome extent. Fan et al. [38]  
 621 using an energy balance model to obtain the maximum horizontal extent of a UHI heat dome in numerous urban  
 622 areas found the nighttime extent of 1.5 to 3.5 times the diameter of the city's urban area (2.5 average) and the  
 623 daytime value of 2.0 to 3.3 (2.65 average).

624

625 Applying this energy method (instead of the area ratio factor in Eq. C-3), yields a diameter in 2019 compared to that  
 626 of 1950 with an increase of 1.8. This method implies a factor of  $2.5 \times 1.8 = 4.5$  higher in the night and  $2.65 \times 1.8 = 4.8$   
 627 in the day in 1950 with an average 4.65. This increase occurs 62.5% of the time according to Fan et al., where their  
 628 steady state occurred about 4 hours after sunrise and 5 hours after sunset yielding an effective UHI amplification  
 629 factor of 2.9. We note this amplification factor is in good agreement with Equation C-3. Fan et al. [38] assessed the  
 630 heat flux over the urban area extent to its neighboring rural area where the air is transported from the urban heat  
 631 dome flow. Therefore the heat dome extends in a similar manner as observed in the footprint studies. If we use the  
 632 dome concept, we obtain some vertical extent which is a logical when considering GW. We can make an assumption  
 633 that the actual surface area for the heat flux is increased by the surface area of the dome. We actually do not know  
 634 the true diameter of the dome, but it is larger than the assessment by Fan et al. Using the dome extend due to Fan et  
 635 al. [38] applied to the area of diameter  $D$ , the amplification factor should be correlated to the ratios of the dome  
 636 surface areas:

$$637 \quad AF_{UHI \text{ for } 2019} = \left( \frac{D_{2019}}{D_{1950}} \right)^2 = 2.9^2 = 8.4 \quad (C-4)$$

638

639 Thus, this equation is a second value for  $H_{T-N}$ , where it is reasonable to use the ratios of the dome's surface area for  
 640 an alternate approach in estimating the effective UHI amplification factor [5]. We will have two values, 3.1 and 8.4  
 641 to work with that provides an upper and lower bounds for effective amplification area.

## 642 **Appendix D: Albedo Compared to GHG Change**

643

644 A change in albedo forcing compared with a change in GHGs can be described. The variation in the energy due to  
 645 an average albedo change and its re-radiation is

646

$$647 \quad \Delta P_{\alpha} = \Delta P_{\alpha'} + f_2 \Delta P_{\alpha'} = 1.6276 \Delta P_{\alpha'} = 1.63 \times 0.153 = 0.25 \quad (D-1)$$

648

649 The average change in GHGs can be written in terms of  $\Delta f$

650

$$651 \quad \Delta P_{GHG} = \Delta f P_{\alpha} = 0.96\% (238) = 2.29 \quad (D-2)$$

652

653 This resulting ratio from Table 1 is

654

$$655 \quad \frac{\Delta P_{\alpha}}{\Delta P_{GHG}} = \frac{\Delta P_{\alpha'} (1 + f_2)}{\Delta f P_{\alpha}} = \frac{0.154 W / m^2}{0.0096} \frac{1.6276}{238 W / m^2} = 0.109 \quad (D-3)$$

656

657 Note this ratio is of course dependent on the 2019 albedo 0.15% change. However, it also provides a valuable  
 658 estimate. We note this is an alternate way to estimate the amount of albedo change to equate to the change in the  
 659 GHG.

$$660 \quad \Delta P_{GHG} = \frac{\Delta P_{\alpha}}{0.109} = \frac{1.6276 \Delta P_{\alpha'}}{0.109} = 2.29 W / m^2 \quad (D-4)$$

661

662 We note in Eq. 8 we required 1.5% albedo change to resolve 96% of global warming. In this alternate method, the  
 663 estimate is 1.43%, which is in reasonable agreement.

664

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667 Conflicts of Interest: The author declares that there are no conflicts of interest.

668

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