

**Analyzing some equations concerning the “Classical Stability with Broken Supersymmetry” by Ramanujan’s mathematics. Further possible mathematical connections with some parameters of Particle Physics and String Theory.**

**Michele Nardelli<sup>1</sup>, Antonio Nardelli**

**Abstract**

*In this research thesis, we have analyzed and deepened some equations concerning the “Classical Stability with Broken Supersymmetry” by Ramanujan’s mathematics and described new possible mathematical connections with some parameters of Particle Physics and String Theory.*

---

<sup>1</sup> M.Nardelli studied at Dipartimento di Scienze della Terra Università degli Studi di Napoli Federico II, Largo S. Marcellino, 10 - 80138 Napoli, Dipartimento di Matematica ed Applicazioni “R. Caccioppoli” - Università degli Studi di Napoli “Federico II” – Polo delle Scienze e delle Tecnologie Monte S. Angelo, Via Cintia (Fuorigrotta), 80126 Napoli, Italy

$$\sqrt{\frac{\pi e}{2}} = \frac{1}{1 + \frac{1}{1 + \frac{2}{1 + \frac{3}{1 + \frac{4}{1 + \frac{5}{1 + \frac{6}{1 + \frac{7}{1 + \frac{8}{\ddots}}}}}}}}}} + \left\{ 1 + \frac{1}{1 \cdot 3} + \frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{1 \cdot 3 \cdot 5 \cdot 7} + \frac{1}{1 \cdot 3 \cdot 5 \cdot 7 \cdot 9} + \dots \right\}$$


Srinivasa Ramanujan  
1887 - 1920

<https://twitter.com/pickover/status/1056696709961650176>

From:

## Rotating strings confronting PDG mesons

Jacob Sonnenschein and Dorin Weissman - arXiv:1402.5603v1 [hep-ph] 23 Feb 2014

Traj.	$N$	$m$	$\alpha'$	$a$
$\pi/\pi_2$	4 + 3	$m_{u/d} = 110 - 250$	0.788 - 0.852	$a_0 = (-0.22) - (-0.00)$ $a_2 = (-0.00) - 0.26$
$a_1$	4	$m_{u/d} = 0 - 390$	0.783 - 0.849	$(-0.18) - 0.21$
$h_1$	4	$m_{u/d} = 0 - 235$	0.833 - 0.850	$(-0.14) - (-0.02)$
$\omega/\omega_3$	5 + 3	$m_{u/d} = 255 - 390$	0.988 - 1.18	$a_1 = 0.81 - 1.00$ $a_3 = 0.95 - 1.15$
$\phi$	3	$m_s = 510 - 520$	1.072 - 1.112	1.00
$\Psi$	4	$m_c = 1380 - 1460$	0.494 - 0.547	0.71 - 0.88
$\Upsilon$	6	$m_b = 4725 - 4740$	0.455 - 0.471	1.00
$\chi_b$	3	$m_b = 4800$	0.499	0.58

**Table 2.** The results of the meson fits in the  $(n, M^2)$  plane. The ranges listed are those where  $\chi^2$  is within 10% of its optimal value.  $N$  is the number of data points in the trajectory.

## Rogers-Ramanujan continued fraction

$$\frac{1}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \dots}}}}} = e^{2\pi/5} \left( \sqrt{\Phi \sqrt{5} - \Phi} \right) = 0,9981360456 \dots$$

<http://villemin.gerard.free.fr/Wwwgvm/Nombre/FracRama.htm>

With regard the Non-Supersymmetric Vacua, we have the following equations (5.33) and (5.34) concerning the scalar perturbations:

From:

### **On Classical Stability with Broken Supersymmetry**

*I. Basile, J. Mourad and A. Sagnotti - arXiv:1811.11448v2 [hep-th] 10 Jan 2019*

Substituting these expressions in the first of eqs. (5.26) finally leads to a second-order eigenvalue equation for  $m^2$ :

$$A'' + A' \left( 24\Omega' - \frac{2}{\phi'} e^{2\Omega} V_\phi \right) + A \left( m^2 - \frac{7}{4} e^{2\Omega} V - 14 e^{2\Omega} \Omega' \frac{V_\phi}{\phi'} \right) = 0. \quad (5.33)$$

There is nothing else, since differentiating the third of eqs. (5.26) and using the background equations gives

$$\phi' \phi'' = -8A'' - 120A'\Omega' + 8e^{2\Omega} \frac{V_\phi}{\phi'} A' + 56e^{2\Omega} \frac{V_\phi}{\phi'} \Omega' A + 7e^{2\Omega} V A, \quad (5.34)$$

Taking this result into account, one can verify that the last of eqs. (5.26) also leads to (5.33), whose properties we now turn to discuss.

From:

$$A'' + A' \left( 24\Omega' - \frac{2}{\phi'} e^{2\Omega} V_\phi \right) + A \left( m^2 - \frac{7}{4} e^{2\Omega} V - 14 e^{2\Omega} \Omega' \frac{V_\phi}{\phi'} \right) = 0$$

We have that:

From:

**Modular equations and approximations to  $\pi$  – Srinivasa Ramanujan**  
 Quarterly Journal of Mathematics, XLV, 1914, 350 – 372

$$64g_{22}^{24} = e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots,$$

$$64g_{22}^{-24} = 4096e^{-\pi\sqrt{22}} + \dots,$$

$$64(g_{22}^{24} + g_{22}^{-24}) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots = 64\{(1 + \sqrt{2})^{12} + (1 - \sqrt{2})^{12}\}$$

We put:

$$\left( A'' + A' \left( 24\Omega' - \frac{2}{\phi'} e^{2\Omega} V_\phi \right) \right) = e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots$$

$$\left( A \left( m^2 - \frac{7}{4} e^{2\Omega} V - 14e^{2\Omega} \Omega' \frac{V_\phi}{\phi'} \right) \right) = e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} + \dots$$

Thence:

$$A'' + A' \left( 24\Omega' - \frac{2}{\phi'} e^{2\Omega} V_\phi \right) + A \left( m^2 - \frac{7}{4} e^{2\Omega} V - 14e^{2\Omega} \Omega' \frac{V_\phi}{\phi'} \right) = 0$$

$$e^{(\pi\sqrt{22})} - 24 + 276e^{(-\pi\sqrt{22})} + e^{(\pi\sqrt{22})} - 24 + 4372e^{(-\pi\sqrt{22})}$$

**Input:**

$$e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} + e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}}$$

**Exact result:**

$$-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}$$

**Decimal approximation:**

$$5.01785599836741526610154931939557024423276967565237470... \times 10^6$$

5017856

**Property:**

$-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}$  is a transcendental number

**Alternate forms:**

$$2 \left( -24 + 2324 e^{-\sqrt{22} \pi} + e^{\sqrt{22} \pi} \right)$$

$$2 e^{-\sqrt{22} \pi} \left( 2324 - 24 e^{\sqrt{22} \pi} + e^{2\sqrt{22} \pi} \right)$$

**Series representations:**

$$e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} = 2 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \left( 2324 - 24 e^{\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} + e^{2\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \right)$$

$$e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} = 2 \exp \left( -\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \binom{-1/2}{k}}{k!} \right) \left( 2324 - 24 e^{\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \binom{-1/2}{k}}{k!}} + \exp \left( 2\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \binom{-1/2}{k}}{k!} \right) \right)$$

$$e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} = 2 \exp \left( -\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1/2}{k} (22 - z_0)^k z_0^{-k}}{k!} \right) \left( 2324 - 24 \exp \left( \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1/2}{k} (22 - z_0)^k z_0^{-k}}{k!} \right) + \exp \left( 2\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1/2}{k} (22 - z_0)^k z_0^{-k}}{k!} \right) \right)$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\left( \left( \left( \left( \left( e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} \right) \right) + \left( \left( e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} \right) \right) \right) \right) \right)^{1/2}$$

**Input:**

$$\sqrt{\left( e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} \right) + \left( e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} \right)}$$

**Exact result:**

$$\sqrt{-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}}$$

**Decimal approximation:**

2240.057141763891536934239982228162035382247986130420471070...

2240.0571417...  $\approx$  2240 = 64\*35

**Property:**

$$\sqrt{-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}} \text{ is a transcendental number}$$

**Alternate forms:**

$$\sqrt{2(-24 + 2324 e^{-\sqrt{22} \pi} + e^{\sqrt{22} \pi})}$$
$$e^{-\sqrt{11/2} \pi} \sqrt{2(2324 - 24 e^{\sqrt{22} \pi} + e^{2\sqrt{22} \pi})}$$

**All 2nd roots of  $-48 + 4648 e^{(-\sqrt{22} \pi)} + 2 e^{(\sqrt{22} \pi)}$ :**

$$\sqrt{-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}} e^0 \approx 2240. \text{ (real, principal root)}$$

$$\sqrt{-48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi}} e^{i\pi} \approx -2240. \text{ (real root)}$$

**Series representations:**

$$\sqrt{\left(e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}}\right) + \left(e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}}\right)} =$$
$$\sqrt{-49 + 4648 e^{-\pi \sqrt{22}} + 2 e^{\pi \sqrt{22}}} \sum_{k=0}^{\infty} \left(-49 + 4648 e^{-\pi \sqrt{22}} + 2 e^{\pi \sqrt{22}}\right)^{-k} \left(\frac{1}{2}\right)_k$$

$$\sqrt{\left(e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}}\right) + \left(e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}}\right)} =$$
$$\sqrt{-49 + 4648 e^{-\pi \sqrt{22}} + 2 e^{\pi \sqrt{22}}} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-49 + 4648 e^{-\pi \sqrt{22}} + 2 e^{\pi \sqrt{22}}\right)^{-k} \left(-\frac{1}{2}\right)_k}{k!}$$

$$\sqrt{\left(e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}}\right) + \left(e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}}\right)} =$$
$$\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k \left(-48 + 4648 e^{-\pi \sqrt{22}} + 2 e^{\pi \sqrt{22}} - z_0\right)^k z_0^{-k}}{k!}$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

**Integral representation:**

$$(1+z)^\alpha = \frac{\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(s)\Gamma(-\alpha-s)}{z^s} ds}{(2\pi i)\Gamma(-\alpha)} \quad \text{for } (0 < \gamma < -\text{Re}(\alpha) \text{ and } |\arg(z)| < \pi)$$

$$\left( \left( \left( \left( e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} \right) \right) + \left( \left( e^{\pi\sqrt{22}} - 24 + 4372e^{-\pi\sqrt{22}} \right) \right) \right) \right)^{1/2} - 2 \times 64$$

**Input:**

$$\sqrt{\left( e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}} \right) + \left( e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}} \right)} - 2 \times 64$$

**Exact result:**

$$\sqrt{-48 + 4648 e^{-\sqrt{22}\pi} + 2 e^{\sqrt{22}\pi}} - 128$$

**Decimal approximation:**

2112.057141763891536934239982228162035382247986130420471070...

2112.0571417... result practically equal to the rest mass of strange D meson 2112.3

**Property:**

$-128 + \sqrt{-48 + 4648 e^{-\sqrt{22}\pi} + 2 e^{\sqrt{22}\pi}}$  is a transcendental number

**Alternate forms:**

$$\sqrt{2\left(-24 + 2324 e^{-\sqrt{22}\pi} + e^{\sqrt{22}\pi}\right)} - 128$$

$$e^{-\sqrt{11/2}\pi} \sqrt{2\left(2324 - 24 e^{\sqrt{22}\pi} + e^{2\sqrt{22}\pi}\right)} - 128$$

$$e^{-\sqrt{11/2}\pi} \left( \sqrt{2\left(2324 - 24 e^{\sqrt{22}\pi} + e^{2\sqrt{22}\pi}\right)} - 128 e^{\sqrt{11/2}\pi} \right)$$

**Series representations:**

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} - 2 \times 64 = -128 +$$

$$\sqrt{2} \sqrt{e^{-\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \left(2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} + e^{2\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}\right)}$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} - 2 \times 64 =$$

$$-128 + \sqrt{2} \sqrt{\left(\exp\left(-\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)\right.$$

$$\left.\left(2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}} + \exp\left(2\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)\right)\right)}$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} - 2 \times 64 =$$

$$-128 + \sqrt{\left(-48 + 4648 \exp\left[-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right]\right) +$$

$$2 \exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)}$$

2240.0571417 - 2112.0571417

**Input interpretation:**

2240.0571417 - 2112.0571417

**Result:**

128

128

((((((e^(Pi\*sqrt22) - 24 + 276\*e^(-Pi\*sqrt22)))))) + (((e^(Pi\*sqrt22) - 24 + 4372\*e^(-Pi\*sqrt22))))))^1/2 - 2112.0571417 - Pi + 1/golden ratio

**Input interpretation:**

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} - 2112.0571417 - \pi + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

125.4764414...

125.4764414... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Series representations:**

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} - 2112.05714170000 -$$

$$\pi + \frac{1}{\phi} = \frac{1}{\phi} 1.4142135623731 \left( 0.70710678118655 - 1493.4499271495 \phi + \right.$$

$$1.000000000000000 \left. \sqrt{\left( e^{-\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \left( 2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} + \right. \right. \right.$$

$$\left. \left. \left. e^{2\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \right) \right) \right) \phi - 0.70710678118655 \phi \pi \right)$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} -$$

$$2112.05714170000 - \pi + \frac{1}{\phi} = \frac{1}{\phi} 1.4142135623731$$

$$\left( 0.70710678118655 - 1493.4499271495 \phi + 1.000000000000000 \right.$$

$$\left. \sqrt{\left( \exp\left(-\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right) \left( 2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}} + \right. \right. \right.$$

$$\left. \left. \left. \exp\left(2\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right) \right) \right) \right) \phi - 0.70710678118655 \phi \pi \right)$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right) - 2112.05714170000 - \pi + \frac{1}{\phi} = \frac{1}{\phi} 1.0000000000000000} \\ \left(1.0000000000000000 - 2112.0571417000 \phi + 1.0000000000000000 \right. \\ \left. \sqrt{\left(-48 + 4648 \exp\left[-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)\right]}{2\sqrt{\pi}}\right) + 2 \exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)\right)}{2\sqrt{\pi}}\right)} \right) \phi - 1.0000000000000000 \phi \pi$$

((((((e^(Pi\*sqrt22) - 24 + 276\*e^(-Pi\*sqrt22)))))) + (((e^(Pi\*sqrt22) - 24 + 4372\*e^(-Pi\*sqrt22))))))^(1/2) - 2112.0571417 + 11 + 1/golden ratio

**Input interpretation:**

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right) - 2112.0571417 + 11 + \frac{1}{\phi}}$$

φ is the golden ratio

**Result:**

139.6180341...

139.6180341... result practically equal to the rest mass of Pion meson 139.57 MeV

**Series representations:**

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right) - 2112.05714170000 + 11 + \frac{1}{\phi} = \frac{1}{\phi} 1.4142135623731 \left(0.70710678118655 - 1485.6717525565 \phi + 1.0000000000000000 \sqrt{\left(e^{-\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \left(2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} + e^{2\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}\right)\right)} \right) \phi$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} -$$

$$2112.05714170000 + 11 + \frac{1}{\phi} = \frac{1}{\phi} 1.4142135623731 \left( 0.70710678118655 -$$

$$1485.6717525565 \phi + 1.0000000000000000 \sqrt{\left(\exp\left(-\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)\right.$$

$$\left.\left(2324 - 24 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}} + \exp\left(2\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)\right)\right) \phi$$

$$\sqrt{\left(e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}}\right) + \left(e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}}\right)} -$$

$$2112.05714170000 + 11 + \frac{1}{\phi} = \frac{1}{\phi} 1.0000000000000000$$

$$\left( 1.0000000000000000 - 2101.0571417000 \phi + 1.0000000000000000$$

$$\sqrt{\left(-48 + 4648 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)\right.}$$

$$\left.2 \exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)\right) \phi$$

We note that:

$$\frac{1}{64} \left( \left( e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}} + e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}} \right) - 64^2 - 728 - 89 \right)$$

where  $728 = 9^3 - 1$  and 89 is a Fibonacci number

**Input:**

$$\frac{1}{64} \left( e^{\pi\sqrt{22}} - 24 + 276 e^{-\pi\sqrt{22}} + e^{\pi\sqrt{22}} - 24 + 4372 e^{-\pi\sqrt{22}} \right) - 64^2 - 728 - 89$$

**Exact result:**

$$\frac{1}{64} \left( -48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi} \right) - 4913$$

**Decimal approximation:**

73490.99997449086353283670811555578506613702618206835477081...

73490.999...

**Property:**

$-4913 + \frac{1}{64} \left( -48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi} \right)$  is a transcendental number

**Alternate forms:**

$$\frac{1}{32} \left( -157240 + 2324 e^{-\sqrt{22} \pi} + e^{\sqrt{22} \pi} \right)$$

$$-\frac{19655}{4} + \frac{581}{8} e^{-\sqrt{22} \pi} + \frac{e^{\sqrt{22} \pi}}{32}$$

$$\frac{1}{32} e^{-\sqrt{22} \pi} \left( 2324 - 157240 e^{\sqrt{22} \pi} + e^{2\sqrt{22} \pi} \right)$$

**Series representations:**

$$\begin{aligned} & \frac{1}{64} \left( e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} \right) - 64^2 - 728 - 89 = \\ & \frac{1}{32} e^{-\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} \left( 2324 - 157240 e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} + e^{2\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} \right) \end{aligned}$$

$$\begin{aligned} & \frac{1}{64} \left( e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} \right) - 64^2 - 728 - 89 = \\ & \frac{1}{32} \exp \left( -\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right) \\ & \left( 2324 - 157240 e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!} + \exp \left( 2\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right) \right) \end{aligned}$$

$$\begin{aligned} & \frac{1}{64} \left( e^{\pi \sqrt{22}} - 24 + 276 e^{-\pi \sqrt{22}} + e^{\pi \sqrt{22}} - 24 + 4372 e^{-\pi \sqrt{22}} \right) - 64^2 - 728 - 89 = \\ & \frac{1}{32} \exp \left( -\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (22 - z_0)^k z_0^{-k}}{k!} \right) \\ & \left( 2324 - 157240 \exp \left( \pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (22 - z_0)^k z_0^{-k}}{k!} \right) + \right. \\ & \left. \exp \left( 2\pi \sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (22 - z_0)^k z_0^{-k}}{k!} \right) \right) \end{aligned}$$

for not  $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

Thence, we have the following mathematical connections:

$$\begin{aligned}
& \left( \frac{1}{64} \left( -48 + 4648 e^{-\sqrt{22} \pi} + 2 e^{\sqrt{22} \pi} \right) - 4913 \right) = 73490.999... \Rightarrow \\
& \Rightarrow -3927 + 2 \left( \sqrt[13]{ N \exp \left[ \int d\hat{\sigma} \left( -\frac{1}{4u^2} P_i D P_i \right) \right] |Bp\rangle_{\text{NS}} + \int [dX^\mu] \exp \left\{ \int d\hat{\sigma} \left( -\frac{1}{4v^2} D X^\mu D^2 X^\mu \right) \right\} |X^\mu, X^i = 0\rangle_{\text{NS}} } \right) = \\
& -3927 + 2 \sqrt[13]{ 2.2983717437 \times 10^{59} + 2.0823329825883 \times 10^{59} } \\
& = 73490.8437525.... \Rightarrow \\
& \Rightarrow \left( A(r) \times \frac{1}{B(r)} \left( -\frac{1}{\phi(r)} \right) \times \frac{1}{e^{\Lambda(r)}} \right) \Rightarrow \\
& \Rightarrow \left( -0.000029211892 \times \frac{1}{0.0003644621} \left( -\frac{1}{0.0005946833} \right) \times \frac{1}{0.00183393} \right) = \\
& = 73491.78832548118710549159572042220548025195726563413398700... \\
& = 73491.7883254... \Rightarrow \\
& \left( I_{21} \ll \int_{-\infty}^{+\infty} \exp \left( -\left( \frac{t}{H} \right)^2 \right) \left| \sum_{\lambda \leq p^{1-\epsilon_1}} \frac{a(\lambda)}{\sqrt{\lambda}} B(\lambda) \lambda^{-i(T+t)} \right|^2 dt \ll \right. \\
& \left. \ll H \left\{ \left( \frac{4}{\epsilon_2 \log T} \right)^{2r} (\log T) (\log X)^{-2\beta} + (\epsilon_2^{-2r} (\log T)^{-2r} + \epsilon_2^{-r} h_1^r (\log T)^{-r} \right) T^{-\epsilon_1} \right\} \right) \\
& / (26 \times 4)^2 - 24 = \left( \frac{7.9313976505275 \times 10^8}{(26 \times 4)^2 - 24} \right) = 73493.30662...
\end{aligned}$$

Mathematical connections with the boundary state corresponding to the NSNS-sector of N Dp-branes in the limit of  $u \rightarrow \infty$ , with the ratio concerning the general

asymptotically flat solution of the equations of motion of the p-brane and with the Karatsuba's equation concerning the zeros of a special type of function connected with Dirichlet series.

From

$$\phi' \phi'' = -8A'' - 120A'\Omega' + 8e^{2\Omega} \frac{V_\phi}{\phi'} A' + 56e^{2\Omega} \frac{V_\phi}{\phi'} \Omega' A + 7e^{2\Omega} V A,$$

For  $\phi'$  equal to the following Rogers-Ramanujan continued fraction

$$\frac{1}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \dots}}}}} = e^{2\pi/5} \left( \sqrt{\Phi \sqrt{5} - \Phi} \right) = 0,9981360456 \dots$$

$V_\phi = 138$ ,  $V = 0.57142857$  and  $\Omega' = \pi$ , we obtain:

-8-

$$120\pi + 8 * e^{(\pi * \sqrt{22})} * (138 / 0.9981360456) + 56 * e^{(\pi * \sqrt{22})} * (138 * \pi / 0.9981360456) + 7 * 0.57142857 * e^{(\pi * \sqrt{22})}$$

**Input interpretation:**

$$-8 - 120\pi + 8 e^{\pi \sqrt{22}} \times \frac{138}{0.9981360456} + 56 e^{\pi \sqrt{22}} \left( 138 \times \frac{\pi}{0.9981360456} \right) + 7 \times 0.57142857 e^{\pi \sqrt{22}}$$

**Result:**

$$6.381175064... \times 10^{10}$$

$$6.381175064 * 10^{10}$$

**Series representations:**

$$-8 - 120\pi + \frac{(8 e^{\pi\sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi\sqrt{22}}) 138\pi}{0.998136} + 7 \times 0.571429 e^{\pi\sqrt{22}} = 7742.43$$

$$\left( -0.00103327 + 0.143374 e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} - 0.015499\pi + e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} \pi \right)$$

$$-8 - 120\pi + \frac{(8 e^{\pi\sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi\sqrt{22}}) 138\pi}{0.998136} + 7 \times 0.571429 e^{\pi\sqrt{22}} =$$

$$-8(1 + 15\pi) + e^{\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1}{k}}{k!}} (1110.06 + 7742.43\pi)$$

$$-8 - 120\pi + \frac{(8 e^{\pi\sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi\sqrt{22}}) 138\pi}{0.998136} + 7 \times 0.571429 e^{\pi\sqrt{22}} =$$

$$-8(1 + 15\pi) + \exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{2\sqrt{\pi}}\right) (1110.06 + 7742.43\pi)$$

(((8-120Pi+8\*e^(Pi\*sqrt22))\*((x+13)/0.9981360456)+56\*e^(Pi\*sqrt22))\*((x+13)\*Pi/0.9981360456)+7\*0.57142857\*e^(Pi\*sqrt22))))=6.381175064e+10

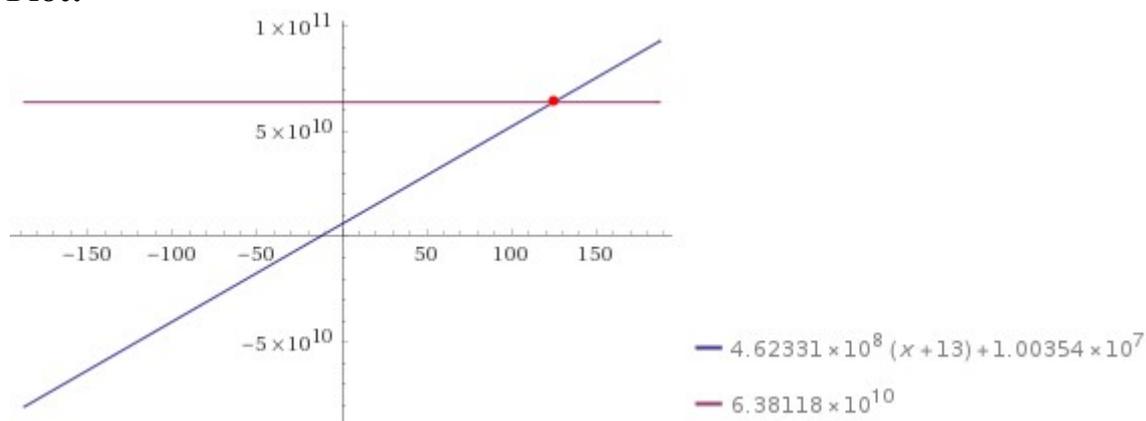
### Input interpretation:

$$-8 - 120\pi + 8 e^{\pi\sqrt{22}} \times \frac{x + 13}{0.9981360456} + 56 e^{\pi\sqrt{22}} \left( (x + 13) \times \frac{\pi}{0.9981360456} \right) + 7 \times 0.57142857 e^{\pi\sqrt{22}} = 6.381175064 \times 10^{10}$$

### Result:

$$4.62331 \times 10^8 (x + 13) + 1.00354 \times 10^7 = 6.38118 \times 10^{10}$$

### Plot:



### Alternate forms:

$$4.62331 \times 10^8 (x + 13.0217) = 6.38118 \times 10^{10}$$

$$4.62331 \times 10^8 x - 5.77914 \times 10^{10} = 0$$

$$4.62331 \times 10^8 x + 6.02034 \times 10^9 = 6.38118 \times 10^{10}$$

**Solution:**

$$x \approx 125.$$

125 result practically equal to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

$$((( -8 - 120\pi + 8 * e^{(\pi * \sqrt{22})} * ((x - \text{golden ratio}) / 0.9981360456) + 56 * e^{(\pi * \sqrt{22})} * ((x - \text{golden ratio}) * \pi / 0.9981360456) + 7 * 0.57142857 * e^{(\pi * \sqrt{22})} )))) = 6.381175064e+10$$

**Input interpretation:**

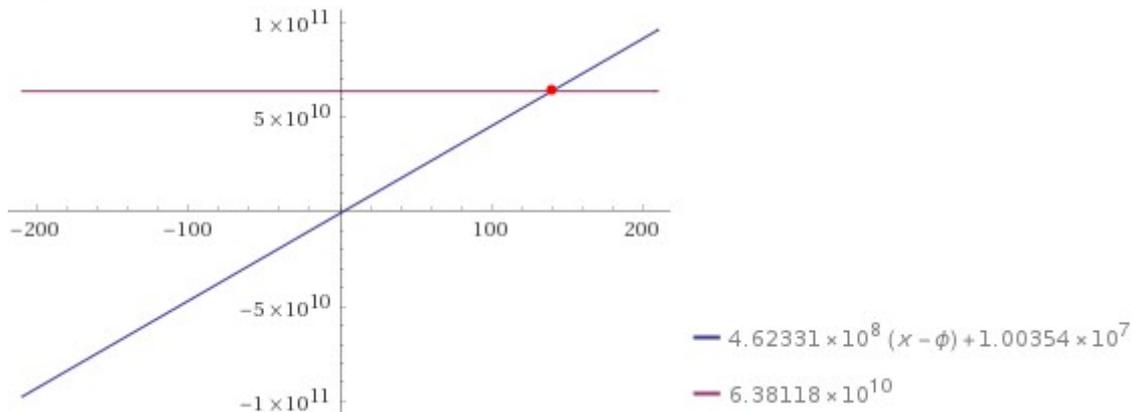
$$-8 - 120\pi + 8 e^{\pi \sqrt{22}} \times \frac{x - \phi}{0.9981360456} + 56 e^{\pi \sqrt{22}} \left( (x - \phi) \times \frac{\pi}{0.9981360456} \right) + 7 \times 0.57142857 e^{\pi \sqrt{22}} = 6.381175064 \times 10^{10}$$

$\phi$  is the golden ratio

**Result:**

$$4.62331 \times 10^8 (x - \phi) + 1.00354 \times 10^7 = 6.38118 \times 10^{10}$$

**Plot:**



**Alternate forms:**

$$4.62331 \times 10^8 (x - 1.59633) = 6.38118 \times 10^{10}$$

$$4.62331 \times 10^8 x - 6.45498 \times 10^{10} = 0$$

$$4.62331 \times 10^8 x - 7.38032 \times 10^8 = 6.38118 \times 10^{10}$$

**Solution:**

$$x \approx 139.618$$

139.618 result practically equal to the rest mass of Pion meson 139.57 MeV

$$72 \cdot \ln \left( \left( -8 - 120\pi + 8 e^{\pi \sqrt{22}} \times \frac{138}{0.9981360456} + 56 e^{\pi \sqrt{22}} \left( 138 \times \frac{\pi}{0.9981360456} \right) + 7 \times 0.57142857 e^{\pi \sqrt{22}} \right) \right) - 64 + \phi$$

**Input interpretation:**

$$72 \log \left( -8 - 120 \pi + 8 e^{\pi \sqrt{22}} \times \frac{138}{0.9981360456} + 56 e^{\pi \sqrt{22}} \left( 138 \times \frac{\pi}{0.9981360456} \right) + 7 \times 0.57142857 e^{\pi \sqrt{22}} \right) - 64 + \phi$$

log(x) is the natural logarithm

φ is the golden ratio

**Result:**

$$1728.9206636...$$

$$1728.9206636...$$

This result is very near to the mass of candidate glueball f<sub>0</sub>(1710) meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

**Alternative representations:**

$$72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - 64 +$$

$$\phi = -64 + \phi + 72 \log_e \left( -8 - 120 \pi + 4. e^{\pi \sqrt{22}} + \frac{1104 e^{\pi \sqrt{22}}}{0.998136} + \frac{7728 \pi e^{\pi \sqrt{22}}}{0.998136} \right)$$

$$72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - 64 +$$

$$\phi = -64 + \phi + 72 \log(a) \log_a \left( -8 - 120 \pi + 4. e^{\pi \sqrt{22}} + \frac{1104 e^{\pi \sqrt{22}}}{0.998136} + \frac{7728 \pi e^{\pi \sqrt{22}}}{0.998136} \right)$$

$$72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - 64 +$$

$$\phi = -64 + \phi - 72 \operatorname{Li}_1 \left( 9 + 120 \pi - 4. e^{\pi \sqrt{22}} - \frac{1104 e^{\pi \sqrt{22}}}{0.998136} - \frac{7728 \pi e^{\pi \sqrt{22}}}{0.998136} \right)$$

$\log_b(x)$  is the base-  $b$  logarithm

$\operatorname{Li}_n(x)$  is the polylogarithm function

### Series representations:

$$72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - 64 +$$

$$\phi = -64 + \phi + 72 \log \left( -8 (1 + 15 \pi) + e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (1110.06 + 7742.43 \pi) \right)$$

$$72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) -$$

$$64 + \phi = -64 + \phi + 72 \log \left( -3 (3 + 40 \pi) + e^{\pi \sqrt{22}} (1110.06 + 7742.43 \pi) \right) -$$

$$72 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -3 (3 + 40 \pi) + e^{\pi \sqrt{22}} (1110.06 + 7742.43 \pi) \right)^{-k}}{k}$$

$$\begin{aligned}
& 72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - \\
& 64 + \phi = \\
& -64 + \phi + 144 i \pi \left[ \frac{\arg \left( -8 - 120 \pi + e^{\pi \sqrt{22}} (1110.06 + 7742.43 \pi) - x \right)}{2 \pi} \right] + 72 \log(x) - \\
& 72 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -8 - 120 \pi + e^{\pi \sqrt{22}} (1110.06 + 7742.43 \pi) - x \right)^k x^{-k}}{k} \quad \text{for } x < 0
\end{aligned}$$

### Integral representations:

$$\begin{aligned}
& 72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - \\
& 64 + \phi = -64 + \phi + 72 \int_1^{-8(1+15\pi)+e^{\pi\sqrt{22}}(1110.06+7742.43\pi)} \frac{1}{t} dt
\end{aligned}$$

$$\begin{aligned}
& 72 \log \left( -8 - 120 \pi + \frac{(8 e^{\pi \sqrt{22}}) 138}{0.998136} + \frac{(56 e^{\pi \sqrt{22}}) 138 \pi}{0.998136} + 7 \times 0.571429 e^{\pi \sqrt{22}} \right) - \\
& 64 + \phi = -64 + \phi + \\
& \frac{36}{i \pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left( -3(3+40\pi) + e^{\pi\sqrt{22}}(1110.06+7742.43\pi) \right)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \\
& \text{for } -1 < \gamma < 0
\end{aligned}$$

Now, we have that:

$$\beta^2 \sigma_7 + \frac{5\sigma_7}{2} + \frac{\tau_7}{2} + 6 \pm \frac{1}{2} \sqrt{(4\beta^4 + 40\beta^2 + 25)\sigma_7^2 + 4(\tau_7 - 12)(\beta^2 - 5/2)\sigma_7 + (\tau_7 - 12)^2}.$$

$$\sigma_7 = 15, \quad \tau_7 = 75, \quad \beta = -1 \quad (4.30) - (4.31)$$

$$15 + 75/2 + 75/2 + 6 + 1/2 * \text{sqrt}(\text{((((4+40+25)15^2+4(75-12)(1-5/2)15+(75-12)^2))))$$

**Input:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) \times 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) \times 15 + (75 - 12)^2}$$

**Result:**

$$96 + 24\sqrt{6}$$

**Decimal approximation:**

154.7877538267962743567348177929413934071827395357600830823...

154.7877538...

**Alternate form:**

$$24(4 + \sqrt{6})$$

**Minimal polynomial:**

$$x^2 - 192x + 5760$$

We have also:

$$15 + 75/2 + 75/2 + 6 + 1/2 * \text{sqrt}(\text{((((4+40+25)15^2+4(75-12)(1-5/2)15+(75-12)^2)))) - 13 - \text{golden ratio}^2$$

**Input:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) \times 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) \times 15 + (75 - 12)^2 - 13 - \phi^2}$$

$\phi$  is the golden ratio

**Result:**

$$-\phi^2 + 83 + 24\sqrt{6}$$

**Decimal approximation:**

139.1697198380463795085302309585757552894624303559543202202...

139.169719... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternate forms:**

$$\frac{1}{2} (163 - \sqrt{5} + 48 \sqrt{6})$$

$$\frac{163}{2} - \frac{\sqrt{5}}{2} + 24 \sqrt{6}$$

$$\frac{1}{2} \left( 163 + \sqrt{13829 - 96 \sqrt{30}} \right)$$

**Minimal polynomial:**

$$x^4 - 326x^3 + 32939x^2 - 1038310x + 10126945$$

**Series representations:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4+40+25)15^2 + 4(75-12)\left(1-\frac{5}{2}\right)15 + (75-12)^2} -$$

$$13 - \phi^2 = 83 - \phi^2 + \frac{1}{2} \sqrt{13823} \sum_{k=0}^{\infty} 13823^{-k} \binom{\frac{1}{2}}{k}$$

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4+40+25)15^2 + 4(75-12)\left(1-\frac{5}{2}\right)15 + (75-12)^2} -$$

$$13 - \phi^2 = 83 - \phi^2 + \frac{1}{2} \sqrt{13823} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{13823}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4+40+25)15^2 + 4(75-12)\left(1-\frac{5}{2}\right)15 + (75-12)^2} -$$

$$13 - \phi^2 = 83 - \phi^2 + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 13823^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{4\sqrt{\pi}}$$

And:

$$15 + 75/2 + 75/2 + 6 + 1/2 * \text{sqrt}(\left(\left(\left(4+40+25\right)15^2 + 4\left(75-12\right)\left(1-5/2\right)15 + \left(75-12\right)^2\right)\right)) - 29 -$$

1/golden ratio

**Input:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) \times 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) \times 15 + (75 - 12)^2} - 29 - \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$-\frac{1}{\phi} + 67 + 24 \sqrt{6}$$

**Decimal approximation:**

125.1697198380463795085302309585757552894624303559543202202...

125.1697198... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Alternate forms:**

$$\frac{1}{2} (135 - \sqrt{5} + 48 \sqrt{6})$$

$$\frac{(-67 - 24 \sqrt{6}) \phi + 1}{\phi}$$

$$\frac{1}{2} \left( 135 + \sqrt{13829 - 96 \sqrt{30}} \right)$$

**Minimal polynomial:**

$$x^4 - 270 x^3 + 20423 x^2 - 296730 x + 1190521$$

**Series representations:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) 15 + (75 - 12)^2} - 29 - \frac{1}{\phi} = 67 - \frac{1}{\phi} + \frac{1}{2} \sqrt{13823} \sum_{k=0}^{\infty} 13823^{-k} \binom{\frac{1}{2}}{k}$$

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) 15 + (75 - 12)^2} -$$

$$29 - \frac{1}{\phi} = 67 - \frac{1}{\phi} + \frac{1}{2} \sqrt{13823} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{13823}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$15 + \frac{75}{2} + \frac{75}{2} + 6 + \frac{1}{2} \sqrt{(4 + 40 + 25) 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) 15 + (75 - 12)^2} -$$

$$29 - \frac{1}{\phi} = 67 - \frac{1}{\phi} + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 13823^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{4\sqrt{\pi}}$$

$$15+75/2+75/2+6-1/2 * \text{sqrt}((((4+40+25)15^2+4(75-12)(1-5/2)15+(75-12)^2)))$$

**Input:**

$$15 + \frac{75}{2} + \frac{75}{2} + 6 - \frac{1}{2} \sqrt{(4 + 40 + 25) \times 15^2 + 4(75 - 12) \left(1 - \frac{5}{2}\right) \times 15 + (75 - 12)^2}$$

**Result:**

$$96 - 24\sqrt{6}$$

**Decimal approximation:**

37.21224617320372564326518220705860659281726046423991691761...

37.212246...

**Alternate forms:**

$$24(4 - \sqrt{6})$$

$$-24(\sqrt{6} - 4)$$

**Minimal polynomial:**

$$x^2 - 192x + 5760$$

Now, we have that:

$$\beta^2 \sigma_3 + \frac{3\sigma_3}{2} + \frac{\tau_3}{2} + 2 \pm \frac{1}{2} \sqrt{4\beta^4 \sigma_3^2 + 16\sigma_3 \left( \sigma_3 + \frac{\tau_3}{4} - 1 \right) \beta^2 + 9 \left( \sigma_3 - \frac{\tau_3}{3} + \frac{4}{3} \right)^2}. \quad (3.41)$$

There are regions of instability as one varies the parameters, but for the actual orientifold potential, where  $(\beta, \sigma_3, \tau_3) = (1, \frac{3}{2}, \frac{9}{2})$ , the two eigenvalues,

$$3/2 + 3/2 * 3/2 + 9/2 * 1/2 + 2 + 1/2 * \text{sqrt}(((4*9/4 + 16*3/2(3/2 + 9/2 * 1/4 - 1) + 9(3/2 - 9/2 * 1/3 + 4/3)^2)))$$

**Input:**

$$\frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2}$$

**Exact result:**

12

12

$$3/2 + 3/2 * 3/2 + 9/2 * 1/2 + 2 - 1/2 * \text{sqrt}(((4*9/4 + 16*3/2(3/2 + 9/2 * 1/4 - 1) + 9(3/2 - 9/2 * 1/3 + 4/3)^2)))$$

**Input:**

$$\frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 - \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2}$$

**Exact result:**

4

4

$$((((3/2 + 3/2 * 3/2 + 9/2 * 1/2 + 2 + 1/2 * \text{sqrt}(((4*9/4 + 16*3/2(3/2 + 9/2 * 1/4 - 1) + 9(3/2 - 9/2 * 1/3 + 4/3)^2)))))))))^2$$

**Input:**

$$\left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2$$

**Exact result:**

144

144

$$12 * (((((3/2 + 3/2 * 3/2 + 9/2 * 1/2 + 2 + 1/2 * \sqrt{((4 * 9/4 + 16 * 3/2(3/2 + 9/2 * 1/4 - 1) + 9(3/2 - 9/2 * 1/3 + 4/3)^2))})))))) ^ 2$$

**Input:**

$$12 \left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2$$

**Exact result:**

1728

1728

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

$$(((3/2 + 3/2 * 3/2 + 9/2 * 1/2 + 2 + 1/2 * \sqrt{((4 * 9/4 + 16 * 3/2(3/2 + 9/2 * 1/4 - 1) + 9(3/2 - 9/2 * 1/3 + 4/3)^2))})))) ^ 2 - 5 + 1/\text{golden ratio}$$

**Input:**

$$\left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2 - 5 + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$\frac{1}{\phi} + 139$$

**Decimal approximation:**

139.6180339887498948482045868343656381177203091798057628621...

139.61803398.... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternate forms:**

$$\frac{1}{2} (277 + \sqrt{5})$$

$$\frac{139\phi + 1}{\phi}$$

$$\frac{\sqrt{5}}{2} + \frac{277}{2}$$

**Series representations:**

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 -$$

$$5 + \frac{1}{\phi} = -5 + \frac{1}{\phi} + \left( 8 + \frac{1}{2} \sqrt{63} \sum_{k=0}^{\infty} 63^{-k} \binom{\frac{1}{2}}{k} \right)^2$$

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 -$$

$$5 + \frac{1}{\phi} = -5 + \frac{1}{\phi} + \left( 8 + \frac{1}{2} \sqrt{63} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{63}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^2$$

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 -$$

$$5 + \frac{1}{\phi} = -5 + \frac{1}{\phi} + \left( 8 + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 63^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{4 \sqrt{\pi}} \right)^2$$

(((3/2+3/2\*3/2+9/2\*1/2+2+1/2\*sqrt(((4\*9/4+16\*3/2(3/2+9/2\*1/4-1)+9(3/2-9/2\*1/3+4/3)^2)))))))))^2 - 18 - 1/golden ratio

**Input:**

$$\left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2 - 18 - \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$126 - \frac{1}{\phi}$$

**Decimal approximation:**

125.3819660112501051517954131656343618822796908201942371378...

125.381966.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

**Alternate forms:**

$$\frac{1}{2} (253 - \sqrt{5})$$

$$\frac{126\phi - 1}{\phi}$$

$$-\frac{1 - 126\phi}{\phi}$$

**Series representations:**

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 - 18 - \frac{1}{\phi} = -18 - \frac{1}{\phi} + \left( 8 + \frac{1}{2} \sqrt{63} \sum_{k=0}^{\infty} 63^{-k} \binom{\frac{1}{2}}{k} \right)^2$$

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 -$$

$$18 - \frac{1}{\phi} = -18 - \frac{1}{\phi} + \left( 8 + \frac{1}{2} \sqrt{63} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{63}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)^2$$

$$\left( \frac{3}{2} + \frac{3 \times 3}{2 \times 2} + \frac{9}{2 \times 2} + 2 + \frac{1}{2} \sqrt{\frac{4 \times 9}{4} + \frac{16}{2} \times 3 \left( \frac{3}{2} + \frac{9}{2 \times 4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2 \times 3} + \frac{4}{3} \right)^2} \right)^2 -$$

$$18 - \frac{1}{\phi} = -18 - \frac{1}{\phi} + \left( 8 + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 63^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{4 \sqrt{\pi}} \right)^2$$

We note that:

from: **Manuscript Book 1 of Srinivasa Ramanujan**

Page 177

$$V \equiv \frac{2lmn}{y + \beta - 2ml^2} + \frac{2(1-m)(l^2-n^2)}{1 + \frac{2(1+m)(l^2-l^2)}{3y + \beta + \dots}}$$

$$\frac{2(2-m)(2^2-n^2)}{1 + \frac{2(2+m)(2^2-l^2)}{5y + \beta + \dots}}$$

where  $y = x^2 - (1-m)^2$  &  $\beta = (n^2 - l^2)(1-2m)$ .

$$f/\phi(x,y) = x + \frac{(1+y)^2+n}{2x + \frac{(3+y)^2+n}{2x + \frac{(5+y)^2+n}{2x + \dots}}}$$

then  $\phi(x,y) = \phi(y,x)$ .

For  $x = 2, l = 3, m = 5, n = 8$

$$y = 2^2 - (1-5)^2 = -12$$

$$p = (8^2 - 3^2)(1 - 2*5) = -495$$

$$2*3*5*8 / ((((-12-495-2*5*3^2) + (((2(1-5)(1-8^2)) / (1 + (((((-96 / (-36-495 + (2(2-5)(4-64)) / (1 + (((((-70) / (-60-495))))))))))))))))))$$

**Input:**

$$\frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}}$$

**Exact result:**

$$\frac{204880}{213791}$$

**Decimal approximation:**

-0.95831910604281751804332268430382944090256371877207178973...

-0.958319106...

**Continued fraction:**

$$\cfrac{1}{-1 + \cfrac{1}{-22 + \cfrac{1}{-1 + \cfrac{1}{-121 + \cfrac{1}{-14 + \cfrac{1}{-1 + \cfrac{1}{-1 + \cfrac{1}{2}}}}}}}}}$$

$$[-(2*3*5*8) / ((((-12-495-2*5*3^2) + (((2(1-5)(1-8^2)) / (1 + (((((-96 / (-36-495 + (2(2-5)(4-64)) / (1 + (((((-70) / (-60-495))))))))))))))))))]^{1/64}$$

**Input:**

$$\sqrt[64]{\frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}}}$$

**Result:**

$$\sqrt[64]{\frac{12\,805}{213\,791}} \sqrt[16]{2}$$

**Decimal approximation:**

0.999334995270014233707606973481877009422036043201135085501...

0.999334995... result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} \approx 0.9991104684$$

and to the dilaton value **0.989117352243 =  $\phi$**

**Alternate forms:**

$$\frac{\sqrt[16]{2} \sqrt[64]{12805} \sqrt[63]{213791}}{213791}$$

root of  $213791x^{64} - 204880$  near  $x = 0.999335$

2log base 0.99933499527[-(2\*3\*5\*8)/(((((-12-495-2\*5\*3^2)+(((2(1-5)(1-8^2))/(1+((((((-96)/(-36-495+(2(2-5)(4-64))/(1+((((((-70)/(-60-495))))))))))))))))))] - Pi+1/golden ratio

**Input interpretation:**

$$2 \log_{0.99933499527} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) - \pi + \frac{1}{\phi}$$

$\log_b(x)$  is the base- $b$  logarithm

$\phi$  is the golden ratio

### Result:

125.47644...

125.47644.... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

### Alternative representation:

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) - \pi + \frac{1}{\phi} =$$

$$- \pi + \frac{1}{\phi} + \frac{2 \log \left( \frac{240}{-597 - \frac{8(1-8^2)}{1 - \frac{96}{-531 + \frac{360}{1 - \frac{70}{555}}}}} \right)}{\log(0.999334995270000)}$$

### Series representations:

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left(-\frac{8911}{213791}\right)^k}{k}}{\log(0.999334995270000)}$$

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - 1.000000000000 \pi - 3006.49740532 \log\left(\frac{204880}{213791}\right) -$$

$$2 \log\left(\frac{204880}{213791}\right) \sum_{k=0}^{\infty} (-0.000665004730000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

2log base 0.99933499527[-(2\*3\*5\*8)/(((((-12-495-2\*5\*3^2)+(((2(1-5)(1-8^2))/(1+((((((-96/(-36-495+(2(2-5)(4-64)))/(1+((((((-70)/(-60-495))))))))))))))))))] + 11 + 1/golden ratio

**Input interpretation:**

$$2 \log_{0.99933499527} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) + 11 + \frac{1}{\phi}$$

$\log_b(x)$  is the base- $b$  logarithm

$\phi$  is the golden ratio

**Result:**

139.61803...

139.61803.... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternative representation:**

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{2 \log \left( \frac{240}{-597 - \frac{8(1-8^2)}{1 - \frac{96}{-531 + \frac{360}{1 - \frac{70}{555}}}}} \right)}{\log(0.999334995270000)}$$

**Series representations:**

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} - \frac{2 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -\frac{8911}{213791} \right)^k}{k}}{\log(0.999334995270000)}$$

$$2 \log_{0.999334995270000} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} - 3006.49740532 \log\left(\frac{204880}{213791}\right) -$$

$$2 \log\left(\frac{204880}{213791}\right) \sum_{k=0}^{\infty} (-0.000665004730000)^k G(k)$$

for  $\left( G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

Thence, we have the following mathematical connections:

$$\left[ \left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2 - 18 - \frac{1}{\phi} \right] = 125.381966.. \Rightarrow$$

$$\Rightarrow \left[ 2 \log_{0.99933499527} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) - \pi + \frac{1}{\phi} \right] = 125.47644\dots$$

$$\left[ \left( \frac{3}{2} + \frac{3}{2} \times \frac{3}{2} + \frac{9}{2} \times \frac{1}{2} + 2 + \frac{1}{2} \sqrt{4 \times \frac{9}{4} + 16 \times \frac{3}{2} \left( \frac{3}{2} + \frac{9}{2} \times \frac{1}{4} - 1 \right) + 9 \left( \frac{3}{2} - \frac{9}{2} \times \frac{1}{3} + \frac{4}{3} \right)^2} \right)^2 - 5 + \frac{1}{\phi} \right] = 139.61803398 \Rightarrow$$

$$\Rightarrow \left[ 2 \log_{0.99933499527} \left( \frac{2 \times 3 \times 5 \times 8}{(-12 - 495 - 2 \times 5 \times 3^2) + \frac{2(1-5)(1-8^2)}{1 - \frac{96}{-36-495 + \frac{2(2-5)(4-64)}{1 - \frac{70}{-60-495}}}}} \right) + 11 + \frac{1}{\phi} \right] = 139.61803\dots$$

Now, we have that:

Einstein frame this translates into the dilaton potential [10]

$$V = T e^{\frac{5}{2}\phi} . \tag{1.2}$$

In the heterotic case  $V \sim e^{\frac{5}{2}\phi}$ , and

$$b = \frac{7}{4} e^{2\Omega} V \left( 1 + 20 \frac{\Omega'}{\phi'} \right) . \tag{5.45}$$

For the (1.2) and  $T = 1$ , we obtain:

$$\exp(-5/2*0.9981360456)$$

**Input interpretation:**

$$\exp\left(-\frac{5}{2} \times 0.9981360456\right)$$

**Result:**

0.08246839796...

0.08246839796...

From the (5.45), we obtain:

$$7/4 * e^{(\pi * \sqrt{22})} * 0.08246839796 (1 + 20 * (\pi / 0.9981360456))$$

**Input interpretation:**

$$\frac{7}{4} e^{\pi \sqrt{22}} \times 0.08246839796 \left( 1 + 20 \times \frac{\pi}{0.9981360456} \right)$$

**Result:**

2.315543744...  $\times 10^7$

2.315543744...  $\times 10^7$

**Series representations:**

$$\frac{1}{4} e^{\pi \sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20 \pi}{0.998136} \right) = 0.14432 e^{\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} (1 + 20.0373 \pi)$$

$$\frac{1}{4} e^{\pi \sqrt{22}} 7 \times 0.0824684 \left(1 + \frac{20 \pi}{0.998136}\right) =$$

$$0.14432 e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} \frac{\left(\frac{-1}{21}\right)^k \left(\frac{-1}{2}\right)_k}{k!} (1 + 20.0373 \pi)$$

$$\frac{1}{4} e^{\pi \sqrt{22}} 7 \times 0.0824684 \left(1 + \frac{20 \pi}{0.998136}\right) =$$

$$0.14432 \exp\left(\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right) (1 + 20.0373 \pi)$$

((((1/64^2(((7/4\* e^(Pi\*sqrt22) \* 0.08246839796 (1+20\*(Pi/0.9981360456))))))))))

**Input interpretation:**

$$\frac{1}{64^2} \left(\frac{7}{4} e^{\pi \sqrt{22}} \times 0.08246839796 \left(1 + 20 \times \frac{\pi}{0.9981360456}\right)\right)$$

**Result:**

5653.182970...

5653.18297...

**Series representations:**

$$\frac{e^{\pi \sqrt{22}} 7 \times 0.0824684 \left(1 + \frac{20 \pi}{0.998136}\right)}{4 \times 64^2} =$$

$$0.0000352343 e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (1 + 20.0373 \pi)$$

$$\frac{e^{\pi \sqrt{22}} 7 \times 0.0824684 \left(1 + \frac{20 \pi}{0.998136}\right)}{4 \times 64^2} =$$

$$0.0000352343 e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} \frac{\left(\frac{-1}{21}\right)^k \left(\frac{-1}{2}\right)_k}{k!} (1 + 20.0373 \pi)$$

$$\frac{e^{\pi \sqrt{22}} 7 \times 0.0824684 \left(1 + \frac{20 \pi}{0.998136}\right)}{4 \times 64^2} =$$

$$0.0000352343 \exp\left(\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right) (1 + 20.0373 \pi)$$

$$\left(\left(\left(\frac{1}{64^2}\left(\left(\frac{7}{4}e^{\pi\sqrt{22}}\right) \times 0.08246839796\left(1+20\times\frac{\pi}{0.9981360456}\right)\right)\right)\right)\right)+123+11$$

**Input interpretation:**

$$\frac{1}{64^2} \left( \frac{7}{4} e^{\pi\sqrt{22}} \times 0.08246839796 \left( 1 + 20 \times \frac{\pi}{0.9981360456} \right) \right) + 123 + 11$$

**Result:**

5787.182970...

5787.18297... result practically equal to the rest mass of bottom Xi baryon 5787.8

**Series representations:**

$$\frac{e^{\pi\sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right)}{4 \times 64^2} + 123 + 11 =$$

$$134 + e^{\pi\sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}} (0.0000352343 + 0.000706002\pi)$$

$$\frac{e^{\pi\sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right)}{4 \times 64^2} + 123 + 11 =$$

$$134 + e^{\pi\sqrt{21} \sum_{k=0}^{\infty} \frac{(-1)^k \binom{-1}{2k}}{k!}} (0.0000352343 + 0.000706002\pi)$$

$$\frac{e^{\pi\sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right)}{4 \times 64^2} + 123 + 11 =$$

$$134 + \exp\left( \frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}} \right) (0.0000352343 + 0.000706002\pi)$$

$$\left(\left(\left(\frac{29+2}{10^2}\right) \times \frac{1}{64^2} \left(\left(\frac{7}{4}e^{\pi\sqrt{22}}\right) \times 0.08246839796\left(1+20\times\frac{\pi}{0.9981360456}\right)\right)\right)\right) - 24$$

**Input interpretation:**

$$\frac{29+2}{10^2} \times \frac{1}{64^2} \left( \frac{7}{4} e^{\pi\sqrt{22}} \times 0.08246839796 \left( 1 + 20 \times \frac{\pi}{0.9981360456} \right) \right) - 24$$

**Result:**

1728.486721...

1728.486721...

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the  $j$ -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

**Series representations:**

$$\frac{\left( e^{\pi \sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right) \right) (29 + 2)}{(64^2 \times 4) 10^2} - 24 =$$

$$-24 + e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (0.0000109226 + 0.000218861 \pi)$$

$$\frac{\left( e^{\pi \sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right) \right) (29 + 2)}{(64^2 \times 4) 10^2} - 24 =$$

$$-24 + e^{\pi \sqrt{21}} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!} (0.0000109226 + 0.000218861 \pi)$$

$$\frac{\left( e^{\pi \sqrt{22}} 7 \times 0.0824684 \left( 1 + \frac{20\pi}{0.998136} \right) \right) (29 + 2)}{(64^2 \times 4) 10^2} - 24 =$$

$$-24 + \exp \left( \frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{2 \sqrt{\pi}} \right) (0.0000109226 + 0.000218861 \pi)$$

Now, we have that:

$AdS_3 \times S^7$  background. In addition, the zeroth-order dilaton equation gives

$$V'_0 = \frac{\beta}{2} \tilde{h}^2 e^{\beta \phi_0}, \quad (3.5)$$

which links the three-form flux, sized by  $\tilde{h}$ , to the derivative of the scalar potential. Notice that the allowed signs of  $V'_0$  and  $\beta$  must coincide, a condition that holds for the perturbative orientifold vacuum, where  $\beta = 1$ . The Einstein equations translate into

$$\frac{21}{R^2} - \frac{1}{R_{AdS}^2} = \frac{1}{4} e^{\beta \phi_0} \tilde{h}^2 + \frac{1}{2} V_0, \quad (3.6)$$

$$\frac{15}{R^2} - \frac{3}{R_{AdS}^2} = -\frac{1}{4} e^{\beta \phi_0} \tilde{h}^2 + \frac{1}{2} V_0, \quad (3.7)$$

and it is convenient to define the two variables

$$\sigma_3 = \frac{R_{AdS}^2}{2\beta} V'_0 = 1 + 3 \frac{R_{AdS}^2}{R^2}, \quad \tau_3 = R_{AdS}^2 V''_0, \quad (3.8)$$

which will often appear in the next section. Notice that  $\sigma_3 \geq 1$  and

$$R_{AdS}^2 V_0 = 12 \left( \sigma_3 - \frac{4}{3} \right), \quad (3.9)$$

so that the value  $\sigma_3 = \frac{4}{3}$  separates negative and positive values of  $V_0$  for these generalized  $AdS_3 \times S^7$  vacua, and for the (*projective*)*disk-level* orientifold potential

$$\sigma_3 = \frac{3}{2}, \quad \tau_3 = \frac{9}{2}. \quad (3.10)$$

From eq. (3.9), we have:

$$12(3/2-4/3)$$

$$12\left(\frac{3}{2} - \frac{4}{3}\right)$$

2

Thence  $V_0 = 2$

From eq. (3.6), we obtain:

$$\frac{21}{R^2} - \frac{1}{R_{AdS}^2} = \frac{1}{4} e^{\beta \phi_0} \tilde{h}^2 + \frac{1}{2} V_0$$

For  $R_{AdS}^2 = 1$ ;  $R^2 = 1$ , and  $e^{\pi\sqrt{22}} - 24 + 276e^{-\pi\sqrt{22}} - \dots$

we obtain:

$$(21-1)x = \frac{1}{4} * e^{-(\pi*\sqrt{22})} * 276^2 + 1$$

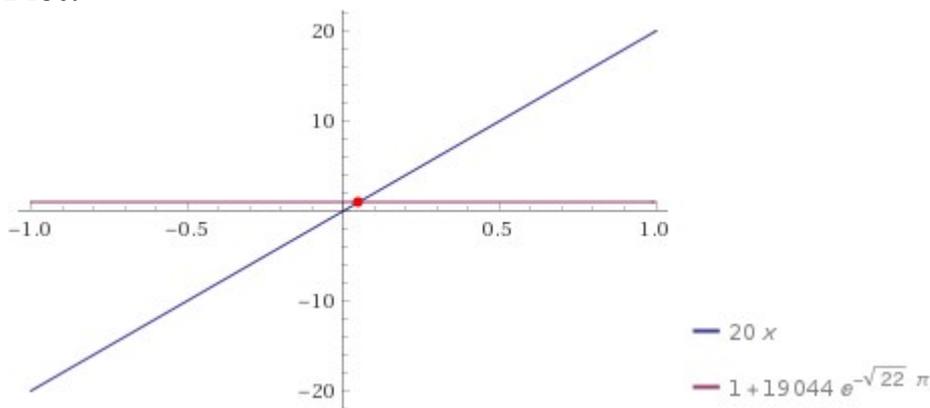
**Input:**

$$(21-1)x = \frac{1}{4} e^{-(\pi\sqrt{22})} \times 276^2 + 1$$

**Exact result:**

$$20x = 1 + 19044 e^{-\sqrt{22} \pi}$$

**Plot:**



**Alternate forms:**

$$20x - 19044 e^{-\sqrt{22} \pi} - 1 = 0$$

$$20x = e^{-\sqrt{22} \pi} (19044 + e^{\sqrt{22} \pi})$$

**Solution:**

$$x = \frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}$$

**Input:**

$$\frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}$$

**Decimal approximation:**

0.050379521011426820452806179207043538442700769978101013002...

0.050379521...

**Property:**

$\frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}$  is a transcendental number

**Alternate forms:**

$$\frac{1}{20} \left( 1 + 19\,044 e^{-\sqrt{22} \pi} \right)$$

$$\frac{1}{20} e^{-\sqrt{22} \pi} \left( 19\,044 + e^{\sqrt{22} \pi} \right)$$

**Series representations:**

$$\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761 = \frac{1}{20} + \frac{4761}{5} e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}$$

$$\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761 = \frac{1}{20} + \frac{4761}{5} \exp \left( -\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \binom{-1/2}{k}}{k!} \right)$$

$$\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761 = \frac{1}{20} + \frac{4761}{5} \exp \left( -\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}} \right)$$

$7 / \left( \left( \left( \frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi} \right) \right) \right) + 1 / \text{golden ratio}$

**Input:**

$$\frac{7}{\frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}} + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Decimal approximation:**

139.5633804205330885306347895826403715652757127044088743680...

139.56338042... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$\frac{7}{\frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}} + \frac{1}{\phi}$  is a transcendental number

**Alternate forms:**

$$\frac{1}{\phi} + \frac{140}{1 + 19044 e^{-\sqrt{22} \pi}}$$

$$\frac{1}{2} (\sqrt{5} - 1) + \frac{7}{\frac{1}{20} + \frac{4761}{5} e^{-\sqrt{22} \pi}}$$

$$\frac{140 \phi + 1 + 19044 e^{-\sqrt{22} \pi}}{(1 + 19044 e^{-\sqrt{22} \pi}) \phi}$$

**Series representations:**

$$\frac{7}{\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761} + \frac{1}{\phi} = \frac{7}{\frac{1}{20} + \frac{4761}{5} e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}} + \frac{1}{\phi}$$

$$\frac{7}{\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761} + \frac{1}{\phi} = \frac{7}{\frac{1}{20} + \frac{4761}{5} \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{(-\frac{1}{21})^k (-\frac{1}{2})_k}{k!}\right)} + \frac{1}{\phi}$$

$$\frac{7}{\frac{1}{20} + \frac{1}{5} e^{-\sqrt{22} \pi} 4761} + \frac{1}{\phi} = \frac{7}{\frac{1}{20} + \frac{4761}{5} \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{2 \sqrt{\pi}}\right)} + \frac{1}{\phi}$$

From eq. (3.7), we obtain:

$$(15-3)x = -1/4 * e^{-(\pi*\sqrt{22})} * 276^2 + 1$$

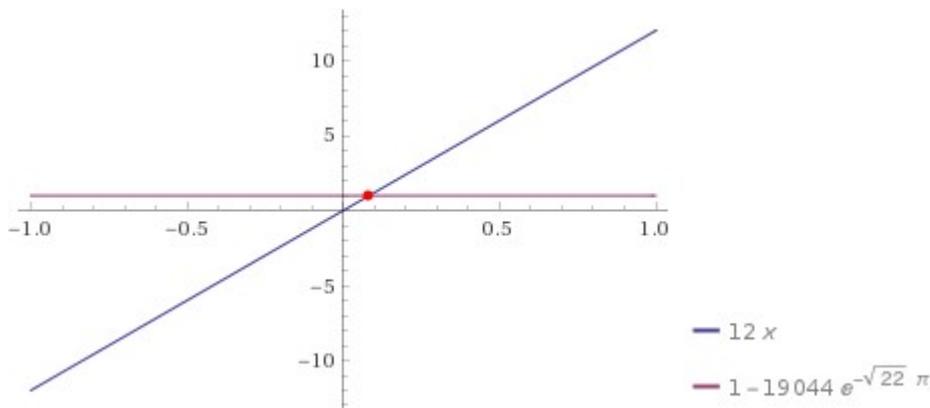
**Input:**

$$(15 - 3)x = -\frac{1}{4} e^{-(\pi \sqrt{22})} \times 276^2 + 1$$

**Exact result:**

$$12x = 1 - 19044 e^{-\sqrt{22} \pi}$$

**Plot:**



**Alternate forms:**

$$12(x + 1587 e^{-\sqrt{22} \pi}) = 1$$

$$12x + 19044 e^{-\sqrt{22} \pi} - 1 = 0$$

$$12x = e^{-\sqrt{22} \pi} (e^{\sqrt{22} \pi} - 19044)$$

**Solution:**

$$x = \frac{1}{12} - 1587 e^{-\sqrt{22} \pi}$$

$$1/12 - 1587 e^{(-\text{sqrt}(22) \pi)}$$

**Input:**

$$\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}$$

**Decimal approximation:**

0.082700798314288632578656367988260769262165383369831644995...

0.0827007983...

**Property:**

$\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}$  is a transcendental number

**Alternate forms:**

$$\frac{1}{12} (1 - 19044 e^{-\sqrt{22} \pi})$$

$$\frac{1}{12} e^{-\sqrt{22} \pi} (e^{\sqrt{22} \pi} - 19044)$$

**Series representations:**

$$\frac{1}{12} - 1587 e^{-\sqrt{22} \pi} = \frac{1}{12} - 1587 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}$$

$$\frac{1}{12} - 1587 e^{-\sqrt{22} \pi} = \frac{1}{12} - 1587 \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)$$

$$\frac{1}{12} - 1587 e^{-\sqrt{22} \pi} = \frac{1}{12} - 1587 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)$$

11/(((1/12 - 1587 e^(-sqrt(22) π))))+5+golden ratio

**Input:**

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} + 5 + \phi$$

$\phi$  is the golden ratio

**Decimal approximation:**

139.6276327376833100900013364247870846143606714913243368267...

139.6276327... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$5 + \frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} + \phi$  is a transcendental number

**Alternate forms:**

$$\phi + 5 - \frac{132}{19044 e^{-\sqrt{22} \pi} - 1}$$

$$\frac{1}{2} (275 + \sqrt{5}) + \frac{2513808}{e^{\sqrt{22} \pi} - 19044}$$

$$\frac{1}{2} (11 + \sqrt{5}) + \frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

**Series representations:**

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} + 5 + \phi = 5 + \frac{11}{\frac{1}{12} - 1587 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}} + \phi$$

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} + 5 + \phi = 5 + \frac{11}{\frac{1}{12} - 1587 \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)} + \phi$$

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} + 5 + \phi = 5 + \frac{11}{\frac{1}{12} - 1587 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)} + \phi$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

$11/(((1/12 - 1587 e^{(-\sqrt{22} \pi))})-7-1/\text{golden ratio})$

**Input:**

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Decimal approximation:**

125.3915647601835203935921627560558083789200531317128111024...

125.39156476... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Property:**

$-7 + \frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - \frac{1}{\phi}$  is a transcendental number

**Alternate forms:**

$$-\frac{1}{\phi} - 7 - \frac{132}{19044 e^{-\sqrt{22} \pi} - 1}$$

$$-7 - \frac{2}{1 + \sqrt{5}} + \frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

$$\frac{1}{2}(-13 - \sqrt{5}) + \frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

**Series representations:**

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} = -7 + \frac{11}{\frac{1}{12} - 1587 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}} - \frac{1}{\phi}$$

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} = -7 + \frac{11}{\frac{1}{12} - 1587 \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)} - \frac{1}{\phi}$$

$$\frac{11}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} = -7 + \frac{11}{\frac{1}{12} - 1587 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)} - \frac{1}{\phi}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\operatorname{Res}_{z=z_0} f$  is a complex residue

$$64/(((1/12 - 1587 e^{(-\sqrt{22}) \pi}))) - 7 - 1/\text{golden ratio} + 16$$

**Input:**

$$\frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} + 16$$

$\phi$  is the golden ratio

**Exact result:**

$$-\frac{1}{\phi} + 9 + \frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

**Decimal approximation:**

782.2559950959536120131583198735409596809145260872113947502...

782.25599509... result practically equal to the rest mass of Omega meson 782.65

**Property:**

$$9 + \frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - \frac{1}{\phi} \text{ is a transcendental number}$$

**Alternate forms:**

$$-\frac{1}{\phi} + 9 - \frac{768}{19044 e^{-\sqrt{22} \pi} - 1}$$

$$9 - \frac{2}{1 + \sqrt{5}} + \frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

$$\frac{1}{2} (19 - \sqrt{5}) + \frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

**Series representations:**

$$\frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} + 16 = 9 + \frac{64}{\frac{1}{12} - 1587 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}} - \frac{1}{\phi}$$

$$\frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} + 16 = 9 + \frac{64}{\frac{1}{12} - 1587 \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)} - \frac{1}{\phi}$$

$$\frac{64}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 7 - \frac{1}{\phi} + 16 =$$

$$9 + \frac{64}{\frac{1}{12} - 1587 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2\sqrt{\pi}}\right)} - \frac{1}{\phi}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\operatorname{Res}_{z=z_0} f$  is a complex residue

144/(((1/12 - 1587 e<sup>^(-sqrt(22) π))</sup>))-11-golden ratio

**Input:**

$$\frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 11 - \phi$$

$\phi$  is the golden ratio

**Decimal approximation:**

1728.598531451832995589861953258424206929208070170982841765...

1728.5985314...

This result is very near to the mass of candidate glueball  $f_0(1710)$  meson. Furthermore, 1728 occurs in the algebraic formula for the  $j$ -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

**Property:**

$$-11 + \frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - \phi \text{ is a transcendental number}$$

**Alternate forms:**

$$-\phi - 11 - \frac{1728}{19044 e^{-\sqrt{22} \pi} - 1}$$

$$\frac{1}{2} (3433 - \sqrt{5}) + \frac{32908032}{e^{\sqrt{22} \pi} - 19044}$$

$$\frac{1}{2} (-23 - \sqrt{5}) + \frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}}$$

**Series representations:**

$$\frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 11 - \phi = -11 + \frac{144}{\frac{1}{12} - 1587 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}} - \phi$$

$$\frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 11 - \phi = -11 + \frac{144}{\frac{1}{12} - 1587 \exp\left(-\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!}\right)} - \phi$$

$$\frac{144}{\frac{1}{12} - 1587 e^{-\sqrt{22} \pi}} - 11 - \phi = -11 + \frac{144}{\frac{1}{12} - 1587 \exp\left(-\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}\right)} - \phi$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

From (3.5), we obtain:

$$\frac{1}{2} * 276^2 * e^{-(\text{Pi} * \text{sqrt}22)}$$

**Input:**

$$\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}$$

**Exact result:**

$$38\,088 e^{-\sqrt{22} \pi}$$

**Decimal approximation:**

0.015180840457072818112247168281741537708030799124040520108...

0.01518084...

**Property:**

$38\,088 e^{-\sqrt{22} \pi}$  is a transcendental number

**Series representations:**

$$\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})} = 38\,088 e^{-\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}$$

$$\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})} = 38\,088 \exp \left( -\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{21}\right)^k \left(-\frac{1}{2}\right)_k}{k!} \right)$$

$$\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})} = 38\,088 \exp \left( -\frac{\pi \sum_{j=0}^{\infty} \operatorname{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}} \right)$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\operatorname{Res}_f$  is a complex residue  
 $z \rightarrow 0$

$$2 / (1/2 * 276^2 * e^{-(\pi * \sqrt{22})}) + 8$$

**Input:**

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} + 8$$

**Exact result:**

$$8 + \frac{e^{\sqrt{22} \pi}}{19044}$$

**Decimal approximation:**

139.7450114606923160662428688364675048559341910768854461105...

139.74501146... result practically equal to the rest mass of Pion meson 139.57 MeV

**Property:**

$8 + \frac{e^{\sqrt{22} \pi}}{19044}$  is a transcendental number

**Alternate form:**

$$\frac{152\,352 + e^{\sqrt{22} \pi}}{19\,044}$$

**Series representations:**

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} + 8 = 8 + \frac{e^{\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}}{19\,044}$$

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} + 8 = 8 + \frac{e^{\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{(-\frac{1}{21})^k (-\frac{1}{2})_k}{k!}}}{19\,044}$$

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} + 8 = 8 + \frac{\exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{2 \sqrt{\pi}}\right)}{19\,044}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

$$2/(1/2 * 276^2 * e^{-(\pi*\sqrt{22})}) - 7 + 1/\text{golden ratio}$$

**Input:**

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} - 7 + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Exact result:**

$$\frac{1}{\phi} - 7 + \frac{e^{\sqrt{22} \pi}}{19044}$$

**Decimal approximation:**

125.3630454494422109144474556708331429736545002566912089727...

125.36304544... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Property:**

$$-7 + \frac{e^{\sqrt{22} \pi}}{19044} + \frac{1}{\phi} \text{ is a transcendental number}$$

**Alternate forms:**

$$\frac{1}{2} (\sqrt{5} - 15) + \frac{e^{\sqrt{22} \pi}}{19044}$$

$$\frac{19044 (1 - 7\phi) + e^{\sqrt{22} \pi} \phi}{19044 \phi}$$

$$-7 + \frac{2}{1 + \sqrt{5}} + \frac{e^{\sqrt{22} \pi}}{19044}$$

**Series representations:**

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} - 7 + \frac{1}{\phi} = -7 + \frac{e^{\pi \sqrt{21} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k}}}{19044} + \frac{1}{\phi}$$

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} - 7 + \frac{1}{\phi} = -7 + \frac{e^{\pi \sqrt{21} \sum_{k=0}^{\infty} \frac{(-\frac{1}{21})^k (-\frac{1}{2})^k}{k!}}}{19044} + \frac{1}{\phi}$$

$$\frac{2}{\frac{1}{2} \times 276^2 e^{-(\pi \sqrt{22})}} - 7 + \frac{1}{\phi} = -7 + \frac{\exp\left(\frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{2 \sqrt{\pi}}\right)}{19044} + \frac{1}{\phi}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

Now, we have that:

$$\sigma_3 = \frac{3}{2}, \quad \tau_3 = \frac{9}{2} \cdot (\ell \geq 2)$$

The eigenvalues of the mass matrix are thus

$$(\sigma_3 - 1) \frac{\ell(\ell + 6) + 5}{3} \pm 2 \sqrt{1 + \sigma_3(\sigma_3 - 1) \frac{\ell(\ell + 6) + 5}{3}}. \quad (3.28)$$

$$(3/2-1)*1/3((2(2+6)+5))+2\text{sqrt}((((1+3/2(3/2-1)*1/3((2(2+6)+5))))))$$

**Input:**

$$\left(\frac{3}{2} - 1\right) \times \frac{1}{3} (2(2+6)+5) + 2 \sqrt{1 + \frac{3}{2} \left(\frac{3}{2} - 1\right) \times \frac{1}{3} (2(2+6)+5)}$$

**Exact result:**

$$\frac{17}{2}$$

**Decimal form:**

$$8.5$$

$$8.5$$

And:

$$(3/2-1)*1/3((2(2+6)+5))-2\text{sqrt}((((1+3/2(3/2-1)*1/3((2(2+6)+5))))))$$

**Input:**

$$\left(\frac{3}{2} - 1\right) \times \frac{1}{3} (2(2+6)+5) - 2 \sqrt{1 + \frac{3}{2} \left(\frac{3}{2} - 1\right) \times \frac{1}{3} (2(2+6)+5)}$$

**Exact result:**

$$-\frac{3}{2}$$

**Decimal form:**

$$-1.5$$

$$-1.5$$

For  $\ell = 11$ , we obtain:

$$(3/2-1)*1/3((11(11+6)+5))+2\text{sqrt}((((1+3/2(3/2-1)*1/3((11(11+6)+5))))))$$

**Input:**

$$\left(\frac{3}{2} - 1\right) \times \frac{1}{3} (11(11+6)+5) + 2 \sqrt{1 + \frac{3}{2} \left(\frac{3}{2} - 1\right) \times \frac{1}{3} (11(11+6)+5)}$$

**Exact result:**

$$46$$

$$46$$

From which:

$$3*((((3/2-1)*1/3((11(11+6)+5))+2\text{sqrt}((((1+3/2(3/2-1)*1/3((11(11+6)+5))))))))+golden\ ratio$$

**Input:**

$$3 \left( \left(\frac{3}{2} - 1\right) \times \frac{1}{3} (11(11+6)+5) + 2 \sqrt{1 + \frac{3}{2} \left(\frac{3}{2} - 1\right) \times \frac{1}{3} (11(11+6)+5)} \right) + \phi$$

$\phi$  is the golden ratio

**Result:**

$$\phi + 138$$

**Decimal approximation:**

139.6180339887498948482045868343656381177203091798057628621...

139.6180339887... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternate forms:**

$$\frac{1}{2}(277 + \sqrt{5})$$

$$\frac{277}{2} + \frac{\sqrt{5}}{2}$$

$$138 + \frac{1}{2}(1 + \sqrt{5})$$

**Series representations:**

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left(\frac{3}{2} - 1\right) 3(11(11+6)+5)}{2 \times 3}} \right) + \phi =$$

$$96 + \phi + 6 \sqrt{48} \sum_{k=0}^{\infty} 48^{-k} \binom{\frac{1}{2}}{k}$$

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left(\frac{3}{2} - 1\right) 3(11(11+6)+5)}{2 \times 3}} \right) + \phi =$$

$$96 + \phi + 6 \sqrt{48} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{48}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left(\frac{3}{2} - 1\right) 3(11(11+6)+5)}{2 \times 3}} \right) + \phi =$$

$$96 + \phi + \frac{3 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 48^{-s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=0} f$  is a complex residue

$$3 * (((((3/2-1) * 1/3((11(11+6)+5)) + 2\sqrt{((1+3/2(3/2-1) * 1/3((11(11+6)+5))))})) - 13 + 1/\text{golden ratio}$$

**Input:**

$$3 \left( \left( \frac{3}{2} - 1 \right) \times \frac{1}{3} (11(11+6)+5) + 2 \sqrt{1 + \frac{3}{2} \left( \frac{3}{2} - 1 \right) \times \frac{1}{3} (11(11+6)+5)} \right) - 13 + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$\frac{1}{\phi} + 125$$

**Decimal approximation:**

125.6180339887498948482045868343656381177203091798057628621...

125.6180339887... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Alternate forms:**

$$\frac{1}{2} (249 + \sqrt{5})$$

$$\frac{125\phi + 1}{\phi}$$

$$\frac{\sqrt{5}}{2} + \frac{249}{2}$$

**Series representations:**

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left( \frac{3}{2} - 1 \right) 3 (11(11+6)+5)}{2 \times 3}} \right) - 13 + \frac{1}{\phi} =$$

$$83 + \frac{1}{\phi} + 6 \sqrt{48} \sum_{k=0}^{\infty} 48^{-k} \binom{\frac{1}{2}}{k}$$

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left( \frac{3}{2} - 1 \right) 3 (11(11+6)+5)}{2 \times 3}} \right) - 13 + \frac{1}{\phi} =$$

$$83 + \frac{1}{\phi} + 6 \sqrt{48} \sum_{k=0}^{\infty} \frac{\left( -\frac{1}{48} \right)^k \left( -\frac{1}{2} \right)_k}{k!}$$

$$3 \left( \frac{1}{3} \left( \frac{3}{2} - 1 \right) (11(11+6)+5) + 2 \sqrt{1 + \frac{\left( \frac{3}{2} - 1 \right) 3 (11(11+6)+5)}{2 \times 3}} \right) - 13 + \frac{1}{\phi} =$$

$$83 + \frac{1}{\phi} + \frac{3 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 48^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

Now, we have that:

which changes sign at  $\sigma_7 = 12$ , and finally for the *torus-level* heterotic potential

$$\sigma_7 = 15, \quad \tau_7 = 75. \quad (4.9)$$

$$(\ell + 1)^2 (\sigma_7 - 3) \pm 2 \sqrt{\sigma_7 (\sigma_7 - 3) (\ell + 1)^2 + 9}. \quad (4.18)$$

$$(3+1)^2(15-3)+2\text{sqrt}((((15(15-3)(3+1)^2+9))))$$

**Input:**

$$(3+1)^2(15-3)+2\sqrt{15(15-3)(3+1)^2+9}$$

**Result:**

$$192+6\sqrt{321}$$

**Decimal approximation:**

299.4988372030135031078778906039125523416602879422205287241...  
 299.498837203...

**Alternate form:**

$$6(32 + \sqrt{321})$$

**Minimal polynomial:**

$$x^2 - 384x + 25308$$

$1/2(((3+1)^2(15-3)+2\sqrt{15(15-3)(3+1)^2+9})))-11+1/\text{golden ratio}$

**Input:**

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2+9} \right) - 11 + \frac{1}{\phi}$$

$\phi$  is the golden ratio

**Result:**

$$\frac{1}{\phi} - 11 + \frac{1}{2} (192 + 6\sqrt{321})$$

**Decimal approximation:**

139.3674525902566464021435321363219142885504531509160272242...

139.36745259... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternate forms:**

$$\frac{1}{2} (169 + \sqrt{5} + 6\sqrt{321})$$

$$\frac{1}{\phi} + 85 + 3\sqrt{321}$$

$$\frac{(85 + 3\sqrt{321})\phi + 1}{\phi}$$

**Minimal polynomial:**

$$x^4 - 338x^3 + 37061x^2 - 1436500x + 18048055$$

**Series representations:**

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 11 + \frac{1}{\phi} = 85 + \frac{1}{\phi} + \sqrt{2888} \sum_{k=0}^{\infty} 2888^{-k} \binom{\frac{1}{2}}{k}$$

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 11 + \frac{1}{\phi} = 85 + \frac{1}{\phi} + \sqrt{2888} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2888}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 11 + \frac{1}{\phi} = 85 + \frac{1}{\phi} + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2888^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

$\text{Res}_{z=z_0} f$  is a complex residue

$$1/2((((3+1)^2(15-3)+2\text{sqrt}((((15(15-3)(3+1)^2+9)))))))-29+\text{Pi}+\text{golden ratio}$$

**Input:**

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 29 + \pi + \phi$$

$\phi$  is the golden ratio

**Result:**

$$\phi - 29 + \frac{1}{2} \left( 192 + 6 \sqrt{321} \right) + \pi$$

**Decimal approximation:**

125.5090452438464396406061755196014171727476225502911330451...

125.5090452... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Property:**

$-29 + \frac{1}{2} (192 + 6 \sqrt{321}) + \phi + \pi$  is a transcendental number

**Alternate forms:**

$$\frac{1}{2} (135 + \sqrt{5} + 6 \sqrt{321} + 2 \pi)$$

$$\phi + 67 + 3 \sqrt{321} + \pi$$

$$\frac{135}{2} + \frac{\sqrt{5}}{2} + 3 \sqrt{321} + \pi$$

**Series representations:**

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 29 + \pi + \phi = 67 + \phi + \pi + \sqrt{2888} \sum_{k=0}^{\infty} 2888^{-k} \binom{\frac{1}{2}}{k}$$

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 29 + \pi + \phi = 67 + \phi + \pi + \sqrt{2888} \sum_{k=0}^{\infty} \frac{\left(-\frac{1}{2888}\right)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$\frac{1}{2} \left( (3+1)^2 (15-3) + 2 \sqrt{15(15-3)(3+1)^2 + 9} \right) - 29 + \pi + \phi = 67 + \phi + \pi + \frac{\sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 2888^{-s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{2 \sqrt{\pi}}$$

$\binom{n}{m}$  is the binomial coefficient

$n!$  is the factorial function

$(\alpha)_n$  is the Pochhammer symbol (rising factorial)

$\Gamma(x)$  is the gamma function

Now, we have that:

with  $\alpha > 0$  for  $d > 10$  and  $\alpha < 0$  for  $d < 10$ .

$$\varphi = -\frac{(d-2)^2}{8\phi'} [A' + (d-3)A\Omega'] \quad (6.11)$$

$$\begin{aligned} A'' + A' \left[ 3(d-2)\Omega' - \frac{(d-2)}{4\phi'} e^{2\Omega} V_\phi \right] \\ + A \left[ m^2 - \frac{2(d-3)}{(d-2)} e^{2\Omega} V - \frac{(d-2)(d-3)}{4} e^{2\Omega} \Omega' \frac{V_\phi}{\phi'} \right] = 0, \end{aligned} \quad (6.10)$$

For  $\phi'$  equal to the following Rogers-Ramanujan continued fraction, with minus sign:

$$\frac{1}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \dots}}}}} = e^{2\pi/5} \left( \sqrt{\Phi} \sqrt{5} - \Phi \right) = 0,9981360456 \dots$$

$V_\phi = 138$ ,  $V = 0.57142857$ ,  $\Omega' = \pi$  and  $d = 7$ , we obtain:

$$-(7-2)^2 / (8 * -0.9981360456) * (1+(7-3)*\pi)$$

**Input interpretation:**

$$-\frac{(7-2)^2}{8 \times (-0.9981360456)} (1 + (7-3)\pi)$$

**Result:**

42.47407791...

42.47407791...

**Alternative representations:**

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = \frac{-(1 + 720^\circ)5^2}{-7.98509}$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = \frac{-(1 - 4i \log(-1))5^2}{-7.98509}$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = \frac{-(1 + 4 \cos^{-1}(-1))5^2}{-7.98509}$$

**Series representations:**

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = 3.13084 + 50.0934 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = -21.9159 + 25.0467 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = 3.13084 + 12.5233 \sum_{k=0}^{\infty} \frac{2^{-k}(-6 + 50k)}{\binom{3k}{k}}$$

**Integral representations:**

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = 3.13084 + 25.0467 \int_0^{\infty} \frac{1}{1 + t^2} dt$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = 3.13084 + 50.0934 \int_0^1 \sqrt{1 - t^2} dt$$

$$\frac{(1 + (7 - 3)\pi)(-(7 - 2)^2)}{8(-0.998136)} = 3.13084 + 25.0467 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

$3 * (((-(7-2)^2 / (8 * -0.9981360456)) * (1 + (7-3) * \text{Pi})))) - \text{golden ratio}$

**Input interpretation:**

$$3 \left( -\frac{(7-2)^2}{8 \times (-0.9981360456)} (1 + (7-3)\pi) \right) - \phi$$

$\phi$  is the golden ratio

**Result:**

125.8041998...

125.8041998... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Alternative representations:**

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 2 \cos(216^\circ) - \frac{3(1+4\pi)5^2}{7.98509}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 2 \cos(216^\circ) - \frac{3(1+720^\circ)5^2}{7.98509}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = -2 \cos\left(\frac{\pi}{5}\right) - \frac{3(1+4\pi)5^2}{7.98509}$$

**Series representations:**

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 9.39251 - \phi + 150.28 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = -65.7476 - \phi + 75.1401 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 9.39251 - \phi + 37.57 \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}$$

**Integral representations:**

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 9.39251 - \phi + 75.1401 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 9.39251 - \phi + 150.28 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} - \phi = 9.39251 - \phi + 75.1401 \int_0^\infty \frac{\sin(t)}{t} dt$$

$3 * (((-(7-2)^2 / (8 * -0.9981360456)) * (1 + (7-3) * \text{Pi})))) + 11 + 3 - \text{golden ratio}$

### Input interpretation:

$$3 \left( \frac{(7-2)^2}{8 \times (-0.9981360456)} (1 + (7-3)\pi) \right) + 11 + 3 - \phi$$

$\phi$  is the golden ratio

### Result:

139.8041998...

139.8041998... result practically equal to the rest mass of Pion meson 139.57 MeV

### Alternative representations:

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 14 + 2 \cos(216^\circ) - \frac{3(1+4\pi)5^2}{7.98509}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 14 + 2 \cos(216^\circ) - \frac{3(1+720^\circ)5^2}{7.98509}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 14 - 2 \cos\left(\frac{\pi}{5}\right) - \frac{3(1+4\pi)5^2}{7.98509}$$

### Series representations:

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 23.3925 - \phi + 150.28 \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = -51.7476 - \phi + 75.1401 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 23.3925 - \phi + 37.57 \sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}$$

**Integral representations:**

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 23.3925 - \phi + 75.1401 \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 23.3925 - \phi + 150.28 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{3(-7-2)^2(1+(7-3)\pi)}{8(-0.998136)} + 11 + 3 - \phi = 23.3925 - \phi + 75.1401 \int_0^{\infty} \frac{\sin(t)}{t} dt$$

With regard

$$\begin{aligned} A'' + A' \left[ 3(d-2)\Omega' - \frac{(d-2)}{4\phi'} e^{2\Omega} V_{\phi} \right] \\ + A \left[ m^2 - \frac{2(d-3)}{(d-2)} e^{2\Omega} V - \frac{(d-2)(d-3)}{4} e^{2\Omega} \Omega' \frac{V_{\phi}}{\phi'} \right] = 0, \end{aligned} \quad (6.10)$$

and

$$m^2 > \frac{(d-2)^2 a^2}{4}.$$

For a = 2,  $m^2 > 25$ ;  $m^2 = 34$

$V_{\phi} = 138$ ,  $V = 0.57142857$ ,  $\Omega' = \pi$ ,  $d = 7$ ,

$$-2((((15\pi - 5/(4 \times 0.9981360456) e^{\pi\sqrt{22}} \times 138))) + (((((34 - 8/5 e^{\pi\sqrt{22}}) * 0.57142857 - 5 * e^{\pi\sqrt{22}} * \pi * 138/0.9981360456))))))$$

**Input interpretation:**

$$-2 \left( \left( 15\pi - \frac{5}{4 \times 0.9981360456} e^{\pi\sqrt{22}} \times 138 \right) + \left( 34 + \frac{8}{5} e^{\pi\sqrt{22}} \times (-0.57142857) - 5 e^{\pi\sqrt{22}} \pi \times \frac{138}{0.9981360456} \right) \right)$$

**Result:**

$$1.176941030... \times 10^{10}$$

$$1.176941030... * 10^{10}$$

**Series representations:**

$$-2 \left( \left( 15\pi - \frac{5 e^{\pi\sqrt{22}}}{4 \times 0.998136} 138 \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) = -68 - 30\pi + e^{\pi\sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (347.473 + 1382.58\pi)$$

$$-2 \left( \left( 15\pi - \frac{5 e^{\pi\sqrt{22}}}{4 \times 0.998136} 138 \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) = -68 - 30\pi + e^{\pi\sqrt{21}} \sum_{k=0}^{\infty} \frac{\binom{-1/2}{k} \binom{-1}{k}}{k!} (347.473 + 1382.58\pi)$$

$$-2 \left( \left( 15\pi - \frac{5 e^{\pi\sqrt{22}}}{4 \times 0.998136} 138 \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) = -68 - 30\pi + \exp \left( \frac{\pi \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} 21^{-s} \Gamma(-\frac{1}{2}-s) \Gamma(s)}{2\sqrt{\pi}} \right) (347.473 + 1382.58\pi)$$

$$2\pi \ln[(-2((((15\pi - 5/(4 \times 0.9981360456) e^{\pi\sqrt{22}} \times 138))) + (((((34 - 8/5 e^{\pi\sqrt{22}}) * 0.57142857 - 5 * e^{\pi\sqrt{22}} * \pi * 138/0.9981360456)))))))] - 7 + 1/\text{golden ratio}$$

**Input interpretation:**

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5}{4 \times 0.9981360456} e^{\pi\sqrt{22}} \times 138 \right) + \left( 34 + \frac{8}{5} e^{\pi\sqrt{22}} \times (-0.57142857) - 5 e^{\pi\sqrt{22}} \pi \times \frac{138}{0.9981360456} \right) \right) \right) - 7 + \frac{1}{\phi}$$

$\log(x)$  is the natural logarithm

$\phi$  is the golden ratio

**Result:**

139.31737078...

139.31737078... result practically equal to the rest mass of Pion meson 139.57 MeV

**Alternative representations:**

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} =$$

$$-7 + 2\pi \log_e \left( -2 \left( 34 + 15\pi - \frac{690\pi e^{\pi\sqrt{22}}}{0.998136} - \frac{690 e^{\pi\sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi\sqrt{22}} \right) \right) + \frac{1}{\phi}$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} = -7 + 2\pi \log(a)$$

$$\log_a \left( -2 \left( 34 + 15\pi - \frac{690\pi e^{\pi\sqrt{22}}}{0.998136} - \frac{690 e^{\pi\sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi\sqrt{22}} \right) \right) + \frac{1}{\phi}$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} =$$

$$-7 - 2\pi \operatorname{Li}_1 \left( 1 + 2 \left( 34 + 15\pi - \frac{690\pi e^{\pi\sqrt{22}}}{0.998136} - \frac{690 e^{\pi\sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi\sqrt{22}} \right) \right) + \frac{1}{\phi}$$

**Series representations:**

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} = -7 + \frac{1}{\phi} + 2\pi \log \left( -68 - 30\pi + e^{\pi\sqrt{21}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (347.473 + 1382.58\pi) \right)$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}}}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} \cdot 0.571429 - \frac{(138 \times 5)e^{\pi\sqrt{22}}}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} = -7 + \frac{1}{\phi} + 2\pi \log \left( -69 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) \right) -$$

$$2\pi \sum_{k=1}^{\infty} \frac{(-1)^k \left( -69 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) \right)^{-k}}{k}$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}}}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} \cdot 0.571429 - \frac{(138 \times 5)e^{\pi\sqrt{22}}}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} =$$

$$-7 + \frac{1}{\phi} + 4i\pi^2 \left[ \frac{\arg \left( -68 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) - x \right)}{2\pi} \right] + 2\pi \log(x) -$$

$$2\pi \sum_{k=1}^{\infty} \frac{(-1)^k \left( -68 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) - x \right)^k x^{-k}}{k} \quad \text{for } x < 0$$

### Integral representations:

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}}}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} \cdot 0.571429 - \frac{(138 \times 5)e^{\pi\sqrt{22}}}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} = -7 + \frac{1}{\phi} + 2\pi \int_1^{-68-30\pi+e^{\pi\sqrt{22}}(347.473+1382.58\pi)} \frac{1}{t} dt$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}}}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} \cdot 0.571429 - \frac{(138 \times 5)e^{\pi\sqrt{22}}}{0.998136} \right) \right) \right) -$$

$$7 + \frac{1}{\phi} =$$

$$-7 + \frac{1}{\phi} + \frac{1}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\left( -69 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) \right)^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds$$

for  $-1 < \gamma < 0$

$$2\pi \ln\left[(-2\left(\left(\left(\left(15\pi - \frac{5}{4 \times 0.9981360456} e^{\pi \sqrt{22}} \times 138\right)\right) + \left(\left(\left(\left(34 - \frac{8}{5} e^{\pi \sqrt{22}} \times (-0.57142857) - 5 e^{\pi \sqrt{22}} \pi \times \frac{138}{0.9981360456}\right)\right)\right)\right)\right)\right)] - 21 + \frac{1}{\phi}$$

**Input interpretation:**

$$2\pi \log\left(-2\left(\left(15\pi - \frac{5}{4 \times 0.9981360456} e^{\pi \sqrt{22}} \times 138\right) + \left(34 + \frac{8}{5} e^{\pi \sqrt{22}} \times (-0.57142857) - 5 e^{\pi \sqrt{22}} \pi \times \frac{138}{0.9981360456}\right)\right)\right) - 21 + \frac{1}{\phi}$$

$\log(x)$  is the natural logarithm

$\phi$  is the golden ratio

**Result:**

125.31737078...

125.31737078... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for  $T = 0$  and to the Higgs boson mass 125.18 GeV

**Alternative representations:**

$$2\pi \log\left(-2\left(\left(15\pi - \frac{5 e^{\pi \sqrt{22}} 138}{4 \times 0.998136}\right) + \left(34 - \frac{8}{5} e^{\pi \sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi \sqrt{22}} \pi}{0.998136}\right)\right)\right) - 21 + \frac{1}{\phi} = -21 + 2\pi \log_e\left(-2\left(34 + 15\pi - \frac{690 \pi e^{\pi \sqrt{22}}}{0.998136} - \frac{690 e^{\pi \sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi \sqrt{22}}\right)\right) + \frac{1}{\phi}$$

$$2\pi \log\left(-2\left(\left(15\pi - \frac{5 e^{\pi \sqrt{22}} 138}{4 \times 0.998136}\right) + \left(34 - \frac{8}{5} e^{\pi \sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi \sqrt{22}} \pi}{0.998136}\right)\right)\right) - 21 + \frac{1}{\phi} = -21 + 2\pi \log(a) \log_a\left(-2\left(34 + 15\pi - \frac{690 \pi e^{\pi \sqrt{22}}}{0.998136} - \frac{690 e^{\pi \sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi \sqrt{22}}\right)\right) + \frac{1}{\phi}$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} =$$

$$-21 - 2\pi \operatorname{Li}_1 \left( 1 + 2 \left( 34 + 15\pi - \frac{690\pi e^{\pi\sqrt{22}}}{0.998136} - \frac{690 e^{\pi\sqrt{22}}}{3.99254} - \frac{1}{5} \times 4.57143 e^{\pi\sqrt{22}} \right) \right) + \frac{1}{\phi}$$

### Series representations:

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} = -21 + \frac{1}{\phi} + 2\pi \log \left( -68 - 30\pi + e^{\pi\sqrt{22}} \sum_{k=0}^{\infty} 21^{-k} \binom{1/2}{k} (347.473 + 1382.58\pi) \right)$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} = -21 + \frac{1}{\phi} + 2\pi \log \left( -69 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) \right) -$$

$$2\pi \sum_{k=1}^{\infty} \frac{(-1)^k \left( -69 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) \right)^{-k}}{k}$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} =$$

$$-21 + \frac{1}{\phi} + 4i\pi^2 \left[ \frac{\arg \left( -68 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) - x \right)}{2\pi} \right] + 2\pi \log(x) -$$

$$2\pi \sum_{k=1}^{\infty} \frac{(-1)^k \left( -68 - 30\pi + e^{\pi\sqrt{22}} (347.473 + 1382.58\pi) - x \right)^k x^{-k}}{k} \quad \text{for } x < 0$$

### Integral representations:

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}} 138}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5) e^{\pi\sqrt{22}} \pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} = -21 + \frac{1}{\phi} + 2\pi \int_1^{-68-30\pi+e^{\pi\sqrt{22}}(347.473+1382.58\pi)} \frac{1}{t} dt$$

$$2\pi \log \left( -2 \left( \left( 15\pi - \frac{5e^{\pi\sqrt{22}}}{4 \times 0.998136} \right) + \left( 34 - \frac{8}{5} e^{\pi\sqrt{22}} 0.571429 - \frac{(138 \times 5)e^{\pi\sqrt{22}}\pi}{0.998136} \right) \right) \right) -$$

$$21 + \frac{1}{\phi} = -21 + \frac{1}{\phi} +$$

$$\frac{1}{i} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{(-69 - 30\pi + e^{\pi\sqrt{22}}(347.473 + 1382.58\pi))^{-s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds$$

for  $-1 < \gamma < 0$

Now, we have that:

$$h_{ij} = A_{ij} + B_{ij} \log \left[ \tanh \left( \sqrt{\alpha_{O,H}} t \sqrt{\frac{d-1}{2(d-2)}} \sqrt{1 - \left( \frac{\tilde{\gamma}}{\gamma^{(c)}} \right)^2} \right) \right], \quad (8.20)$$

with  $\alpha > 0$  for  $d > 10$  and  $\alpha < 0$  for  $d < 10$ .

$$\frac{\gamma_d}{\gamma^{(c)}} = \frac{1}{2}$$

$$A = 2, \quad B = 3, \quad \alpha = 5, \quad d = 11$$

$$2+3 \ln (\tanh(((\text{sqrt}5*\text{sqrt}(10/18))*\text{sqrt}(1-1/4))))$$

**Input:**

$$2+3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right)$$

$\tanh(x)$  is the hyperbolic tangent function

$\log(x)$  is the natural logarithm

**Exact result:**

$$2+3 \log \left( \tanh \left( \frac{5}{2\sqrt{3}} \right) \right)$$

**Decimal approximation:**

1.665110346842890765945420649301523907615803359459272966995...

1.6651103468...

**Alternate forms:**

$$2 + 3 \log \left( \frac{\sinh\left(\frac{5}{2\sqrt{3}}\right)}{\cosh\left(\frac{5}{2\sqrt{3}}\right)} \right)$$

$$2 + 3 \log \left( e^{5/\sqrt{3}} - 1 \right) - 3 \log \left( 1 + e^{5/\sqrt{3}} \right)$$

$$2 + 3 \log \left( \frac{e^{5/(2\sqrt{3})} - e^{-5/(2\sqrt{3})}}{e^{-5/(2\sqrt{3})} + e^{5/(2\sqrt{3})}} \right)$$

**Alternative representations:**

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 + 3 \log_e \left( \tanh \left( \sqrt{5} \sqrt{1 - \frac{1}{4}} \sqrt{\frac{10}{18}} \right) \right)$$

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 + 3 \log(a) \log_a \left( \tanh \left( \sqrt{5} \sqrt{1 - \frac{1}{4}} \sqrt{\frac{10}{18}} \right) \right)$$

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 + 3 \log \left( i \cot \left( \frac{\pi}{2} + i \sqrt{5} \sqrt{1 - \frac{1}{4}} \sqrt{\frac{10}{18}} \right) \right)$$

**Series representation:**

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 - 3 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -1 + \tanh \left( \frac{5}{2\sqrt{3}} \right) \right)^k}{k}$$

**Integral representations:**

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 + 3 \int_1^{\tanh\left(\frac{5}{2\sqrt{3}}\right)} \frac{1}{t} dt$$

$$2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) = 2 + 3 \log \left( \int_0^{\frac{5}{2\sqrt{3}}} \operatorname{sech}^2(t) dt \right)$$



$$\left(2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) \right) - \frac{47}{10^3} =$$

$$2 + 3 \log \left( i \cot \left( \frac{\pi}{2} + i \sqrt{5} \sqrt{1 - \frac{1}{4}} \sqrt{\frac{10}{18}} \right) \right) - \frac{47}{10^3}$$

**Series representation:**

$$\left(2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) \right) - \frac{47}{10^3} = \frac{1953}{1000} - 3 \sum_{k=1}^{\infty} \frac{(-1)^k \left( -1 + \tanh \left( \frac{5}{2\sqrt{3}} \right) \right)^k}{k}$$

**Integral representations:**

$$\left(2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) \right) - \frac{47}{10^3} = \frac{1953}{1000} + 3 \int_1^{\tanh \left( \frac{5}{2\sqrt{3}} \right)} \frac{1}{t} dt$$

$$\left(2 + 3 \log \left( \tanh \left( \sqrt{5} \sqrt{\frac{10}{18}} \sqrt{1 - \frac{1}{4}} \right) \right) \right) - \frac{47}{10^3} = \frac{1953}{1000} + 3 \log \left( \int_0^{\frac{5}{2\sqrt{3}}} \operatorname{sech}^2(t) dt \right)$$

**Observations**

It should be highlighted how all the expressions has been developed using always parameters belonging to the Ramanujan's mathematics, the Lucas and / or Fibonacci sequences connected strictly to the golden ratio, in addition to  $\pi$  and the golden ratio itself.

## **Acknowledgments**

We would like to thank Prof. **George E. Andrews** Evan Pugh Professor of Mathematics at Pennsylvania State University for his great availability and kindness towards me

## References

### **On Classical Stability with Broken Supersymmetry**

*I. Basile, J. Mourad and A. Sagnotti* - arXiv:1811.11448v2 [hep-th] 10 Jan 2019

### **Modular equations and approximations to $\pi$ – Srinivasa Ramanujan**

Quarterly Journal of Mathematics, XLV, 1914, 350 – 372