

New mathematical connections between various solutions of Ramanujan's equations, approximations to π and some parameters of Particle Physics (Yukawa's Pion) and Cosmology (value of Cosmological Constant). XV

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Abstract

In this research thesis, we have analyzed further Ramanujan formulas and described further possible mathematical connections with some parameters of Particle Physics (Yukawa's Pion) and Cosmology, principally the value of Cosmological Constant.

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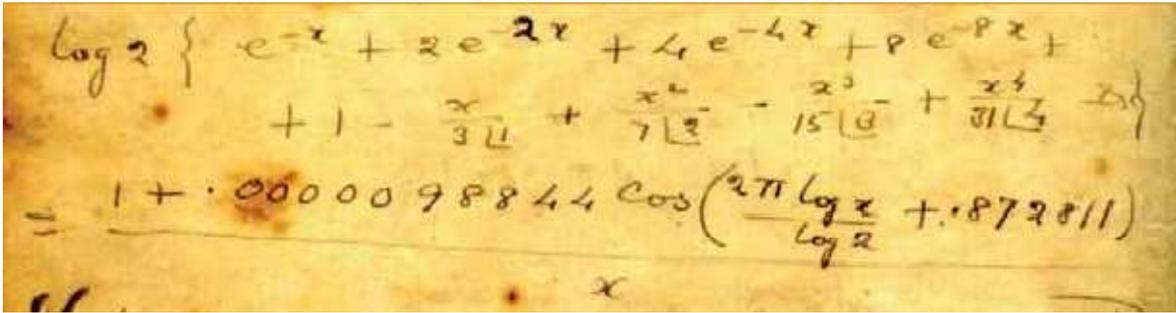
<https://www.britannica.com/biography/Srinivasa-Ramanujan>



https://it.wikipedia.org/wiki/Hideki_Yukawa

From:

MANUSCRIPT BOOK 3 OF SRINIVASA RAMANUJAN



For $x = 5$

$$1/5 * (((1 + 0.0000098844 \cos((2\pi * \ln(5)) / (\ln 2) + 0.872811))))$$

Input interpretation:

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right)$$

$\log(x)$ is the natural logarithm

Result:

0.19999808266...

0.19999808266...

Addition formulas:

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$0.2 + 1.97688 \times 10^{-6} \cos(0.872811) \cos\left(\frac{2\pi \log(5)}{\log(2)}\right) -$$

$$1.97688 \times 10^{-6} \sin(0.872811) \sin\left(\frac{2\pi \log(5)}{\log(2)}\right)$$

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$\frac{1}{5} + 1.97688 \times 10^{-6} \cos(0.872811) \cos\left(-\frac{2\pi \log(5)}{\log(2)}\right) +$$

$$1.97688 \times 10^{-6} \sin(0.872811) \sin\left(-\frac{2\pi \log(5)}{\log(2)}\right)$$

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$0.2 + 1.97688 \times 10^{-6} \cosh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) -$$

$$1.97688 \times 10^{-6} i \sinh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)$$

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} + 1.97688 \times 10^{-6} \cosh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) + \\ & 1.97688 \times 10^{-6} i \sinh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811) \end{aligned}$$

Alternative representations:

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cosh\left(i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) \right) \end{aligned}$$

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) \right) \end{aligned}$$

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} \left(1 + 4.9422 \times 10^{-6} \left(e^{-i(0.872811 + (2\pi \log(5))/\log(2))} + e^{i(0.872811 + (2\pi \log(5))/\log(2))} \right) \right) \end{aligned}$$

Series representations:

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} + 1.97688 \times 10^{-6} \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)^{2k}}{(2k)!} \end{aligned}$$

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} - 1.97688 \times 10^{-6} \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \pi \left(-\frac{1}{2} + \frac{2\log(5)}{\log(2)}\right)\right)^{1+2k}}{(1+2k)!} \end{aligned}$$

$$\begin{aligned} & \frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = \\ & \frac{1}{5} + 1.97688 \times 10^{-6} \sum_{k=0}^{\infty} \frac{\cos\left(\frac{k\pi}{2} + z_0\right) \left(0.872811 + \frac{2\pi \log(5)}{\log(2)} - z_0\right)^k}{k!} \end{aligned}$$

Integral representations:

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$\frac{1}{5} - 1.97688 \times 10^{-6} \int_{\frac{\pi}{2}}^{0.872811 + \frac{2\pi \log(5)}{\log(2)}} \sin(t) dt$$

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) = 0.200002 +$$

$$\int_0^1 \frac{(-1.72544 \times 10^{-6} \log(2) - 3.95376 \times 10^{-6} \pi \log(5)) \sin\left(t \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)}{\log(2)} dt$$

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$\frac{1}{5} + \frac{9.8844 \times 10^{-7} \sqrt{\pi}}{i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} e^{\frac{s - (0.436406 \log(2) + \pi \log(5))^2}{s \log^2(2)}} \frac{ds}{\sqrt{s}} \text{ for } \gamma > 0$$

$$\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) =$$

$$0.2 + \frac{9.8844 \times 10^{-7} \sqrt{\pi}}{i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{4^s \Gamma(s) \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)^{-2s}}{\Gamma\left(\frac{1}{2} - s\right)} ds \text{ for } 0 < \gamma < \frac{1}{2}$$

Handwritten notes on aged paper showing a formula and numerical calculations:

$$= \frac{2^m e^{\frac{1}{x}} \int_0^{\log \frac{1}{2}} \frac{da}{a} + (A x + B x^2 + \dots)}{\sqrt{2 + 2\pi(1-x)}} \left\{ \begin{array}{l} \log\left(\frac{2\pi}{\log 2}\right) = 2.20437894 \\ \frac{2\pi}{\log 2} = 9.0647203; \quad \frac{2\pi^2}{\log 2} = 28.4776587 \end{array} \right.$$

$$(2\pi)/\ln 2 + \ln((2\pi)/(\ln 2)) + (2\pi^2)/(\ln 2)$$

Input:

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)}$$

$\log(x)$ is the natural logarithm

Decimal approximation:

39.74676892062040829754981594521092926316133820588956731996...

39.74676892....

Alternate forms:

$$\frac{2\pi(1+\pi)}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\frac{2\pi + 2\pi^2 + \log(2)\log\left(\frac{2\pi}{\log(2)}\right)}{\log(2)}$$

$$\frac{2\pi + 2\pi^2 + \log(2)\log(\pi) - \log(2)(\log(\log(2)) - \log(2))}{\log(2)}$$

Alternative representations:

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \log_e\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi}{\log_e(2)} + \frac{2\pi^2}{\log_e(2)}$$

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \log(a)\log_a\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi}{\log(a)\log_a(2)} + \frac{2\pi^2}{\log(a)\log_a(2)}$$

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = -\text{Li}_1\left(1 - \frac{2\pi}{\log(2)}\right) + -\frac{2\pi}{\text{Li}_1(-1)} + -\frac{2\pi^2}{\text{Li}_1(-1)}$$

Series representations:

$$\begin{aligned} \frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = & \\ \frac{\left|\frac{\arg\left(\frac{2\pi}{\log(2)} - z_0\right)}{2\pi}\right| \log\left(\frac{1}{z_0}\right) + \log(z_0) + \left|\frac{\arg\left(\frac{2\pi}{\log(2)} - z_0\right)}{2\pi}\right| \log(z_0) + & \\ \frac{\log(z_0) + \left[\frac{\arg(2-z_0)}{2\pi}\right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0)\right) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k}}{2\pi^2} + & \\ \frac{\log(z_0) + \left[\frac{\arg(2-z_0)}{2\pi}\right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0)\right) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k}}{2\pi^2} - & \\ \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{2\pi}{\log(2)} - z_0\right)^k z_0^{-k}}{k} & \end{aligned}$$

$$\begin{aligned}
& \frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \\
& \left(-2\pi - 2\pi^2 + 4\pi^2 \left[\frac{\arg(2-x)}{2\pi} \right] \left[\frac{\arg\left(-x + \frac{2\pi}{\log(2)}\right)}{2\pi} \right] - 2i\pi \left[\frac{\arg(2-x)}{2\pi} \right] \log(x) - \right. \\
& \quad 2i\pi \left[\frac{\arg\left(-x + \frac{2\pi}{\log(2)}\right)}{2\pi} \right] \log(x) - \log^2(x) + \\
& \quad 2i\pi \left[\frac{\arg\left(-x + \frac{2\pi}{\log(2)}\right)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} + \\
& \quad \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} + 2i\pi \left[\frac{\arg(2-x)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(-x + \frac{2\pi}{\log(2)}\right)^k}{k} + \\
& \quad \log(x) \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(-x + \frac{2\pi}{\log(2)}\right)^k}{k} - \\
& \quad \left. \sum_{k_1=1}^{\infty} \sum_{k_2=1}^{\infty} \frac{(-1)^{k_1+k_2} (2-x)^{k_1} x^{-k_1-k_2} \left(-x + \frac{2\pi}{\log(2)}\right)^{k_2}}{k_1 k_2} \right) / \\
& \left(-2i\pi \left[\frac{\arg(2-x)}{2\pi} \right] - \log(x) + \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} \right) \text{ for } x < 0
\end{aligned}$$

$$\begin{aligned}
& \frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \\
& \left(-2\pi - 2\pi^2 + 4\pi^2 \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right]^2 - 4i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] \log(z_0) - \right. \\
& \quad \log^2(z_0) + 2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} + \\
& \quad \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} + 2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] \\
& \quad \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{2\pi}{\log(2)} - z_0\right)^k z_0^{-k}}{k} + \log(z_0) \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{2\pi}{\log(2)} - z_0\right)^k z_0^{-k}}{k} - \\
& \quad \left. \sum_{k_1=1}^{\infty} \sum_{k_2=1}^{\infty} \frac{(-1)^{k_1+k_2} (2-z_0)^{k_1} \left(\frac{2\pi}{\log(2)} - z_0\right)^{k_2} z_0^{-k_1-k_2}}{k_1 k_2} \right) / \\
& \left(-2i\pi \left[\frac{\pi - \arg\left(\frac{1}{z_0}\right) - \arg(z_0)}{2\pi} \right] - \log(z_0) + \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right)
\end{aligned}$$

Integral representations:

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \frac{2\pi + 2\pi^2 + \log(2) \int_0^1 \int_0^1 \frac{1}{(1+t_1)(\log(2)+(2\pi-\log(2))t_2)} dt_2 dt_1}{\int_1^2 \frac{1}{t} dt}$$

$$\frac{2\pi}{\log(2)} + \log\left(\frac{2\pi}{\log(2)}\right) + \frac{2\pi^2}{\log(2)} = \frac{i \left(8\pi^3 + 8\pi^4 - \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right) \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{2\pi}{\log(2)}\right)^{-s}}{\Gamma(1-s)} ds \right)}{2\pi \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds} \text{ for } -1 < \gamma < 0$$

$$\sqrt{(2\pi)/\ln 2 * \ln((2\pi)/(\ln 2)) * (2\pi^2)/(\ln 2) + 7}$$

Where 7 is a Lucas number

Input:

$$\sqrt{\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)} + 7}$$

log(x) is the natural logarithm

Exact result:

$$\sqrt{7 + \frac{4\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)}}$$

Decimal approximation:

24.00095127397296446243539768297818855527629886546675650885...

24.0009512739...

This value is linked to the "Ramanujan function" (an elliptic modular function that satisfies the need for "conformal symmetry") that has 24 "modes" corresponding to the physical vibrations of a bosonic string.

Alternate forms:

$$\sqrt{7 + \frac{4 \pi^3 (\log(2) + \log(\pi) - \log(\log(2)))}{\log^2(2)}}$$

$$\frac{\sqrt{7 \log^2(2) + 4 \pi^3 \log\left(\frac{2 \pi}{\log(2)}\right)}}{\log(2)}$$

$$\frac{\sqrt{7 \log^2(2) + 4 \pi^3 \log(\pi) - 4 \pi^3 \log\left(\frac{\log(2)}{2}\right)}}{\log(2)}$$

All 2nd roots of $7 + (4 \pi^3 \log((2 \pi)/\log(2)))/(\log^2(2))$:

$$e^0 \sqrt{7 + \frac{4 \pi^3 \log\left(\frac{2 \pi}{\log(2)}\right)}{\log^2(2)}} \approx 24.00 \text{ (real, principal root)}$$

$$e^{i \pi} \sqrt{7 + \frac{4 \pi^3 \log\left(\frac{2 \pi}{\log(2)}\right)}{\log^2(2)}} \approx -24.00 \text{ (real root)}$$

Alternative representations:

$$\sqrt{\frac{(\log\left(\frac{2 \pi}{\log(2)}\right)(2 \pi^2))(2 \pi)}{\log(2) \log(2)} + 7} = \sqrt{7 + 4 \pi \log_e\left(\frac{2 \pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log_e(2)}\right)^2}$$

$$\sqrt{\frac{(\log\left(\frac{2 \pi}{\log(2)}\right)(2 \pi^2))(2 \pi)}{\log(2) \log(2)} + 7} = \sqrt{7 + 4 \pi \log(a) \log_a\left(\frac{2 \pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log(a) \log_a(2)}\right)^2}$$

$$\sqrt{\frac{(\log\left(\frac{2 \pi}{\log(2)}\right)(2 \pi^2))(2 \pi)}{\log(2) \log(2)} + 7} = \sqrt{7 - 4 \pi \text{Li}_1\left(1 - \frac{2 \pi}{\log(2)}\right) \pi^2 \left(-\frac{1}{\text{Li}_1(-1)}\right)^2}$$

Series representations:

$$\sqrt{\frac{(\log(\frac{2\pi}{\log(2)})(2\pi^2))(2\pi)}{\log(2)\log(2)} + 7} = \sqrt{7 + \frac{4\pi^3 \left(2i\pi \left[\frac{\arg(-x + \frac{2\pi}{\log(2)})}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k x^{-k} \left(-x + \frac{2\pi}{\log(2)}\right)^k}{k} \right)}{\left(2i\pi \left[\frac{\arg(2-x)}{2\pi} \right] + \log(x) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-x)^k x^{-k}}{k} \right)^2}} \quad \text{for } x < 0$$

$$\sqrt{\frac{(\log(\frac{2\pi}{\log(2)})(2\pi^2))(2\pi)}{\log(2)\log(2)} + 7} = \sqrt{7 + \frac{4\pi^3 \left(2i\pi \left[\frac{\pi - \arg(\frac{1}{z_0}) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{2\pi}{\log(2)} - z_0\right)^k z_0^{-k}}{k} \right)}{\left(2i\pi \left[\frac{\pi - \arg(\frac{1}{z_0}) - \arg(z_0)}{2\pi} \right] + \log(z_0) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right)^2}}$$

$$\sqrt{\frac{(\log(\frac{2\pi}{\log(2)})(2\pi^2))(2\pi)}{\log(2)\log(2)} + 7} = \sqrt{7 + \frac{4\pi^3 \left(\log(z_0) + \left[\frac{\arg(\frac{2\pi}{\log(2)} - z_0)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k \left(\frac{2\pi}{\log(2)} - z_0\right)^k z_0^{-k}}{k} \right)}{\left(\log(z_0) + \left[\frac{\arg(2-z_0)}{2\pi} \right] \left(\log\left(\frac{1}{z_0}\right) + \log(z_0) \right) - \sum_{k=1}^{\infty} \frac{(-1)^k (2-z_0)^k z_0^{-k}}{k} \right)^2}}$$

Integral representations:

$$\sqrt{\frac{(\log(\frac{2\pi}{\log(2)})(2\pi^2))(2\pi)}{\log(2)\log(2)} + 7} = \sqrt{7 + \frac{4\pi^3 \int_1^{\frac{2\pi}{\log(2)}} \frac{1}{t} dt}{\left(\int_1^2 \frac{1}{t} dt \right)^2}}$$

$$\sqrt{\frac{(\log(\frac{2\pi}{\log(2)})(2\pi^2))(2\pi)}{\log(2)\log(2)} + 7} = \sqrt{7 + \frac{8i\pi^4 \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s) \left(-1 + \frac{2\pi}{\log(2)}\right)^{-s}}{\Gamma(1-s)} ds}{\left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{\Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \right)^2}}$$

for $-1 < \gamma < 0$

$$\left(\left(\left(\frac{1}{5} * \left(\left(\left(1 + 0.0000098844 \cos\left(\frac{2\pi \ln(5)}{\ln(2)} + 0.872811\right)\right)\right)\right)\right)\right) * \left[\frac{2\pi}{\ln 2} * \ln\left(\frac{2\pi}{\ln(2)}\right) * \frac{2\pi^2}{\ln(2)}\right] + 11 + \frac{1}{\text{golden ratio}}\right)$$

Where 11 is a Lucas number

Input interpretation:

$$\left(\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)\right) \left(\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)}\right) + 11 + \frac{1}{\phi}$$

log(x) is the natural logarithm

φ is the golden ratio

Result:

125.42607534...

125.42607534... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Addition formulas:

$$\frac{\left(2\pi \log\left(\frac{2\pi}{\log(2)}\right)\right) \left(2\pi^2\right) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \left(101170. + \cos(0.872811) \cos\left(-\frac{2\pi \log(5)}{\log(2)}\right) + \sin(0.872811) \sin\left(-\frac{2\pi \log(5)}{\log(2)}\right)\right)$$

$$\frac{\left(2\pi \log\left(\frac{2\pi}{\log(2)}\right)\right) \left(2\pi^2\right) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \left(101170. + \cos(0.872811) \cos\left(\frac{2\pi \log(5)}{\log(2)}\right) - \sin(0.872811) \sin\left(\frac{2\pi \log(5)}{\log(2)}\right)\right)$$

$$\frac{\left(2\pi \log\left(\frac{2\pi}{\log(2)}\right)\right) \left(2\pi^2\right) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \left(101170. + \cosh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) - i \left(\sinh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\left(101170. + \cosh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) + i \sinh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)$$

Alternative representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} = 11 + \frac{1}{\phi} +$$

$$\frac{4}{5} \pi \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)\right) \log\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log(2)}\right)^2$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{4}{5} \pi \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\left(1 + 4.9422 \times 10^{-6} \left(e^{-i(0.872811 + 2\pi \log(5))/\log(2)} + e^{i(0.872811 + 2\pi \log(5))/\log(2)}\right)\right)$$

$$\pi^2 \left(\frac{1}{\log(2)}\right)^2$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} = 11 + \frac{1}{\phi} +$$

$$\frac{4}{5} \pi \left(1 + 9.8844 \times 10^{-6} \cosh\left(i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)\right) \log_e\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log_e(2)}\right)^2$$

Series representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} = 11 + \frac{1}{\phi} +$$

$$\frac{0.8 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} + \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)^{2k}}{(2k)!}}{\log^2(2)}$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 11 + \frac{1}{\phi} = 11 + \frac{1}{\phi} +$$

$$\frac{4 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{5 \log^2(2)} - \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \pi \left(-\frac{1}{2} + \frac{2 \log(5)}{\log(2)}\right)\right)^{1+2k}}{(1+2k)!}}{\log^2(2)}$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2))^5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{0.8\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} +$$

$$\frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{\cos\left(\frac{k\pi}{2} + z_0\right) \left(0.872811 + \frac{2\pi \log(5)}{\log(2)} - z_0\right)^k}{k!}}{\log^2(2)}$$

Integral representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2))^5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} - \frac{1}{\log^3(2)} 0.000015815 \pi^3 \left(-50585.3 \log(2) +\right.$$

$$\left.0.436406 \log(2) + \pi \log(5) \int_0^1 \sin\left(t \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) dt\right) \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2))^5} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{0.8\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} - \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} \int_{\frac{\pi}{2}}^{0.872811 + \frac{2\pi \log(5)}{\log(2)}} \sin(t) dt$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2))^5} + 11 + \frac{1}{\phi} =$$

$$-\frac{1}{\phi \left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2)} 0.000015815$$

$$\left(-63230.9 \left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2) - 695540 \cdot \phi \left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2) - 50585.3 \phi \pi^3 \log(2)\right.$$

$$\left.\int_1^{\frac{2\pi}{\log(2)}} \frac{1}{t} dt + 2 \log(2) \int_0^1 \int_0^1 \frac{\sin\left(\left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right) t_2\right)}{\log(2) + (2\pi - \log(2)) t_1} dt_2 dt_1\right)$$

and:

$$\left(\left(\left(\frac{1}{5} * \left(\left(\left(1 + 0.0000098844 \cos\left(\frac{2\pi * \ln(5)}{\ln(2)} + 0.872811\right)\right)\right)\right)\right)\right) * \left[\frac{2\pi}{\ln 2} * \ln\left(\frac{2\pi}{\ln(2)}\right) * \frac{2\pi^2}{\ln(2)}\right] + 29 - \pi$$

Where 29 is a Lucas number

Input interpretation:

$$\left(\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)\right) \left(\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)}\right) + 29 - \pi$$

$\log(x)$ is the natural logarithm

Result:

139.66644870...

139.66644870... result practically equal to the rest mass of Pion meson 139.57 MeV

Addition formulas:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\left(101170. + \cos(0.872811) \cos\left(-\frac{2\pi \log(5)}{\log(2)}\right) + \sin(0.872811) \sin\left(-\frac{2\pi \log(5)}{\log(2)}\right)\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\left(101170. + \cos(0.872811) \cos\left(\frac{2\pi \log(5)}{\log(2)}\right) - \sin(0.872811) \sin\left(\frac{2\pi \log(5)}{\log(2)}\right)\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \left(101170. + \cosh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) - i \left(\sinh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{1}{\log^2(2)} 7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\left(101170. + \cosh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) + i \sinh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)$$

Alternative representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi = 29 - \pi +$$

$$\frac{4}{5} \pi \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)\right) \log\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log(2)}\right)^2$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{4}{5} \pi \log\left(\frac{2\pi}{\log(2)}\right) \left(1 + 4.9422 \times 10^{-6} \left(e^{-i(0.872811 + (2\pi \log(5))/\log(2))} + e^{i(0.872811 + (2\pi \log(5))/\log(2))}\right)\right) \pi^2 \left(\frac{1}{\log(2)}\right)^2$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi = 29 - \pi +$$

$$\frac{4}{5} \pi \left(1 + 9.8844 \times 10^{-6} \cosh\left(i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)\right) \log_e\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log_e(2)}\right)^2$$

Series representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{0.8 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} + \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)^{2k}}{(2k)!}}{\log^2(2)}$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi = 29 - \pi +$$

$$\frac{4 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{5 \log^2(2)} - \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \pi \left(-\frac{1}{2} + \frac{2 \log(5)}{\log(2)}\right)\right)^{1+2k}}{(1+2k)!}}{\log^2(2)}$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{0.8 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} + \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \sum_{k=0}^{\infty} \frac{\cos\left(\frac{k\pi}{2} + z_0\right) \left(0.872811 + \frac{2\pi \log(5)}{\log(2)} - z_0\right)^k}{k!}}{\log^2(2)}$$

Integral representations:

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi - \frac{1}{\log^3(2)} 0.000015815 \pi^3 \left(-50585.3 \log(2) + 0.436406 \log(2) + \pi \log(5) \int_0^1 \sin\left(t \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) dt\right) \log\left(\frac{2\pi}{\log(2)}\right)$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$29 - \pi + \frac{0.8 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} - \frac{7.90752 \times 10^{-6} \pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)} \int_{\frac{\pi}{2}}^{0.872811 + \frac{2\pi \log(5)}{\log(2)}} \sin(t) dt$$

$$\frac{(2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{(\log(2) \log(2)) 5} + 29 - \pi =$$

$$-\frac{1}{\left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2)} 0.000015815 \left[-1.8337 \times 10^6 \left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2) + 63230.9 \pi \left(\int_1^2 \frac{1}{t} dt\right)^2 \log(2) - 50585.3 \pi^3 \log(2) \int_1^{\frac{2\pi}{\log(2)}} \frac{1}{t} dt + 2 \log(2) \int_0^1 \int_0^1 \frac{\sin\left(\left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right) t_2\right)}{\log(2) + (2\pi - \log(2)) t_1} dt_2 dt_1\right]$$

$$[(2\pi)/\ln 2 * \ln((2\pi)/(\ln 2)) * (2\pi^2)/(\ln 2)] * 1 / (((1/5 * (((1 + 0.0000098844 \cos((2\pi * \ln(5))/(\ln 2) + 0.872811)))))))) + 123 + 11 + 4$$

Where 123, 11 and 4 are Lucas numbers

Input interpretation:

$$\left(\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)}\right) \times \frac{1}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)} + 123 + 11 + 4$$

log(x) is the natural logarithm

Result:

2983.2555869...

2983.2555869... result very near to the rest mass of Charmed eta meson 2980.3 MeV

Addition formulas:

$$\frac{(2\pi)\left(\log\left(\frac{2\pi}{\log(2)}\right)(2\pi^2)\right)}{\frac{1}{5}\left(1+9.8844\times 10^{-6}\cos\left(\frac{2\pi\log(5)}{\log(2)}+0.872811\right)\right)\log(2)\log(2)}+123+11+4=138+\left(20\pi^3\log\left(\frac{2\pi}{\log(2)}\right)\right)/\left(\log^2(2)\left(1+9.8844\times 10^{-6}\cos(0.872811)\cos\left(-\frac{2\pi\log(5)}{\log(2)}\right)+9.8844\times 10^{-6}\sin(0.872811)\sin\left(-\frac{2\pi\log(5)}{\log(2)}\right)\right)\right)$$

$$\frac{(2\pi)\left(\log\left(\frac{2\pi}{\log(2)}\right)(2\pi^2)\right)}{\frac{1}{5}\left(1+9.8844\times 10^{-6}\cos\left(\frac{2\pi\log(5)}{\log(2)}+0.872811\right)\right)\log(2)\log(2)}+123+11+4=138+\frac{2.02339\times 10^6\pi^3\log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2)\left(101170.+\cos(0.872811)\cos\left(\frac{2\pi\log(5)}{\log(2)}\right)-\sin(0.872811)\sin\left(\frac{2\pi\log(5)}{\log(2)}\right)\right)}$$

$$\frac{(2\pi)\left(\log\left(\frac{2\pi}{\log(2)}\right)(2\pi^2)\right)}{\frac{1}{5}\left(1+9.8844\times 10^{-6}\cos\left(\frac{2\pi\log(5)}{\log(2)}+0.872811\right)\right)\log(2)\log(2)}+123+11+4=138+\left(20\pi^3\log\left(\frac{2\pi}{\log(2)}\right)\right)/\left(\log^2(2)\left(1+9.8844\times 10^{-6}\cosh\left(\frac{2i\pi\log(5)}{\log(2)}\right)\cos(0.872811)+9.8844\times 10^{-6}i\sinh\left(\frac{2i\pi\log(5)}{\log(2)}\right)\sin(0.872811)\right)\right)$$

$$\frac{(2\pi)\left(\log\left(\frac{2\pi}{\log(2)}\right)(2\pi^2)\right)}{\frac{1}{5}\left(1+9.8844\times 10^{-6}\cos\left(\frac{2\pi\log(5)}{\log(2)}+0.872811\right)\right)\log(2)\log(2)}+123+11+4=138+\left(2.02339\times 10^6\pi^3\log\left(\frac{2\pi}{\log(2)}\right)\right)/\left(\log^2(2)\left(101170.+\cosh\left(-\frac{2i\pi\log(5)}{\log(2)}\right)\cos(0.872811)-i\left(\sinh\left(-\frac{2i\pi\log(5)}{\log(2)}\right)\sin(0.872811)\right)\right)\right)$$

Alternative representations:

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{4\pi \log\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log(2)}\right)^2}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) \right)}$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{4\pi \log_e\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log_e(2)}\right)^2}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cosh\left(i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) \right)}$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{4\pi \log_e\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log_e(2)}\right)^2}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right) \right)}$$

Series representations:

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{20\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2) \left(1 + 9.8844 \times 10^{-6} \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)^{2k}}{(2k)!} \right)}$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{20\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2) \left(1 - 9.8844 \times 10^{-6} \sum_{k=0}^{\infty} \frac{(-1)^k \left(0.872811 + \pi \left(-\frac{1}{2} + \frac{2\log(5)}{\log(2)}\right)\right)^{1+2k}}{(1+2k)!} \right)}$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{20\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\log^2(2) \left(1 + 9.8844 \times 10^{-6} \sum_{k=0}^{\infty} \frac{\cos\left(\frac{k\pi}{2} + z_0\right) \left(0.872811 + \frac{2\pi \log(5)}{\log(2)} - z_0\right)^k}{k!} \right)}$$

Integral representations:

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 + \frac{20\pi^3 \log\left(\frac{2\pi}{\log(2)}\right)}{\left(1 - 9.8844 \times 10^{-6} \int_{\frac{\pi}{2}}^{0.872811 + \frac{2\pi \log(5)}{\log(2)}} \sin(t) dt \right) \log^2(2)}$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$138 - \left(1.0117 \times 10^6 \pi^3 \log\left(\frac{2\pi}{\log(2)}\right) \right) / \left(\log(2) \left(-50585.3 \log(2) + \right. \right.$$

$$\left. \left. 0.436406 \log(2) + \pi \log(5) \int_0^1 \sin\left(t \left(0.872811 + \frac{2\pi \log(5)}{\log(2)} \right)\right) dt \right) \right)$$

$$\frac{(2\pi) \left(\log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right)}{\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \log(2) \log(2)} + 123 + 11 + 4 =$$

$$\left(20 \left[6.9 i \pi \left(\int_1^2 \frac{1}{t} dt \right)^2 + i \pi^4 \int_1^{\frac{2\pi}{\log(2)}} \frac{1}{t} dt + \right. \right.$$

$$\left. \left. 0.0000341012 \left(\int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{-\frac{(0.436406 \log(2) + \pi \log(5))^2}{s \log^2(2)}}}{\sqrt{s}} ds \right) \left(\int_1^2 \frac{1}{t} dt \right)^2 \sqrt{\pi} \right) \right] /$$

$$\left(\left(\int_1^2 \frac{1}{t} dt \right)^2 \left(i \pi + 4.9422 \times 10^{-6} \sqrt{\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{-\frac{(0.436406 \log(2) + \pi \log(5))^2}{s \log^2(2)}}}{\sqrt{s}} ds \right) \right) \text{ for } \gamma >$$

$$0$$

and:

$$\frac{1}{10^{52}} \left[-\frac{2}{10^4} + \frac{29}{(843+76+29+2)\pi} \left(\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)} \right) \right. \\ \left. \left(\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \right) \right]$$

Where 843, 76, 29 and 2 are Lucas numbers

Input interpretation:

$$\frac{1}{10^{52}} \left(-\frac{2}{10^4} + \frac{29}{(843+76+29+2)\pi} \left(\frac{2\pi}{\log(2)} \log\left(\frac{2\pi}{\log(2)}\right) \times \frac{2\pi^2}{\log(2)} \right) \right. \\ \left. \left(\frac{1}{5} \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right) \right) \right)$$

log(x) is the natural logarithm

Result:

$$1.1056531748... \times 10^{-52}$$

1.1056531748... * 10⁻⁵² result practically equal to the value of Cosmological Constant

$$1.1056 \times 10^{-52} \text{ m}^{-2}$$

Addition formulas:

$$\frac{-\frac{2}{10^4} + \frac{29 \left((2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right)}{(843+76+29+2)\pi (\log(2) \log(2)) 5}}{10^{52}} = -2. \times 10^{-56} + \frac{1}{\log^2(2)}$$

$$\pi^2 \log\left(\frac{2\pi}{\log(2)}\right) \left(2.44211 \times 10^{-54} + 2.41387 \times 10^{-59} \cos(0.872811) \cos\left(-\frac{2\pi \log(5)}{\log(2)}\right) + \right. \\ \left. 2.41387 \times 10^{-59} \sin(0.872811) \sin\left(-\frac{2\pi \log(5)}{\log(2)}\right) \right)$$

$$\frac{-\frac{2}{10^4} + \frac{29 \left((2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \right) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right) \right)}{(843+76+29+2)\pi (\log(2) \log(2)) 5}}{10^{52}} = -2. \times 10^{-56} + \frac{1}{\log^2(2)}$$

$$\pi^2 \log\left(\frac{2\pi}{\log(2)}\right) \left(2.44211 \times 10^{-54} + 2.41387 \times 10^{-59} \cos(0.872811) \cos\left(\frac{2\pi \log(5)}{\log(2)}\right) - \right. \\ \left. 2.41387 \times 10^{-59} \sin(0.872811) \sin\left(\frac{2\pi \log(5)}{\log(2)}\right) \right)$$

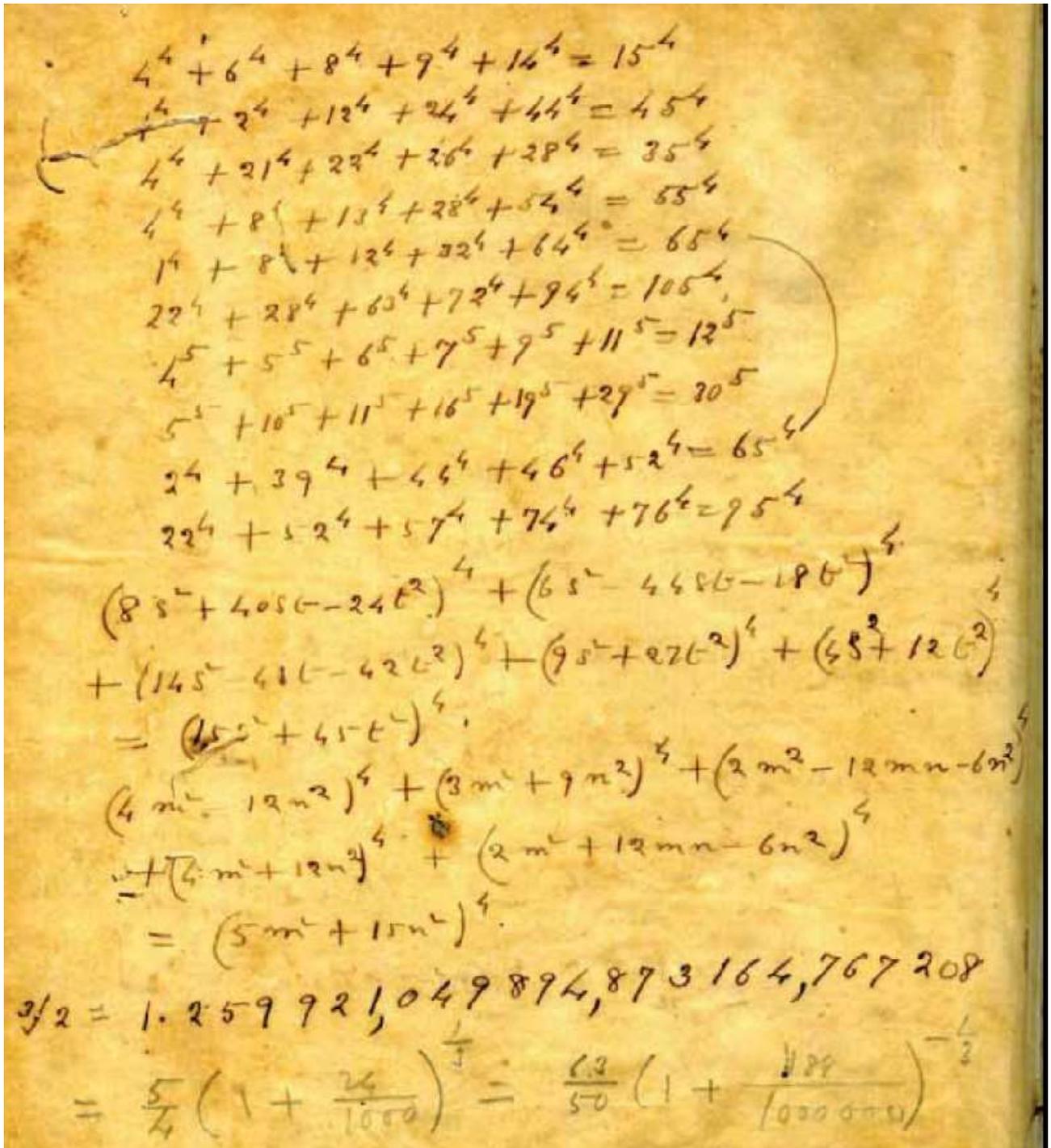
$$\begin{aligned}
& -\frac{2}{10^4} + \frac{2^{\vartheta} (2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{((843+76+2^{\vartheta}+2)\pi) (\log(2) \log(2)) 5} = \\
& -2. \times 10^{-56} + \frac{1}{\log^2(2)} \pi^2 \log\left(\frac{2\pi}{\log(2)}\right) \\
& \left(2.44211 \times 10^{-54} + 2.41387 \times 10^{-5\vartheta} \cosh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) - \right. \\
& \left. 2.41387 \times 10^{-5\vartheta} i \sinh\left(-\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)
\end{aligned}$$

$$\begin{aligned}
& -\frac{2}{10^4} + \frac{2^{\vartheta} (2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{((843+76+2^{\vartheta}+2)\pi) (\log(2) \log(2)) 5} = \\
& -2. \times 10^{-56} + \frac{1}{\log^2(2)} \pi^2 \log\left(\frac{2\pi}{\log(2)}\right) \\
& \left(2.44211 \times 10^{-54} + 2.41387 \times 10^{-5\vartheta} \cosh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \cos(0.872811) + \right. \\
& \left. 2.41387 \times 10^{-5\vartheta} i \sinh\left(\frac{2i\pi \log(5)}{\log(2)}\right) \sin(0.872811)\right)
\end{aligned}$$

Alternative representations:

$$\begin{aligned}
& -\frac{2}{10^4} + \frac{2^{\vartheta} (2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{((843+76+2^{\vartheta}+2)\pi) (\log(2) \log(2)) 5} = \\
& \frac{116\pi \left(1 + 9.8844 \times 10^{-6} \cosh\left(-i\left(0.872811 + \frac{2\pi \log(5)}{\log(2)}\right)\right)\right) \log\left(\frac{2\pi}{\log(2)}\right) \pi^2 \left(\frac{1}{\log(2)}\right)^2}{5 (950\pi)} - \frac{2}{10^4} \\
& 10^{52}
\end{aligned}$$

$$\begin{aligned}
& -\frac{2}{10^4} + \frac{2^{\vartheta} (2\pi) \log\left(\frac{2\pi}{\log(2)}\right) (2\pi^2) \left(1 + 9.8844 \times 10^{-6} \cos\left(\frac{2\pi \log(5)}{\log(2)} + 0.872811\right)\right)}{((843+76+2^{\vartheta}+2)\pi) (\log(2) \log(2)) 5} = \\
& \frac{1}{10^{52}} \left(\frac{1}{5 (950\pi)} 116\pi \log\left(\frac{2\pi}{\log(2)}\right) \right. \\
& \left. \left(1 + 4.9422 \times 10^{-6} \left(e^{-i(0.872811 + (2\pi \log(5))/\log(2))} + e^{i(0.872811 + (2\pi \log(5))/\log(2))}\right)\right) \right. \\
& \left. \pi^2 \left(\frac{1}{\log(2)}\right)^2 - \frac{2}{10^4} \right)
\end{aligned}$$



We have that:

$$\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}} = \frac{63}{50} \sqrt[3]{1 + \frac{188}{1000000}}$$

Input:

$$\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}} = \frac{63}{50} \left(1 + \frac{188}{1000000}\right)^{-1/3}$$

Result:

True

Left hand side:

$$\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}} = \sqrt[3]{2}$$

Right hand side:

$$\frac{63}{50} \left(1 + \frac{188}{1000000}\right)^{-1/3} = \sqrt[3]{2}$$

$$5/4(1+24/1000)^{1/3}$$

Input:

$$\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}}$$

Result:

$$\sqrt[3]{2}$$

Decimal approximation:

1.259921049894873164767210607278228350570251464701507980081...

1.259921049....

$$1 + 1 / \left(\left(\frac{5}{4} (1 + 24/1000)^{1/3} \right) \right)^2 + (11+4)/10^3$$

Where 11 and 4 are Lucas numbers

Input:

$$1 + \frac{1}{\left(\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}}\right)^2} + \frac{11+4}{10^3}$$

Result:

$$\frac{203}{200} + \frac{1}{2^{2/3}}$$

Decimal approximation:

1.644960524947436582383605303639114175285125732350753990040...

$$1.64496052494.... \approx \zeta(2) = \frac{\pi^2}{6} = 1.644934 ...$$

Alternate forms:

$$\frac{1}{200} (203 + 100 \sqrt[3]{2})$$

$$\frac{\sqrt[3]{2}}{2} + \frac{203}{200}$$

$$\frac{200 + 203 \times 2^{2/3}}{200 \times 2^{2/3}}$$

Minimal polynomial:

$$8\,000\,000\,x^3 - 24\,360\,000\,x^2 + 24\,725\,400\,x - 10\,365\,427$$

$$1/10^{27} * (((1+1/(((5/4(1+24/1000)^{1/3})))^2 + (47-4)/10^3)))$$

Where 47 and 4 are Lucas numbers

Input:

$$\frac{1}{10^{27}} \left(1 + \frac{1}{\left(\frac{5}{4} \sqrt[3]{1 + \frac{24}{1000}} \right)^2} + \frac{47-4}{10^3} \right)$$

Result:

$$\frac{\frac{1043}{1000} + \frac{1}{2^{2/3}}}{1\,000\,000\,000\,000\,000\,000\,000\,000\,000}$$

Decimal approximation:

$$1.6729605249474365823836053036391141752851257323507539... \times 10^{-27}$$

1.6729605249....*10⁻²⁷ result practically equal to the proton mass in kg

Now, we have that:

The image shows a handwritten mathematical derivation on aged paper. It starts with the sum of four fourth powers:

$$(8s^2 + 40st - 24t^2)^4 + (6s^2 - 44st - 18t^2)^4 + (14s^2 - 44st - 42t^2)^4 + (9s^2 + 27t^2)^4 + (4s^2 + 12t^2)^4$$
 This sum is then equated to a single fourth power:

$$= (65s^2 + 41t^2)^4$$

For $s = 1$ and $t = \sqrt{2} - 1$, we obtain:

$$\begin{aligned} &(((8+40((\sqrt{2})-1)-24((\sqrt{2})-1)^2)))^4 + (((6-44*((\sqrt{2})-1)-18((\sqrt{2})-1)^2)))^4 + \\ &(((14-41((\sqrt{2})-1)-42((\sqrt{2})-1)^2)))^4 + (((9+27((\sqrt{2})-1)^2)))^4 + \\ &(((4+12((\sqrt{2})-1)^2)))^4 \end{aligned}$$

Input:

$$\begin{aligned} &(8 + 40(\sqrt{2} - 1) - 24(\sqrt{2} - 1)^2)^4 + (6 - 44(\sqrt{2} - 1) - 18(\sqrt{2} - 1)^2)^4 + \\ &(14 - 41(\sqrt{2} - 1) - 42(\sqrt{2} - 1)^2)^4 + (9 + 27(\sqrt{2} - 1)^2)^4 + (4 + 12(\sqrt{2} - 1)^2)^4 \end{aligned}$$

Decimal approximation:

276577.8683745279640708514905690235069071751149137553100813...
276577.8683745....

Alternate form:

$$1910942497 - 1351044828\sqrt{2}$$

Minimal polynomial:

$$x^2 - 3821884994x + 1056972309495841$$

$$(((45+45((\sqrt{2})-1)^2)))^4$$

Input:

$$(45 + 45(\sqrt{2} - 1)^2)^4$$

Decimal approximation:

7.72551228965922470981773462088203512210375631288497210... $\times 10^6$
7.725512289659... $\times 10^6$

Alternate forms:

$$262440000(17 - 12\sqrt{2})$$

$$4461480000 - 3149280000\sqrt{2}$$

$$(180 - 90\sqrt{2})^4$$

Minimal polynomial:

$$x^2 - 8922960000x + 68874753600000000$$

And:

$$\left(\frac{(45+45((\sqrt{2}-1)^2))}{276577.868374527964}\right)^4$$

Input interpretation:

$$\frac{(45 + 45(\sqrt{2} - 1)^2)^4}{276577.868374527964}$$

Result:

27.9325035479618385...

27.9325035479....

$$\left(\frac{(45+45((\sqrt{2}-1)^2))}{276577.868374527964}\right)^4 + \phi^2$$

Input interpretation:

$$\left(\frac{(45 + 45(\sqrt{2} - 1)^2)^4}{276577.868374527964}\right)^2 + \phi^2$$

ϕ is the golden ratio

Result:

782.842788445650588...

782.8427884.... result practically equal to the rest mass of Omega meson 782.65 MeV

$$\frac{1}{\sqrt{2}} \left[\left((8+40((\sqrt{2}-1)-24((\sqrt{2}-1)^2)))^4 + ((6-44*((\sqrt{2}-1)-18((\sqrt{2}-1)^2)))^4 + ((14-41((\sqrt{2}-1)-42((\sqrt{2}-1)^2)))^4 + ((9+27((\sqrt{2}-1)^2)))^4 + ((4+12((\sqrt{2}-1)^2)))^4 \right] + 1314.5$$

Where 1314.5 is the average mass of $a_2(1320)$ meson

Input interpretation:

$$\frac{1}{\sqrt{2}} \left(\left((8 + 40(\sqrt{2} - 1) - 24(\sqrt{2} - 1)^2)^4 + (6 - 44(\sqrt{2} - 1) - 18(\sqrt{2} - 1)^2)^4 + (14 - 41(\sqrt{2} - 1) - 42(\sqrt{2} - 1)^2)^4 + (9 + 27(\sqrt{2} - 1)^2)^4 + (4 + 12(\sqrt{2} - 1)^2)^4 \right) + 1314.5 \right)$$

Result:

196884.6...

196884.6...

196884 is a fundamental number of the following j -invariant

$$j(\tau) = q^{-1} + 744 + 196884q + 21493760q^2 + 864299970q^3 + 20245856256q^4 + \dots$$

(In mathematics, Felix Klein's j -invariant or j function, regarded as a function of a complex variable τ , is a modular function of weight zero for $SL(2, \mathbb{Z})$ defined on the upper half plane of complex numbers. Several remarkable properties of j have to do with its q expansion (Fourier series expansion), written as a Laurent series in terms of $q = e^{2\pi i\tau}$ (the square of the nome), which begins:

$$j(\tau) = q^{-1} + 744 + 196884q + 21493760q^2 + 864299970q^3 + 20245856256q^4 + \dots$$

Note that j has a simple pole at the cusp, so its q -expansion has no terms below q^{-1} .

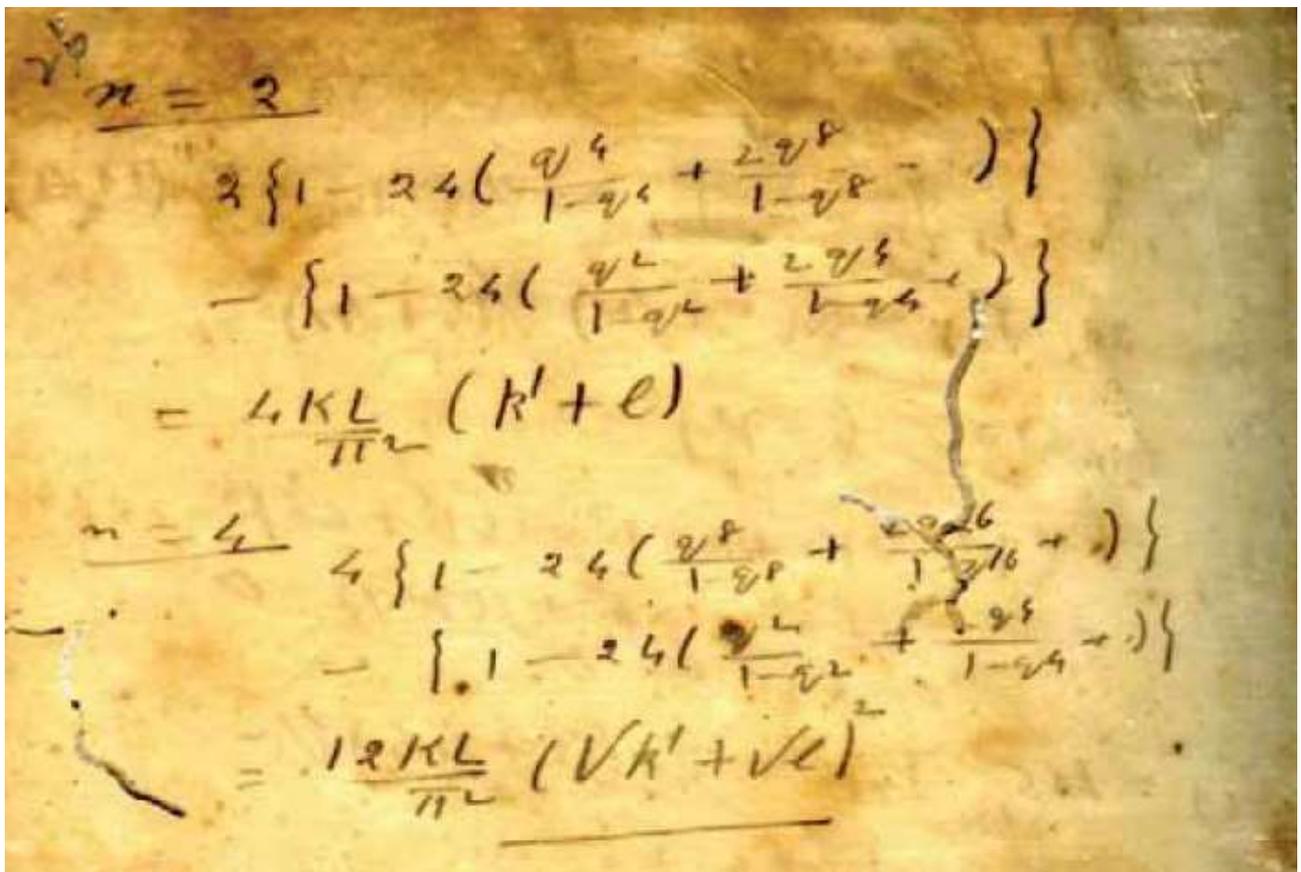
All the Fourier coefficients are integers, which results in several almost integers, notably Ramanujan's constant:

$$e^{\pi\sqrt{163}} \approx 640320^3 + 744.$$

The asymptotic formula for the coefficient of q^n is given by

$$\frac{e^{4\pi\sqrt{n}}}{\sqrt{2}n^{3/4}},$$

as can be proved by the Hardy–Littlewood circle method)



$$q = e^{-2\pi} = 0.0018674427\dots$$

indeed:

$$e^{(-2 \cdot \pi)}$$

Input:

$$e^{-2\pi}$$

Decimal approximation:

0.001867442731707988814430212934827030393422805002475317199...

0.0018674427...

Property:

$e^{-2\pi}$ is a transcendental number

Alternative representations:

$$e^{-2\pi} = e^{-360^\circ}$$

$$e^{-2\pi} = e^{2i \log(-1)}$$

$$e^{-2\pi} = \exp^{-2\pi}(z) \text{ for } z = 1$$

Series representations:

$$e^{-2\pi} = e^{-8 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

$$e^{-2\pi} = \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{-2\pi}$$

$$e^{-2\pi} = \left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}} \right)^{-2\pi}$$

Integral representations:

$$e^{-2\pi} = e^{-8 \int_0^1 \sqrt{1-t^2} dt}$$

$$e^{-2\pi} = e^{-4 \int_0^1 1/\sqrt{1-t^2} dt}$$

$$e^{-2\pi} = e^{-4 \int_0^{\infty} 1/(1+t^2) dt}$$

Note that:

$$1 + e^{-2\pi}$$

Input:

$$1 + e^{-2\pi}$$

Decimal approximation:

1.001867442731707988814430212934827030393422805002475317199...

1.00186744273... result practically equal to the following Rogers-Ramanujan continued fraction:

$$\frac{e^{\frac{2\pi}{5}}}{\sqrt{\varphi\sqrt{5}-\varphi}} = 1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}{1 + \frac{e^{-6\pi}}{1 + \frac{e^{-8\pi}}{1 + \dots}}}} \approx 1.0018674362$$

Property:

$1 + e^{-2\pi}$ is a transcendental number

Alternate form:

$$e^{-2\pi} (1 + e^{2\pi})$$

Alternative representations:

$$1 + e^{-2\pi} = 1 + e^{-360^\circ}$$

$$1 + e^{-2\pi} = 1 + e^{2i \log(-1)}$$

$$1 + e^{-2\pi} = 1 + \exp^{-2\pi}(z) \text{ for } z = 1$$

Series representations:

$$1 + e^{-2\pi} = 1 + e^{-8 \sum_{k=0}^{\infty} (-1)^k / (1+2k)}$$

$$1 + e^{-2\pi} = 1 + \left(\sum_{k=0}^{\infty} \frac{1}{k!} \right)^{-2\pi}$$

$$1 + e^{-2\pi} = 1 + \left(\frac{1}{\sum_{k=0}^{\infty} \frac{(-1)^k}{k!}} \right)^{-2\pi}$$

Integral representations:

$$1 + e^{-2\pi} = 1 + e^{-8 \int_0^1 \sqrt{1-t^2} dt}$$

$$1 + e^{-2\pi} = 1 + e^{-4 \int_0^1 1/\sqrt{1-t^2} dt}$$

$$1 + e^{-2\pi} = 1 + e^{-4 \int_0^{\infty} 1/(1+t^2) dt}$$

We have that:

Handwritten mathematical derivation on aged paper. The text shows the expression for $n=2$, involving terms like $24\left(\frac{q^4}{1-q^4} + \frac{2q^8}{1-q^8}\right)$ and a final result of $\frac{4KL}{\pi^2} (k' + e)$.

For $q = e^{-2\pi} = 0.0018674427\dots$, we obtain:

$$2\left(\left(1-24\left(\frac{0.0018674427^4}{1-0.0018674427^4}+2*0.0018674427^8/(1-0.0018674427^8)\right)\right)\right)-\left(\left(1-24\left(\frac{0.0018674427^2}{1-0.0018674427^2}+2*0.0018674427^4/(1-0.0018674427^4)\right)\right)\right)$$

Input interpretation:

$$2\left(1-24\left(\frac{0.0018674427^4}{1-0.0018674427^4}+2\times\frac{0.0018674427^8}{1-0.0018674427^8}\right)\right)-\left(1-24\left(\frac{0.0018674427^2}{1-0.0018674427^2}+2\times\frac{0.0018674427^4}{1-0.0018674427^4}\right)\right)$$

Result:

1.000083696505585158027787945615603281200307383231703390371...

1.0000836965...

$$\left(\frac{76+29}{10^3}+\frac{55}{10^5}\right)+\left[2\left(\left(1-24\left(\frac{0.0018674427^4}{1-0.0018674427^4}+2*0.0018674427^8/(1-0.0018674427^8)\right)\right)\right)-\left(\left(1-24\left(\frac{0.0018674427^2}{1-0.0018674427^2}+2*0.0018674427^4/(1-0.0018674427^4)\right)\right)\right)\right]$$

Where 76 and 29 are Lucas numbers, while 55 is a Fibonacci number

Input interpretation:

$$\left(\frac{76 + 29}{10^3} + \frac{55}{10^5} \right) + \left(2 \left(1 - 24 \left(\frac{0.0018674427^4}{1 - 0.0018674427^4} + 2 \times \frac{0.0018674427^8}{1 - 0.0018674427^8} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + 2 \times \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right) \right)$$

Result:

1.105633696505585158027787945615603281200307383231703390371...

1.1056336965...

From which:

$$1/10^{52} * 1.105633696505585158027787945615603281200307383231703390371$$

Input interpretation:

$$\frac{1}{10^{52}} \times 1.105633696505585158027787945615603281200307383231703390371$$

Result:

1.1056336965055851580277879456156032812003073832317033... $\times 10^{-52}$

1.1056336965... $\times 10^{-52}$ result practically equal to the value of Cosmological Constant

1.1056 $\times 10^{-52} \text{ m}^{-2}$

$$4x/\pi^2 * (y+z) = 2 \left(\left(1 - 24 \left(\frac{0.0018674427^4}{1 - 0.0018674427^4} + 2 \times \frac{0.0018674427^8}{1 - 0.0018674427^8} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + 2 \times \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right) \right)$$

Input interpretation:

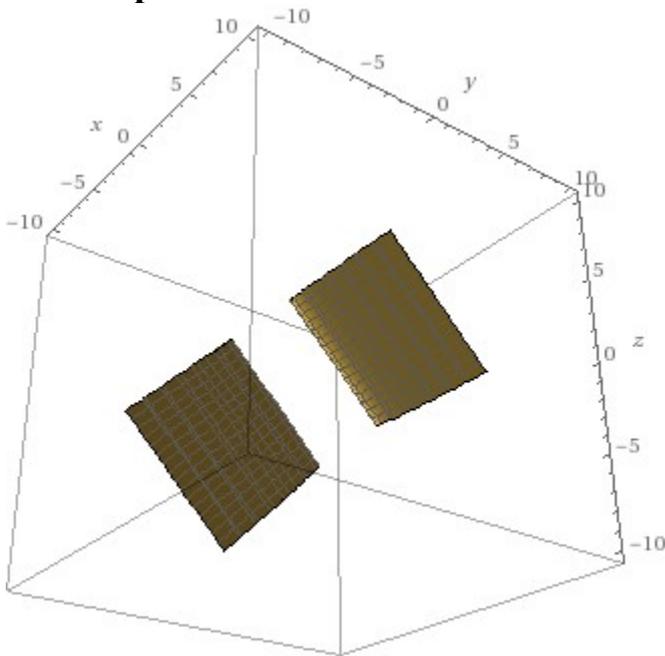
$$4 \times \frac{x}{\pi^2} (y+z) = 2 \left(1 - 24 \left(\frac{0.0018674427^4}{1 - 0.0018674427^4} + 2 \times \frac{0.0018674427^8}{1 - 0.0018674427^8} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + 2 \times \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right)$$

Result:

$$\frac{4x(y+z)}{\pi^2} = 1.00008$$

Geometric figure:

hyperbolic cylinder

Surface plot:**Alternate forms:**

$$xz = 2.46761 - xy$$

$$\frac{4xy}{\pi^2} + \frac{4xz}{\pi^2} - 1.00008 = 0$$

Expanded form:

$$\frac{4xy}{\pi^2} + \frac{4xz}{\pi^2} = 1.00008$$

Solution:

$$x \neq 0, \quad z \approx \frac{5.81818 \times 10^{-15} (4.2412 \times 10^{14} - 1.71875 \times 10^{14} xy)}{x}$$

Solution for the variable z:

$$z \approx \frac{2.4674 (1.00008 - 0.405285 xy)}{x}$$

From

$$4 \times \frac{x}{\pi^2} (y+z) = 2 \left(1 - 24 \left(\frac{0.0018674427^4}{1 - 0.0018674427^4} + 2 \times \frac{0.0018674427^8}{1 - 0.0018674427^8} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + 2 \times \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right)$$

for $x = 1$, we obtain:

$$z \approx \frac{2.4674 (1.00008 - 0.405285 x y)}{x}$$

Root:

$$x \neq 0, \quad y \approx \frac{2.4676}{x}$$

$$4/\pi^2 * (2.4676+z)$$

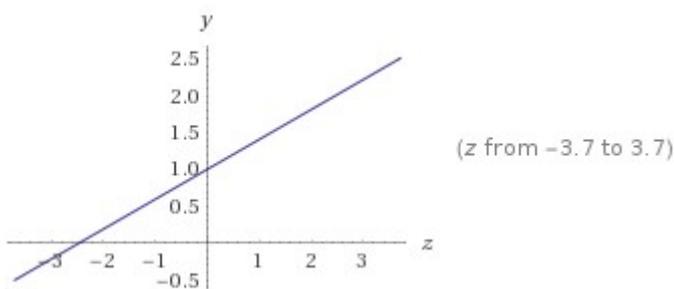
Input interpretation:

$$\frac{4}{\pi^2} (2.4676 + z)$$

Result:

$$\frac{4(z + 2.4676)}{\pi^2}$$

Plot:



Geometric figure:

line

Alternate forms:

$$0.000162114 (2500 z + 6169)$$

$$0.000162114 (2500 z + 6169)$$

$$0.101329 (3.99968 z + 9.8696)$$

Expanded form:

$$\frac{4z}{\pi^2} + 1.00008$$

Root:

$$z \approx -2.4676$$

$$z = -2.4676$$

Branch points:

(none; function is entire)

Derivative:

$$\frac{d}{dz} \left(\frac{4(z + 2.4676)}{\pi^2} \right) = \frac{4}{\pi^2}$$

Indefinite integral:

$$\int \frac{4(2.4676 + z)}{\pi^2} dz = 0.405285 (0.5 z^2 + 2.4676 z) + \text{constant}$$

Definite integral after subtraction of diverging parts:

$$\int_0^\infty \left(\frac{4(2.4676 + z)}{\pi^2} - \left(1.00008 + \frac{4z}{\pi^2} \right) \right) dz = 0$$

From

$$x \neq 0, \quad z \approx \frac{5.81818 \times 10^{-15} (4.2412 \times 10^{14} - 1.71875 \times 10^{14} x y)}{x}$$

$$y = 2,4682943473419$$

Thence:

$$\begin{aligned} & 4/\pi^2 * (2.4682943473419 - 2.467596876) = 2(((1 - 24(((0.0018674427^4 / (1 - \\ & 0.0018674427^4) + 2 * 0.0018674427^8 / (1 - 0.0018674427^8)))))) - (((1 - \\ & 24(((0.0018674427^2 / (1 - 0.0018674427^2) + 2 * 0.0018674427^4 / (1 - \\ & 0.0018674427^4)))))))) \end{aligned}$$

From

$$4/\pi^2 * (2.4682943473419 - 2.467596876)$$

we obtain:

Input interpretation:

$$\frac{4}{\pi^2} (2.4682943473419 - 2.467596876)$$

Result:

0.000282674487671670620408072438986961669760567041318766132...

0.00028267448...

Alternative representations:

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.00278989}{(180^\circ)^2}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.00278989}{6 \zeta(2)}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.00278989}{(-i \log(-1))^2}$$

Series representations:

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.000174368}{\left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}\right)^2}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.000697471}{\left(-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}\right)^2}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.00278989}{\left(\sum_{k=0}^{\infty} \frac{2^{-k}(-6+50k)}{\binom{3k}{k}}\right)^2}$$

Integral representations:

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.000697471}{\left(\int_0^{\infty} \frac{1}{1+t^2} dt\right)^2}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.000174368}{\left(\int_0^1 \sqrt{1-t^2} dt\right)^2}$$

$$\frac{(2.46829434734190000 - 2.4676) 4}{\pi^2} = \frac{0.000697471}{\left(\int_0^\infty \frac{\sin(t)}{t} dt\right)^2}$$

And from

$$2\left(\left(1-24\left(\frac{0.0018674427^4}{1-0.0018674427^4}+2*0.0018674427^8/(1-0.0018674427^8)\right)\right)\right)-\left(\left(1-24\left(\frac{0.0018674427^2}{1-0.0018674427^2}+2*0.0018674427^4/(1-0.0018674427^4)\right)\right)\right)$$

we obtain:

Result:

1.000083696505585158027787945615603281200307383231703390371...
1.0000836965...

We obtain from the difference between the two results:

$$2\left(\left(1-24\left(\frac{0.0018674427^4}{1-0.0018674427^4}+2*0.0018674427^8/(1-0.0018674427^8)\right)\right)\right)-\left(\left(1-24\left(\frac{0.0018674427^2}{1-0.0018674427^2}+2*0.0018674427^4/(1-0.0018674427^4)\right)\right)\right) - 4/\pi^2 * (2.4682943473419-2.467596876)$$

$$1.0000836965055851 - 0.00028267448767167$$

Input interpretation:

1.0000836965055851 - 0.00028267448767167

Result:

0.99980102201791343

0.99980102201791343 result very near to the value of the following Rogers-Ramanujan continued fraction:

$$\frac{e^{-\frac{\pi}{\sqrt{5}}}}{\sqrt{5}} = 1 - \frac{e^{-\pi\sqrt{5}}}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-3\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}}} - \phi + 1 \approx 0.9991104684$$

Repeating decimal:

0.999801022017913430

We have also:

2*1/log base 0.987344899(1.0000836965055851 - 0.00028267448767167)-
Pi+1/golden ratio

Input interpretation:

$$2 \times \frac{1}{\log_{0.987344899}(1.0000836965055851 - 0.00028267448767167)} - \pi + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

125.4765...

125.4765... result very near to the dilaton mass calculated as a type of Higgs boson:
125 GeV for T = 0 and to the Higgs boson mass 125.18 GeV

Alternative representation:

$$\frac{2}{\log_{0.987345}(1.00008369650558510000 - 0.000282674487671670000)} - \pi + \frac{1}{\phi} = -\pi + \frac{1}{\phi} + \frac{2}{\frac{\log(0.99980102201791343000)}{\log(0.987345)}}$$

Series representations:

$$\frac{2}{\log_{0.987345}(1.00008369650558510000 - 0.000282674487671670000)} - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2 \log(0.987345)}{\sum_{k=1}^{\infty} \frac{(-1)^k (-0.00019897798208657000)^k}{k}}$$

$$\frac{2}{\log_{0.987345}(1.00008369650558510000 - 0.000282674487671670000)} - \pi + \frac{1}{\phi} =$$

$$\frac{1}{\phi} - \pi - \frac{2}{\log(0.99980102201791343000) \left(78.5195 + \sum_{k=0}^{\infty} (-0.0126551)^k G(k) \right)}$$

for $\left(G(0) = 0 \text{ and } G(k) = \frac{(-1)^{1+k} k}{2(1+k)(2+k)} + \sum_{j=1}^k \frac{(-1)^{1+j} G(-j+k)}{1+j} \right)$

And:

$$2 * 1 / \log \text{ base } 0.987344899(1.0000836965055851 - 0.00028267448767167) + 11 + 1 / \text{golden ratio}$$

Where 11 is a Lucas number

Input interpretation:

$$2 \times \frac{1}{\log_{0.987344899}(1.0000836965055851 - 0.00028267448767167)} + 11 + \frac{1}{\phi}$$

$\log_b(x)$ is the base- b logarithm

ϕ is the golden ratio

Result:

139.6180...

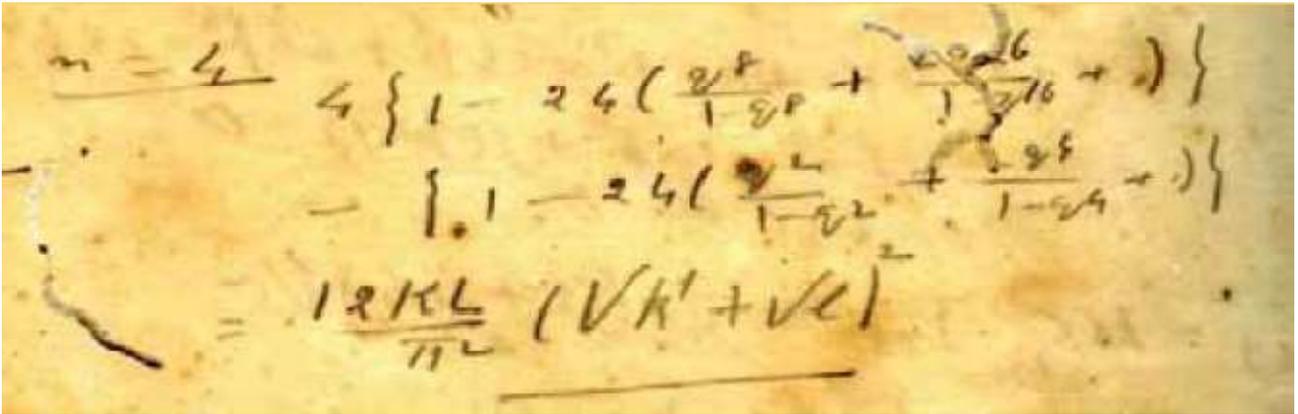
139.618... result practically equal to the rest mass of Pion meson 139.57 MeV

Alternative representation:

$$\frac{2}{\log_{0.987345}(1.00008369650558510000 - 0.000282674487671670000)} + 11 + \frac{1}{\phi} =$$

$$11 + \frac{1}{\phi} + \frac{2}{\frac{\log(0.99980102201791343000)}{\log(0.987345)}}$$

Now, we have that:



$q = e^{-2\pi} = 0.0018674427\dots$, we obtain:

$$4(((1-24(((0.0018674427^8/(1-0.0018674427^8)+2*0.0018674427^16/(1-0.0018674427^16)))))))-(((1-24(((0.0018674427^2/(1-0.0018674427^2)+0.0018674427^4/(1-0.0018674427^4))))))))$$

Input interpretation:

$$4 \left(1 - 24 \left(\frac{0.0018674427^8}{1 - 0.0018674427^8} + 2 \times \frac{0.0018674427^{16}}{1 - 0.0018674427^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right)$$

Result:

3.000083696797462499233594382721855970260810354276485041811...

3.0000836967974.....

And:

$$4(((1-24(((0.0018674427^8/(1-0.0018674427^8)+2*0.0018674427^16/(1-0.0018674427^16)))))))-(((1-24(((0.0018674427^2/(1-0.0018674427^2)+0.0018674427^4/(1-0.0018674427^4))))))))-golden\ ratio-34/123$$

Input interpretation:

$$4 \left(1 - 24 \left(\frac{0.0018674427^8}{1 - 0.0018674427^8} + 2 \times \frac{0.0018674427^{16}}{1 - 0.0018674427^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right) - \phi - \frac{34}{123}$$

ϕ is the golden ratio

Result:

1.10562694382...

1.10562694382...

Alternative representations:

$$\begin{aligned}
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right) - \\
& \left(1 - 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) \right) - \phi - \frac{34}{123} = \\
& -1 - \frac{34}{123} + 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) + \\
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right) - 2 \sin(54^\circ)
\end{aligned}$$

$$\begin{aligned}
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right) - \\
& \left(1 - 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) \right) - \phi - \frac{34}{123} = \\
& -1 + 2 \cos(216^\circ) - \frac{34}{123} + 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) + \\
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right) - \\
& \left(1 - 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) \right) - \phi - \frac{34}{123} = \\
& -1 - \frac{34}{123} + 24 \left(\frac{0.00186744^2}{1 - 0.00186744^2} + \frac{0.00186744^4}{1 - 0.00186744^4} \right) + \\
& 4 \left(1 - 24 \left(\frac{0.00186744^8}{1 - 0.00186744^8} + \frac{2 \times 0.00186744^{16}}{1 - 0.00186744^{16}} \right) \right) + 2 \sin(666^\circ)
\end{aligned}$$

From which:

$$\frac{1}{10^{52}} \left(\left(\left(\left(4 \cdot \left(\frac{0.0018674^8}{1-0.0018674^8} + 2 \cdot \frac{0.0018674^{16}}{1-0.0018674^{16}} \right) \right) - \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) - \phi - \frac{34}{123} \right) \right)$$

Input:

$$\frac{1}{10^{52}} \left(4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + 2 \times \frac{0.0018674^{16}}{1-0.0018674^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) - \phi - \frac{34}{123} \right)$$

ϕ is the golden ratio

Result:

$$1.105626940... \times 10^{-52}$$

1.105626940... * 10⁻⁵² result practically equal to the value of Cosmological Constant

$$1.1056 \cdot 10^{-52} \text{ m}^{-2}$$

Alternative representations:

$$\frac{4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) - \phi - \frac{34}{123}}{10^{52}}$$

$$= \frac{1}{10^{52}} \left(-1 - \frac{34}{123} + 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) + 4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}} \right) \right) - 2 \sin(54^\circ)$$

$$\frac{4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) - \phi - \frac{34}{123}}{10^{52}}$$

$$= \frac{1}{10^{52}} \left(-1 + 2 \cos(216^\circ) - \frac{34}{123} + 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) \right) + 4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}} \right) \right)$$

$$\begin{aligned}
& \frac{4\left(1 - 24\left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}}\right)\right) - \left(1 - 24\left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4}\right)\right) - \phi - \frac{34}{123}}{10^{52}} \\
&= \frac{1}{10^{52}} \left(-1 - \frac{34}{123} + 24 \left(\frac{0.0018674^2}{1-0.0018674^2} + \frac{0.0018674^4}{1-0.0018674^4} \right) + \right. \\
&\quad \left. 4 \left(1 - 24 \left(\frac{0.0018674^8}{1-0.0018674^8} + \frac{2 \times 0.0018674^{16}}{1-0.0018674^{16}} \right) \right) + 2 \sin(666^\circ) \right)
\end{aligned}$$

We have also:

$$7 * (((4(((1-24(((0.0018674427^8/(1-0.0018674427^8)+2*0.0018674427^16/(1-0.0018674427^16)))))))))-(((1-24(((0.0018674427^2/(1-0.0018674427^2)+0.0018674427^4/(1-0.0018674427^4))))))))))^5+27$$

Where 7 is a Lucas number

Input interpretation:

$$7 \left(4 \left(1 - 24 \left(\frac{0.0018674427^8}{1-0.0018674427^8} + 2 \times \frac{0.0018674427^{16}}{1-0.0018674427^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1-0.0018674427^2} + \frac{0.0018674427^4}{1-0.0018674427^4} \right) \right) \right)^5 + 27$$

Result:

1728.237293660916446471437056275943959561159893931080735575...

1728.2372936...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j -invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

With regard the previous expression:

$$7 \left(4 \left(1 - 24 \left(\frac{0.0018674427^8}{1 - 0.0018674427^8} + 2 \times \frac{0.0018674427^{16}}{1 - 0.0018674427^{16}} \right) \right) - \left(1 - 24 \left(\frac{0.0018674427^2}{1 - 0.0018674427^2} + \frac{0.0018674427^4}{1 - 0.0018674427^4} \right) \right) \right)^5 + 27$$

With regard the number 27, we have that:

From:

J. Polchinski, *String Theory Vol. II: Superstring Theory and Beyond*, Cambridge University Press, 1998

Table 11.3. *Dimensions and Coxeter numbers for simple Lie algebras.*

	$SU(n)$	$SO(n), n \geq 4$	$Sp(k)$	E_6	E_7	E_8	F_4	G_2
$\dim(\mathfrak{g})$	$n^2 - 1$	$n(n-1)/2$	$2k^2 + k$	78	133	248	52	14
$h(\mathfrak{g})$	n	$n-2$	$k+1$	12	18	30	9	4

pactification of the heterotic string, and so we record without derivation the necessary results.

The first subgroup is

$$E_8 \rightarrow SU(3) \times E_6 . \quad (11.4.23)$$

We have not described E_6 explicitly, but the reader can reproduce this and the decomposition (11.4.24) from the known properties of spinor representations, as well as the further decomposition of the E_6 representations in table 11.4 (exercise 11.5). In simple compactifications of the $E_8 \times E_8$ string, the fermions of the Standard Model can all be thought of as arising from the 248-dimensional adjoint representation of one of the E_8 s. It is therefore interesting to trace the fate of this representation under the successive symmetry breakings. Under $E_8 \rightarrow SU(3) \times E_6$,

$$248 \rightarrow (8, 1) + (1, 78) + (3, 27) + (\bar{3}, \bar{27}) . \quad (11.4.24)$$

That is, the adjoint of E_8 contains the adjoints of the subgroups, with half the remaining 162 generators transforming as a triplet of $SU(3)$ and a complex 27-dimensional representation of E_6 and half as the conjugate of this. Further subgroups are shown in table 11.4. The first three subgroups correspond to successive breaking of E_6 down to the Standard Model group through smaller grand unified groups; the fourth is an alternate breaking pattern.

Practically:

$$E_8 = 8*1 + 1*78 + 3*27 + 3*27 = 8 + 78 + 81 + 81 = 248$$

$$E_8 = 8 \times 1 + 1 \times 78 + 3 \times 27 + 3 \times 27 = 248$$

where there are the 27-dimensional representation of E_6

From the following expression

$$\pi = \frac{9801}{\sqrt{8}} \left(\sum_{k=0}^{\infty} \frac{(4k)!(1103 + 26390k)}{(k!)^4 396^{4k}} \right)^{-1}$$

we obtain:

$$\frac{9801}{\sqrt{8}} * \left[\left(\sum_{k=0}^{0.08333} \frac{(4k)!(1103+26390k)}{(k!)^4 * 396^{(4k)}} \right)^{-1} \right]$$

Where 0.08333 is 1/12

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{0.08333} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 * 396^{4k}}}$$

n! is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801\sqrt{2}}{4412}$$

$$\frac{9801}{\sqrt{8}} * \left[\left(\sum_{k=0}^{0.61803398} \frac{(4k)!(1103+26390k)}{(k!)^4 * 396^{(4k)}} \right)^{-1} \right]$$

Where 0.61803398 is the golden ratio conjugate

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{0.61803398} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 * 396^{4k}}}$$

$n!$ is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801\sqrt{2}}{4412}$$

$$9801/\sqrt{8} * [((\sum (((4k)!(1103+26390k)))/(((k!)^4*396^{(4k)}))^{-1}, k=0..0.937))]$$

We know that α' is the Regge slope (string tension). With regard the Omega mesons, some values are:

$$\omega/\omega_3 \mid 5 + 3 \mid m_{u/d} = 240 - 345 \mid 0.937 - 1.000 \quad \text{and we take 0.937 and obtain:}$$

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{0.937} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 \times 396^{4k}}}$$

$n!$ is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801\sqrt{2}}{4412}$$

$$9801/\sqrt{8} * [((\sum_{k=0}^{1.672e-27} (((4k)!(1103+26390k)))/(((k!)^4*396^{(4k)})))^{-1}]$$

Where 1.672×10^{-27} is the proton mass in kg

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{1.672 \times 10^{-27}} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 \times 396^{4k}}}$$

n! is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801\sqrt{2}}{4412}$$

$$9801/\sqrt{8} * [((\sum_{k=0}^{0.938272} (((4k)!(1103+26390k)))/(((k!)^4*396^{(4k)})))^{-1}]$$

Where 0.938272 is the proton mass in GeV

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{0.938272} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 \times 396^{4k}}}$$

n! is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801 \sqrt{2}}{4412}$$

$$9801/\text{sqrt}8 * [((\text{sum } (((4k)!(1103+26390k)))/(((k!)^4*396^(4k))))^{-1}, k=0..1.1056e-52)]$$

Where $1.1056 \times 10^{-52} \text{ m}^{-2}$ is the Cosmological Constant

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{1.1056 \times 10^{-52}} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 \times 396^{4k}}}$$

n! is the factorial function

Result:

$$\frac{9801}{2206 \sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801 \sqrt{2}}{4412}$$

$$9801/\text{sqrt}8 * [((\text{sum } (((4k)!(1103+26390k)))/(((k!)^4*396^(4k))))^{-1}, k=0..0.0072973525693)]$$

Where 0.0072973525693 is the value of fine-structure constant

Input interpretation:

$$\frac{9801}{\sqrt{8}} \sum_{k=0}^{0.0072973525693} \frac{1}{\frac{(4k)!(1103+26390k)}{(k!)^4 \times 396^{4k}}}$$

n! is the factorial function

Result:

$$\frac{9801}{2206\sqrt{2}} \approx 3.14159$$

$$3.14159 \approx \pi$$

Alternate form:

$$\frac{9801\sqrt{2}}{4412}$$

$$9801/\text{sqrt}8 * [((((((4*x)!(1103+26390*x)))/(((x!)^4*396^(4*x))))^(-1)))] = 3.1426352128607319011295937189855948920944776506105316$$

Input interpretation:

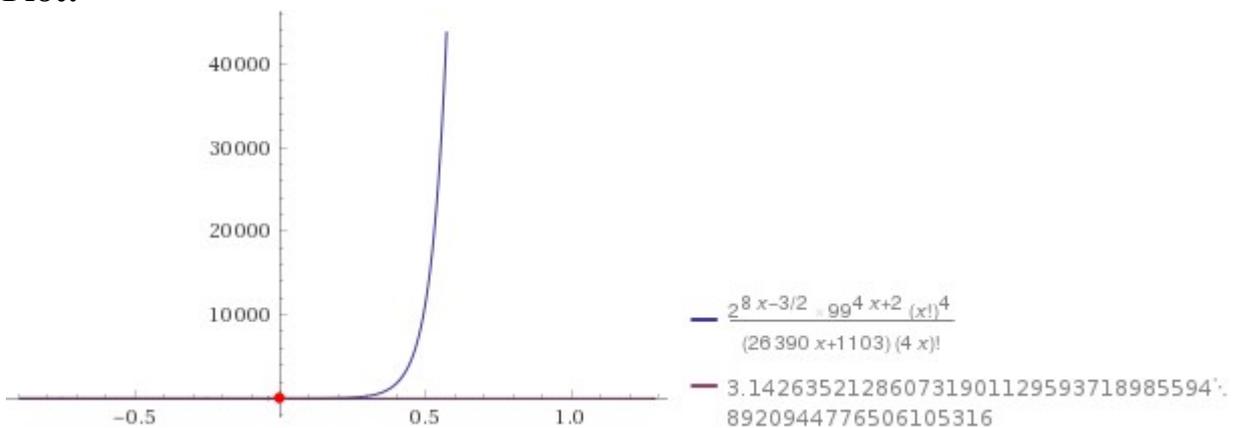
$$\frac{\frac{9801}{\sqrt{8}}}{\frac{(4x)!(1103+26390x)}{(x!)^4 \cdot 396^{4x}}} = 3.1426352128607319011295937189855948920944776506105316$$

n! is the factorial function

Result:

$$\frac{2^{8x-3/2} \times 99^{4x+2} (x!)^4}{(26390x + 1103) (4x)!} = 3.1426352128607319011295937189855948920944776506105316$$

Plot:



Alternate form assuming x is real:

Ramanujan mathematics applied to the Particle Physics

From:

Yukawa - Tomonaga Centennial Symposium

Kyoto Dec. 13 2006

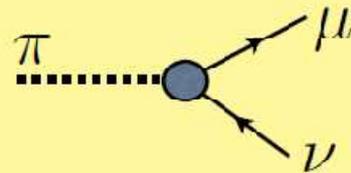
YUKAWA'S PION , LOW-ENERGY QCD and NUCLEAR CHIRAL DYNAMICS

- **ORDER PARAMETER: PION DECAY CONSTANT**

$$\langle 0 | \mathbf{A}_\mu^a(0) | \pi^b(p) \rangle = i \delta^{ab} p_\mu \mathbf{f}_\pi$$

Axial current

$$\mathbf{f}_\pi = 92.4 \text{ MeV}$$



- **SYMMETRY BREAKING SCALE \longleftrightarrow MASS GAP**

$$\Lambda_\chi = 4\pi \mathbf{f}_\pi \sim 1 \text{ GeV}$$

- **PCAC:** $m_\pi^2 \mathbf{f}_\pi^2 = -m_q \langle \bar{\psi}\psi \rangle + \mathcal{O}(m_q^2)$

Gell-Mann - Oakes - Renner Relation

From:

$$\Lambda_\chi = 4\pi \mathbf{f}_\pi \sim 1 \text{ GeV}$$

we obtain:

$$4\pi * 92.4$$

Input:

$$4\pi \times 92.4$$

Result:

1161.132644766787580935792994460104265999273810009039111432...
 1161.13264476...

Adding π to the above expression, we obtain:

$$(4\pi \times 92.4) + \pi$$

Input:

$$4\pi \times 92.4 + \pi$$

Result:

1164.274237420377374174255637843383768883470979408414217253...
 1164.2742....

Note that, from the following Ramanujan's class invariant

$$G_{505} = (\sqrt{5} + 2)^{1/2} \left(\frac{\sqrt{5} + 1}{2} \right)^{1/4} (\sqrt{101} + 10)^{1/4} \\ \times \left(\sqrt{\frac{113 + 5\sqrt{505}}{8}} + \sqrt{\frac{105 + 5\sqrt{505}}{8}} \right)^{1/2} .$$

we obtain:

$$(130\sqrt{5} + 29\sqrt{101}) + \sqrt{169440 + 7540\sqrt{505}} = \left(\sqrt{\frac{113 + 5\sqrt{505}}{8}} + \sqrt{\frac{105 + 5\sqrt{505}}{8}} \right)^3$$

that is: $Q = (G_{505}/G_{101/5})^3 = 1164,2696.$

Thence, from the Ramanujan expression, we can to obtain a value very near to:

$$f_{\pi} = 92.4 \text{ MeV}$$

Indeed:

$$(\sqrt{((113+5\sqrt{505})/8)}+\sqrt{((105+5\sqrt{505})/8)})^3$$

Input:

$$\left(\sqrt{\frac{1}{8}(113+5\sqrt{505})}+\sqrt{\frac{1}{8}(105+5\sqrt{505})}\right)^3$$

Result:

$$\left(\frac{1}{2}\sqrt{\frac{1}{2}(105+5\sqrt{505})}+\frac{1}{2}\sqrt{\frac{1}{2}(113+5\sqrt{505})}\right)^3$$

Decimal approximation:

1164.269601267364667589866974010779128760584499596965142888...

1164.26960126736...

Alternate forms:

$$\left(\frac{5\sqrt{10(21+\sqrt{505})}+25\sqrt{5}+5\sqrt{101}}{8000}\right)^3$$

$$\frac{1}{64}\left(5\sqrt{5}+\sqrt{101}+\sqrt{105-40i}+\sqrt{105+40i}\right)^3$$

$$\sqrt[3]{338881+15080\sqrt{505}+4\sqrt{5(2871007052+127758137\sqrt{505})}}$$

Minimal polynomial:

$$x^8-1355524x^6+400646x^4-1355524x^2+1$$

From which:

$$(\sqrt{((113+5\sqrt{505})/8)}+\sqrt{((105+5\sqrt{505})/8)})^3 * 1/(4\pi)$$

Input:

$$\left(\sqrt{\frac{1}{8}(113+5\sqrt{505})}+\sqrt{\frac{1}{8}(105+5\sqrt{505})}\right)^3 \times \frac{1}{4\pi}$$

Result:

$$\frac{\left(\frac{1}{2}\sqrt{\frac{1}{2}(105+5\sqrt{505})}+\frac{1}{2}\sqrt{\frac{1}{2}(113+5\sqrt{505})}\right)^3}{4\pi}$$

Decimal approximation:

92.64963106666554868222405946213528213380272327498443055873...

92.64963106...

Property:

$$\frac{\left(\frac{1}{2} \sqrt{\frac{1}{2} (105 + 5 \sqrt{505})} + \frac{1}{2} \sqrt{\frac{1}{2} (113 + 5 \sqrt{505})}\right)^3}{4 \pi}$$

is a transcendental number

Alternate forms:

$$\frac{\left(5 \sqrt{10 (21 + \sqrt{505})} + 25 \sqrt{5} + 5 \sqrt{101}\right)^3}{8000 (4 \pi)}$$

$$\frac{(5 \sqrt{5} + \sqrt{101} + \sqrt{105 - 40 i} + \sqrt{105 + 40 i})^3}{256 \pi}$$

$$\frac{\left(5 \sqrt{5} + \sqrt{101} + \sqrt{10 (21 + \sqrt{505})}\right)^3}{256 \pi}$$

From:

$$m_{\pi}^2 f_{\pi}^2 = -m_q \langle \bar{\psi} \psi \rangle + \mathcal{O}(m_q^2)$$

Gell-Mann - Oakes - Renner Relation

we obtain:

$$139.57^2 * 92.4^2$$

Input interpretation:

$$139.57^2 \times 92.4^2$$

Result:

$$1.66313728327824 \times 10^8$$

$$1.66313728327824 * 10^8$$

From which:

$$1/2(((1/11 \ln(139.57^2 * 92.4^2) + 1/12 \ln(139.57^2 * 92.4^2)))) - (34-3)/10^3$$

Where 34 and 3 are Fibonacci numbers

Input interpretation:

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3}$$

$\log(x)$ is the natural logarithm

Result:

1.618151095923245472816460822370504627654253925818529440724...

1.61815109592... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Alternative representations:

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} = \frac{1}{2} \left(\frac{1}{11} \log(a) \log_a(92.4^2 \times 139.57^2) + \frac{1}{12} \log(a) \log_a(92.4^2 \times 139.57^2) \right) - \frac{31}{10^3}$$

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} = \frac{1}{2} \left(\frac{1}{11} \log_e(92.4^2 \times 139.57^2) + \frac{1}{12} \log_e(92.4^2 \times 139.57^2) \right) - \frac{31}{10^3}$$

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} = \frac{1}{2} \left(-\frac{1}{11} \text{Li}_1(1 - 92.4^2 \times 139.57^2) - \frac{1}{12} \text{Li}_1(1 - 92.4^2 \times 139.57^2) \right) - \frac{31}{10^3}$$

Series representations:

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} = -\frac{31}{1000} + \frac{23 \log(1.66314 \times 10^8)}{264} - \frac{23}{264} \sum_{k=1}^{\infty} \frac{(-1)^k e^{-18.9294k}}{k}$$

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} =$$

$$-\frac{31}{1000} + \frac{23}{132} i\pi \left[\frac{\arg(1.66314 \times 10^8 - x)}{2\pi} \right] + \frac{23 \log(x)}{264} -$$

$$\frac{23}{264} \sum_{k=1}^{\infty} \frac{(-1)^k (1.66314 \times 10^8 - x)^k x^{-k}}{k} \text{ for } x < 0$$

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} =$$

$$-\frac{31}{1000} + \frac{23}{264} \left[\frac{\arg(1.66314 \times 10^8 - z_0)}{2\pi} \right] \log\left(\frac{1}{z_0}\right) + \frac{23 \log(z_0)}{264} +$$

$$\frac{23}{264} \left[\frac{\arg(1.66314 \times 10^8 - z_0)}{2\pi} \right] \log(z_0) - \frac{23}{264} \sum_{k=1}^{\infty} \frac{(-1)^k (1.66314 \times 10^8 - z_0)^k z_0^{-k}}{k}$$

Integral representations:

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} =$$

$$-\frac{31}{1000} + \frac{23}{264} \int_1^{1.66314 \times 10^8} \frac{1}{t} dt$$

$$\frac{1}{2} \left(\frac{1}{11} \log(139.57^2 \times 92.4^2) + \frac{1}{12} \log(139.57^2 \times 92.4^2) \right) - \frac{34-3}{10^3} =$$

$$-\frac{31}{1000} + \frac{23}{528 i\pi} \int_{-i\infty+\gamma}^{i\infty+\gamma} \frac{e^{-18.9294 s} \Gamma(-s)^2 \Gamma(1+s)}{\Gamma(1-s)} ds \text{ for } -1 < \gamma < 0$$

Low-Energy Expansion: CHIRAL PERTURBATION THEORY

small parameter:

- $\frac{Q}{4\pi f_\pi} \frac{\text{energy / momentum / pion mass}}{\text{mass gap of order 1 GeV}}$

We have that, for pion mass = 139.57, we obtain:

$$139.57/(4\pi) * 1/92.4$$

Input interpretation:

$$\frac{139.57}{4\pi} \times \frac{1}{92.4}$$

Result:

0.120201598524544545526315513278689553620939030064910749738...

0.1202015985...

Alternative representations:

$$\frac{139.57}{92.4 (4\pi)} = \frac{139.57}{92.4 (720^\circ)}$$

$$\frac{139.57}{92.4 (4\pi)} = \frac{139.57}{92.4 (-4 i \log(-1))}$$

$$\frac{139.57}{92.4 (4\pi)} = \frac{139.57}{92.4 (4 \cos^{-1}(-1))}$$

Series representations:

$$\frac{139.57}{92.4 (4\pi)} = \frac{0.0944061}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{139.57}{92.4 (4\pi)} = \frac{0.188812}{-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\frac{139.57}{92.4 (4\pi)} = \frac{0.377624}{\sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}}}$$

Integral representations:

$$\frac{139.57}{92.4 (4\pi)} = \frac{0.188812}{\int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{139.57}{92.4 (4\pi)} = \frac{0.0944061}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{139.57}{92.4 (4 \pi)} = \frac{0.188812}{\int_0^{\infty} \frac{\sin(t)}{t} dt}$$

and the inverse:

$$1/(139.57 * 1/(4\pi) * 1/92.4)$$

Input interpretation:

$$\frac{1}{139.57 \times \frac{1}{4 \pi} \times \frac{1}{92.4}}$$

Result:

8.31936...

8.31936...

Alternative representations:

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = \frac{1}{\frac{139.57}{92.4 (720^\circ)}}$$

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = \frac{1}{\frac{139.57}{92.4 (-4 i \log(-1))}}$$

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = \frac{1}{\frac{139.57}{92.4 (4 \cos^{-1}(-1))}}$$

Series representations:

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = 10.5925 \sum_{k=0}^{\infty} \frac{(-1)^k}{1 + 2k}$$

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = -5.29627 + 5.29627 \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{1}{\frac{139.57}{92.4 (4 \pi)}} = 2.64813 \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{1}{\frac{139.57}{92.4(4\pi)}} = 5.29627 \int_0^\infty \frac{1}{1+t^2} dt$$

$$\frac{1}{\frac{139.57}{92.4(4\pi)}} = 10.5925 \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{1}{\frac{139.57}{92.4(4\pi)}} = 5.29627 \int_0^\infty \frac{\sin(t)}{t} dt$$

From which we obtain also:

$$10^3 * (((\text{sqrt}(((1/\text{Pi} * 1/((139.57/(4\text{Pi}) * 1/92.4)))))))+(47-2)/10^3)))$$

Where 47 and 2 are Lucas numbers

Input interpretation:

$$10^3 \left(\sqrt{\frac{1}{\pi} \times \frac{1}{\frac{139.57}{4\pi} \times \frac{1}{92.4}}} + \frac{47-2}{10^3} \right)$$

Result:

1672.308684010447443399044902755309661568952777220415753714...

1672.30868401... result practically equal to the rest mass of Omega baryon 1672.45 MeV

Series representations:

$$10^3 \left(\sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + \frac{47-2}{10^3} \right) = 45 + 1000 \sqrt{1.64813} \sum_{k=0}^\infty e^{-0.499643k} \binom{\frac{1}{2}}{k}$$

$$10^3 \left(\sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + \frac{47-2}{10^3} \right) = 45 + 1000 \sqrt{1.64813} \sum_{k=0}^\infty \frac{(-0.606747)^k \binom{-\frac{1}{2}}{k}}{k!}$$

$$10^3 \left(\sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + \frac{47-2}{10^3} \right) = 45 + \frac{500 \sum_{j=0}^\infty \text{Res}_{s=-\frac{1}{2}+j} e^{-0.499643s} \Gamma\left(-\frac{1}{2}-s\right) \Gamma(s)}{\sqrt{\pi}}$$

And:

$$10^3 * (((\sqrt{((1/\pi * 1/((139.57/(4\pi) * 1/92.4))))})) + 89 + 13$$

Input interpretation:

$$10^3 \sqrt{\frac{1}{\pi} \times \frac{1}{\frac{139.57}{4\pi} \times \frac{1}{92.4}}} + 89 + 13$$

Result:

1729.31...

1729.31...

This result is very near to the mass of candidate glueball $f_0(1710)$ meson. Furthermore, 1728 occurs in the algebraic formula for the j-invariant of an elliptic curve. As a consequence, it is sometimes called a Zagier as a pun on the Gross–Zagier theorem. The number 1728 is one less than the Hardy–Ramanujan number 1729

Series representations:

$$10^3 \sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + 89 + 13 = 102 + 1000 \sqrt{1.64813} \sum_{k=0}^{\infty} e^{-0.499643 k} \binom{\frac{1}{2}}{k}$$

$$10^3 \sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + 89 + 13 = 102 + 1000 \sqrt{1.64813} \sum_{k=0}^{\infty} \frac{(-0.606747)^k \left(-\frac{1}{2}\right)_k}{k!}$$

$$10^3 \sqrt{\frac{1}{\frac{139.57\pi}{(4\pi)92.4}}} + 89 + 13 = 102 + \frac{500 \sum_{j=0}^{\infty} \text{Res}_{s=-\frac{1}{2}+j} e^{-0.499643 s} \Gamma\left(-\frac{1}{2} - s\right) \Gamma(s)}{\sqrt{\pi}}$$

We have also:

$$1/10^{52}((((1/8)*1/(139.57*1/(4\pi) *1/92.4)+(76-11)/10^3+7/10^4)))$$

Input interpretation:

$$\frac{1}{10^{52}} \left(\frac{1}{8} \times \frac{1}{139.57 \times \frac{1}{4\pi} \times \frac{1}{92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4} \right)$$

Result:

$$1.10562... \times 10^{-52}$$

1.10562... * 10⁻⁵² result practically equal to the value of Cosmological Constant

$$1.1056 * 10^{-52} \text{ m}^{-2}$$

Alternative representations:

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = \frac{\frac{65}{10^3} + \frac{7}{10^4} + \frac{1}{\frac{8 \times 139.57}{92.4 (720^\circ)}}}{10^{52}}$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = \frac{\frac{65}{10^3} + \frac{7}{10^4} + \frac{1}{\frac{8 \times 139.57}{92.4 (-4 i \log(-1))}}}{10^{52}}$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = \frac{\frac{65}{10^3} + \frac{7}{10^4} + \frac{1}{\frac{8 \times 139.57}{92.4 (4 \cos^{-1}(-1))}}}{10^{52}}$$

Series representations:

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = 6.57 \times 10^{-54} + 1.32407 \times 10^{-52} \sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = -5.96333 \times 10^{-53} + 6.62033 \times 10^{-53} \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = 6.57 \times 10^{-54} + 3.31017 \times 10^{-53} \sum_{k=0}^{\infty} \frac{2^{-k} (-6 + 50k)}{\binom{3k}{k}}$$

Integral representations:

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = 6.57 \times 10^{-54} + 6.62033 \times 10^{-53} \int_0^{\infty} \frac{1}{1+t^2} dt$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = 6.57 \times 10^{-54} + 1.32407 \times 10^{-52} \int_0^1 \sqrt{1-t^2} dt$$

$$\frac{\frac{1}{\frac{8 \times 139.57}{(4\pi)92.4}} + \frac{76-11}{10^3} + \frac{7}{10^4}}{10^{52}} = 6.57 \times 10^{-54} + 6.62033 \times 10^{-53} \int_0^{\infty} \frac{\sin(t)}{t} dt$$

For $Q = 0.284$, we obtain:

$$0.284 / (4\pi) * 1/92.4$$

Input:

$$\frac{0.284}{4\pi} \times \frac{1}{92.4}$$

Result:

0.000244589...

0.000244589...

Alternative representations:

$$\frac{0.284}{92.4 (4\pi)} = \frac{0.284}{92.4 (720^\circ)}$$

$$\frac{0.284}{92.4 (4\pi)} = \frac{0.284}{92.4 (-4i \log(-1))}$$

$$\frac{0.284}{92.4 (4\pi)} = \frac{0.284}{92.4 (4 \cos^{-1}(-1))}$$

Series representations:

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.0001921}{\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k}}$$

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.000384199}{-1 + \sum_{k=1}^{\infty} \frac{2^k}{\binom{2k}{k}}}$$

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.000768398}{\sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}}}$$

Integral representations:

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.000384199}{\int_0^{\infty} \frac{1}{1+t^2} dt}$$

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.0001921}{\int_0^1 \sqrt{1-t^2} dt}$$

$$\frac{0.284}{92.4 (4 \pi)} = \frac{0.000384199}{\int_0^{\infty} \frac{\sin(t)}{t} dt}$$

And:

$$1/(\sqrt{2}) * 1/(((0.284/(4\pi)) * 1/92.4)) + 89 + 3$$

Where 89 and 3 are Fibonacci numbers

Input:

$$\frac{1}{\sqrt{2}} \times \frac{1}{\frac{0.284}{4\pi} \times \frac{1}{92.4}} + 89 + 3$$

Result:

2983.00...

2983.00... result very near to the rest mass of Charmed eta meson 2980.3 MeV

Series representations:

$$\frac{1}{\frac{0.284 \sqrt{2}}{(4 \pi) 92.4}} + 89 + 3 = 92 + \frac{1301.41 \pi}{\sqrt{z_0} \sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}}$$

for not $((z_0 \in \mathbb{R} \text{ and } -\infty < z_0 \leq 0))$

$$\frac{1}{\frac{0.284 \sqrt{2}}{(4 \pi) 92.4}} + 89 + 3 = 92 + \frac{1301.41 \pi}{\exp\left(i \pi \left[\frac{\text{arg}(2-x)}{2 \pi}\right]\right) \sqrt{x} \sum_{k=0}^{\infty} \frac{(-1)^k (2-x)^k x^{-k} \left(-\frac{1}{2}\right)_k}{k!}}$$

for $(x \in \mathbb{R} \text{ and } x < 0)$

$$\frac{1}{\frac{0.284 \sqrt{2}}{(4 \pi) 92.4}} + 89 + 3 = 92 + \frac{1301.41 \pi \left(\frac{1}{z_0}\right)^{-1/2 [\text{arg}(2-z_0)/(2 \pi)]} z_0^{1/2 (-1 - [\text{arg}(2-z_0)/(2 \pi)])}}{\sum_{k=0}^{\infty} \frac{(-1)^k \left(-\frac{1}{2}\right)_k (2-z_0)^k z_0^{-k}}{k!}}$$

Energy Dependent Pion-Nucleus Potential
based on
In-medium Chiral Perturbation Theory

$$f_{\pi}^*(\rho_0) \simeq \underbrace{0.8 f_{\pi}}_{\text{deduced from exp.}} \sim 1 - \underbrace{\frac{\sigma_N}{2 m_{\pi}^2 f_{\pi}^2}}_{\text{theory pred.}} \rho_0 \quad (\sigma_N \simeq 50 \text{ MeV})$$

Thence:

$$0.8 \times 92.4 = 1 - (50 / (2 \times 139.57^2 \times 92.4^2)) \times x$$

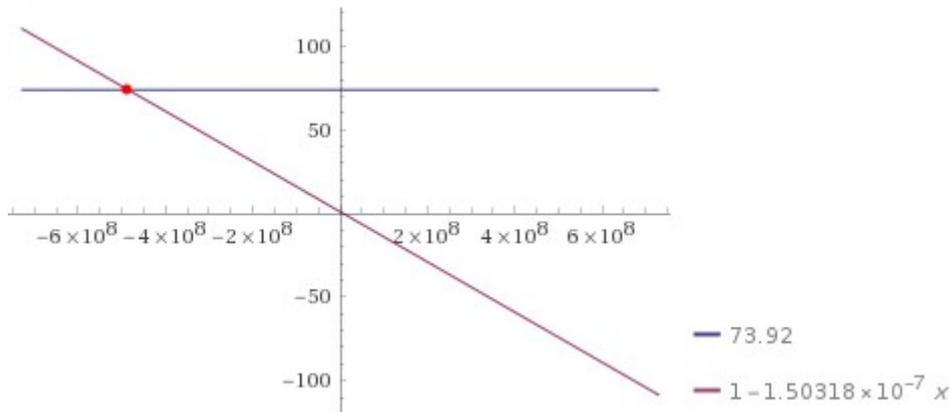
Input interpretation:

$$0.8 \times 92.4 = 1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} x$$

Result:

$$73.92 = 1 - 1.50318 \times 10^{-7} x$$

Plot:



Alternate forms:

$$73.92 = -1.50318 \times 10^{-7} (x - 6.65255 \times 10^6)$$

$$1.50318 \times 10^{-7} x + 72.92 = 0$$

Alternate form assuming x is real:

$$73.92 = 1 - 1.50318 \times 10^{-7} x$$

Solution:

$$x \approx -4.85104 \times 10^8$$

$$-4.85104 \times 10^8$$

We obtain:

$$1 - \frac{50}{(2 \times 139.57^2 \times 92.4^2)} \times (-4.85104 \times 10^8)$$

Input interpretation:

$$1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} (-4.85104 \times 10^8)$$

Result:

73.92001761932164820431119191237110518332470314405893490946...

73.920017619...

And:

$$0.8 \times 92.4$$

Input:

$$0.8 \times 92.4$$

Result:

73.92

73.92

We have also:

$$16((1-(50/(2*139.57^2*92.4^2))*(-4.85104e+8)))+7$$

Where 7 is a Lucas number

Input interpretation:

$$16\left(1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} (-4.85104 \times 10^8)\right) + 7$$

Result:

1189.720281909146371268979070597937682933195250304942958551...

1189.72028.... result practically equal to the rest mass of Sigma baryon 1189.37 MeV

Now, we have that:

$$S = \sigma_N \left(1 - \frac{\vec{\pi}^2}{2f_\pi^2} + \dots\right)$$

SCALAR

We obtain:

$$50(((1-(\pi^2)/(2*92.4^2))))$$

Input:

$$50\left(1 - \frac{\pi^2}{2 \times 92.4^2}\right)$$

Result:

49.9711001...

49.9711001...

Alternative representations:

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 \left(1 - \frac{(180^\circ)^2}{2 \times 92.4^2} \right)$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 \left(1 - \frac{(-i \log(-1))^2}{2 \times 92.4^2} \right)$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 \left(1 - \frac{6 \zeta(2)}{2 \times 92.4^2} \right)$$

Series representations:

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.0468507 \left(\sum_{k=0}^{\infty} \frac{(-1)^k}{1+2k} \right)^2$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.00292817 \left(\sum_{k=0}^{\infty} \frac{2^{-k} (-6+50k)}{\binom{3k}{k}} \right)^2$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.0117127 \sqrt{3}^{-2} \left(\sum_{k=0}^{\infty} \frac{\left(-\frac{1}{3}\right)^k}{1+2k} \right)^2$$

Integral representations:

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.0117127 \left(\int_0^{\infty} \frac{1}{1+t^2} dt \right)^2$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.0468507 \left(\int_0^1 \sqrt{1-t^2} dt \right)^2$$

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) = 50 - 0.0117127 \left(\int_0^{\infty} \frac{\sin(t)}{t} dt \right)^2$$

From the sum of the two formulas, we obtain:

$50(((1-(\pi^2)/(2*92.4^2)))) + 1-(50/(2*139.57^2*92.4^2))*(-4.85104e+8) + \text{golden ratio}$

Input interpretation:

$$50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) + 1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} (-4.85104 \times 10^8) + \phi$$

ϕ is the golden ratio

Result:

125.509...

125.509... result very near to the dilaton mass calculated as a type of Higgs boson: 125 GeV for $T = 0$ and to the Higgs boson mass 125.18 GeV

Dividing the two results, 73.920017619 and 49.9711001, and performing the following calculations, we obtain:

$$1/2 \left[\left(\left(\left(1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} \right) \times (-4.85104 \times 10^8) \right) \right) / \left(\left(\left(\left(1 - \frac{\pi^2}{2 \times 92.4^2} \right) \right) \right) \right) \right]^3$$

Input interpretation:

$$\frac{1}{2} \left(\frac{1 - \frac{50}{2 \times 139.57^2 \times 92.4^2} (-4.85104 \times 10^8)}{50 \left(1 - \frac{\pi^2}{2 \times 92.4^2} \right)} \right)^3$$

Result:

1.618450634959374076296152360895232797644221099033213938520...

1.61845063495... result that is a very good approximation to the value of the golden ratio 1,618033988749...

Now, we have that:

$$\frac{f_\pi^2(T, \rho)}{f_\pi^2(0)} \sim \frac{\langle \bar{q}q \rangle_{T, \rho}}{\langle \bar{q}q \rangle_0} = 1 - \frac{T^2}{8f_\pi^2} - \frac{\sigma_N}{m_\pi^2 f_\pi^2} \rho + \dots$$

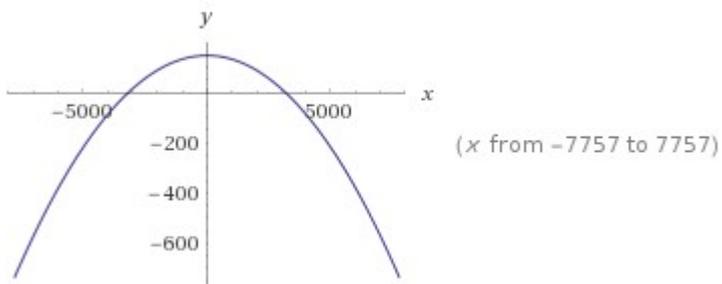
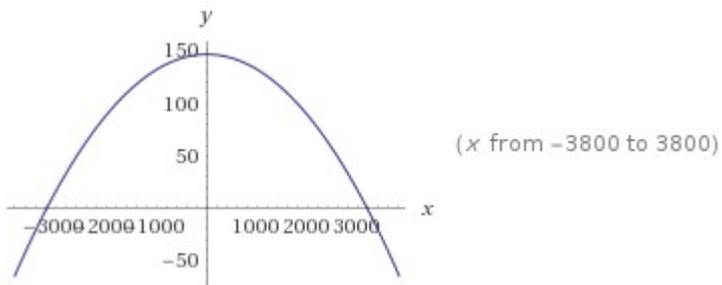
$$1 - \frac{x^2}{8 \times 92.4^2} - \frac{50(-4.85104 \times 10^8)}{139.57^2 \times 92.4^2}$$

Input interpretation:

$$1 - \frac{x^2}{8 \times 92.4^2} - \frac{50(-4.85104 \times 10^8)}{139.57^2 \times 92.4^2}$$

Result:

$$146.84 - 0.0000146408 x^2$$

Plots:**Geometric figure:**

parabola

Alternate forms:

$$-0.0000146408 (x - 3166.94) (x + 3166.94)$$

$$1.22968 \times 10^{-14} (1.19413 \times 10^{16} - 1.19062 \times 10^9 x^2)$$

Roots:

$$x \approx -3166.94$$

$$x \approx 3166.94$$

$$T = 3166.94$$

Polynomial discriminant:

$$\Delta = 0.00859945$$

Properties as a real function:**Domain**

\mathbb{R} (all real numbers)

Range

$$\{y \in \mathbb{R} : y \leq \frac{1\,468\,400\,352\,386\,433}{10\,000\,000\,000\,000}\}$$

Parity

even

\mathbb{R} is the set of real numbers

Derivative:

$$\frac{d}{dx}(146.84 - 0.0000146408 x^2) = -0.0000292817 x$$

Indefinite integral:

$$\int \left(1 - \frac{x^2}{8 \times 92.4^2} - \frac{50(-4.85104 \times 10^8)}{139.57^2 \times 92.4^2} \right) dx = 146.84 x - 4.88028 \times 10^{-6} x^3 + \text{constant}$$

Global maximum:

$$\max\{146.84 - 0.0000146408 x^2\} = \frac{6\,993\,255\,063}{47\,624\,989} \text{ at } x = 0$$

Definite integral after subtraction of diverging parts:

$$\int_0^\infty ((146.84 - 0.0000146408 x^2) - (146.84 - 0.0000146408 x^2)) dx = 0$$

Definite integral area above the axis between the smallest and largest real roots:

$$\int_{-3166.94}^{3166.94} (146.84 - 0.0000146408 x^2) \theta(146.84 - 0.0000146408 x^2) dx = 620\,044.$$

$\theta(x)$ is the Heaviside step function

Definite integral area below the axis between the smallest and largest real roots:

$$\int_{-3166.94}^{3166.94} (146.84 - 0.0000146408 x^2) \theta(-146.84 + 0.0000146408 x^2) dx = -2.16064 \times 10^{-28}$$

$$((((1 - (3166.94^2)/(8 \times 92.4^2) - (50 \times (-4.85104 \times 10^8))/(139.57^2 \times 92.4^2))))))$$

Input interpretation:

$$1 - \frac{3166.94^2}{8 \times 92.4^2} - \frac{50(-4.85104 \times 10^8)}{139.57^2 \times 92.4^2}$$

Result:

-0.00042648082410487696071994017973637347915202225862237574...

-0.00042648082....

From which:

$$-1/((((1-(3166.94^2)/(8*92.4^2))-((50*(-4.85104e+8)))/(((139.57^2*92.4^2)))))))+123$$

Where 123 is a Lucas number

Input interpretation:

$$-\frac{1}{1 - \frac{3166.94^2}{8 \times 92.4^2} - \frac{50(-4.85104 \times 10^8)}{139.57^2 \times 92.4^2}} + 123$$

Result:

2467.771308531535550536019903260575496284363758783973924355...

2467.7713.... result practically equal to the rest mass of charmed Xi baryon 2467.8 MeV

We have that:

$$\sigma_N(Q^2) = \sigma_N - Q^2 \int_{4m_\pi^2}^{\infty} dt \frac{\eta(t)}{t(Q^2 + t)}$$

$$50 \cdot 0.284^2 = 50 - 0.284^2 \cdot \int_{4 \cdot 139.57^2}^{\infty} \frac{1}{x} dx$$

$$50 - 0.284^2 \cdot \int_{4 \cdot 139.57^2}^{1728} \frac{1}{x} dx$$

Input interpretation:

$$50 - 0.284^2 \int_{4 \times 139.57^2}^{1728} \frac{1}{x} dx$$

Result:

$$3.0342 \times 10^9$$

$$3.0342 \cdot 10^9$$

Computation result:

$$50 - 0.284^2 \int_{4 \times 139.57^2}^{1728} \frac{x}{0.284^2} dx = 3.0342 \times 10^9$$

From the integral, we obtain also:

$$\left(\left(\left(50-0.284^2 * \int_{4 \times 139.57^2}^{1728} \frac{1}{0.284^2} x dx\right)\right)\right)^{1/44}$$

Where 139.57 is the Pion meson mass and 1728 is a value in the range of the mass of candidate “glueball” $f_0(1710)$

Input interpretation:

$$\sqrt[44]{50 - 0.284^2 \int_{4 \times 139.57^2}^{1728} \frac{1}{0.284^2} x dx}$$

Result:

1.64248

$$1.64248 \approx \zeta(2) = \frac{\pi^2}{6} = 1.644934 \dots$$

And:

$$\frac{1}{10^{52}} * \left(\left(\left(\left(\left(\left(50-0.284^2 * \int_{4 \times 139.57^2}^{1728} \frac{1}{0.284^2} x dx\right)\right)\right)\right)^{1/44} - \frac{55}{10^2} + \frac{13}{10^3} + \frac{21}{10^5}\right)\right)$$

Where 55, 13 and 21 are Fibonacci numbers

Input interpretation:

$$\frac{1}{10^{52}} \left(\sqrt[44]{50 - 0.284^2 \int_{4 \times 139.57^2}^{1728} \frac{1}{0.284^2} x dx} - \frac{55}{10^2} + \frac{13}{10^3} + \frac{21}{10^5} \right)$$

Result:

1.10569×10^{-52}

$1.10569 * 10^{-52}$ result practically equal to the value of Cosmological Constant

$1.1056 * 10^{-52} \text{ m}^{-2}$

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