

On non-trivial zero point

Toshiro Takami

mmm82889@yahoo.co.jp

Abstract

In the Riemann zeta function, when the value of the nontrivial zero is zero, the value of the real part of the function is negative from 0 to 0.5, but the value of the real part of the function is 0.5 to 1 I found it to be positive. We also found that the positive and negative of the imaginary part also interchanged with the real part 0.5. This tendency is seen as a tendency near the non-trivial zero value, but becomes less and less as it deviates from the non-trivial zero value. We present and discuss the case of four non-trivial zero values. This seems to be an important finding and will be announced here.

1 Introduction

$\zeta(0.0+i14.1347) = -0.479166\dots - 0.0989516\dots i$
 $\zeta(0.1+i14.1347) = -0.367857\dots - 0.0721771\dots i$
 $\zeta(0.2+i14.1347) = -0.264866\dots - 0.0493623\dots i$
 $\zeta(0.3+i14.1347) = -0.169593\dots - 0.0300140\dots i$
 $\zeta(0.4+i14.1347) = -0.0814778\dots - 0.0136953\dots i$
 $\zeta(0.5+i14.1347) = \text{almost zero}$
 $\zeta(0.6+i14.1347) = 0.0753372\dots + 0.0113547\dots i$
 $\zeta(0.7+i14.1347) = 0.144979\dots + 0.0207296\dots i$
 $\zeta(0.8+i14.1347) = 0.209351\dots + 0.0283713\dots i$
 $\zeta(0.9+i14.1347) = 0.268846\dots + 0.0345143\dots i$
 $\zeta(1.0+i14.1347) = 0.323829\dots + 0.0393653\dots i$

 $\zeta(0.0+i21.022) = -0.758769\dots + 0.188304\dots i$
 $\zeta(0.1+i21.022) = -0.568554\dots + 0.138734\dots i$
 $\zeta(0.2+i21.022) = -0.399959\dots + 0.0957785\dots i$
 $\zeta(0.3+i21.022) = -0.250448\dots + 0.0587442\dots i$
 $\zeta(0.4+i21.022) = -0.117787\dots + 0.0269968\dots i$
 $\zeta(0.5+i21.022) = \text{almost zero}$
 $\zeta(0.6+i21.022) = 0.104617\dots - 0.0229066\dots i$

$\zeta(0.7+i21.022)=0.197620\dots - 0.0420713\dots i$
 $\zeta(0.8+i21.022)=0.280344\dots - 0.0579726\dots i$
 $\zeta(0.9+i21.022)=0.353976\dots - 0.0710031\dots i$
 $\zeta(1.0+i21.022)=0.419560\dots - 0.0815165\dots i$

 $\zeta(0.0+i25.0109)=-0.910044\dots - 0.386035\dots i$
 $\zeta(0.1+i25.0109)=-0.678406\dots - 0.276835\dots i$
 $\zeta(0.2+i25.0109)=-0.474749\dots - 0.186231\dots i$
 $\zeta(0.3+i25.0109)=-0.295714\dots - 0.111421\dots i$
 $\zeta(0.4+i25.0109)=-0.138340\dots - 0.0500092\dots i$
 $\zeta(0.5+i25.0109)= \text{almost zero}$
 $\zeta(0.6+i25.0109)=0.121545\dots + 0.0405226\dots i$
 $\zeta(0.7+i25.0109)=0.228375\dots + 0.0728901\dots i$
 $\zeta(0.8+i25.0109)=0.322251\dots + 0.0984346\dots i$
 $\zeta(0.9+i25.0109)=0.404738\dots + 0.118246\dots i$
 $\zeta(1.0+i25.0109)=0.477215\dots + 0.133254\dots i$

 $\zeta(0.0+i30.4249)=-0.798591\dots + 0.602995\dots i$
 $\zeta(0.1+i30.4249)=-0.592313\dots + 0.428177\dots i$
 $\zeta(0.2+i30.4249)=-0.412850\dots + 0.285178\dots i$
 $\zeta(0.3+i30.4249)=-0.256386\dots + 0.168920\dots i$
 $\zeta(0.4+i30.4249)=-0.119683\dots + 0.0750891\dots i$
 $\zeta(0.5+i30.4249)= \text{almost zero}$
 $\zeta(0.6+i30.4249)=0.105056\dots - 0.0593696\dots i$
 $\zeta(0.7+i30.4249)=0.197436\dots - 0.105726\dots i$
 $\zeta(0.8+i30.4249)=0.278863\dots - 0.141265\dots i$
 $\zeta(0.9+i30.4249)=0.350793\dots - 0.167860\dots i$
 $\zeta(1.0+i30.4249)=0.414475\dots - 0.187094\dots i$

 $\zeta(0.0+i32.9351)=-0.824282\dots - 0.704411\dots i$
 $\zeta(0.1+i32.9351)=-0.612478\dots - 0.496080\dots i$
 $\zeta(0.2+i32.9351)=-0.427445\dots - 0.327764\dots i$
 $\zeta(0.3+i32.9351)=-0.265662\dots - 0.192628\dots i$
 $\zeta(0.4+i32.9351)=-0.124073\dots - 0.0849529\dots i$
 $\zeta(0.5+i32.9351)= \text{almost zero}$
 $\zeta(0.6+i32.9351)=0.108767\dots + 0.0663606\dots i$
 $\zeta(0.7+i32.9351)=0.204307\dots + 0.117331\dots i$
 $\zeta(0.8+i32.9351)=0.288316\dots + 0.155737\dots i$
 $\zeta(0.9+i32.9351)=0.362289\dots + 0.183895\dots i$
 $\zeta(1.0+i32.9351)=0.427522\dots + 0.203733\dots i$

 $\zeta(0.0+i37.5862)=-1.47190\dots + 0.522912\dots i$
 $\zeta(0.1+i37.5862)=-1.06819\dots + 0.368755\dots i$
 $\zeta(0.2+i37.5862)=-0.728544\dots + 0.243992\dots i$
 $\zeta(0.3+i37.5862)=-0.442766\dots + 0.143631\dots i$
 $\zeta(0.4+i37.5862)=-0.202307\dots + 0.0634816\dots i$
 $\zeta(0.5+i37.5862)= \text{almost zero}$

$\zeta(0.6+i37.5862)=0.170218\dots - 0.0496243\dots i$
 $\zeta(0.7+i37.5862)=0.313376\dots - 0.0879614\dots i$
 $\zeta(0.8+i37.5862)=0.433743\dots - 0.117013\dots i$
 $\zeta(0.9+i37.5862)=0.534901\dots - 0.138482\dots i$
 $\zeta(1.0+i37.5862)=0.619862\dots - 0.153783\dots i$
 $\zeta(0.0+i40.9187)=-1.20505\dots + 0.318676\dots i$
 $\zeta(0.1+i40.9187)=-0.865813\dots + 0.219703\dots i$
 $\zeta(0.2+i40.9187)=-0.585269\dots + 0.141987\dots i$
 $\zeta(0.3+i40.9187)=-0.352934\dots + 0.0815545\dots i$
 $\zeta(0.4+i40.9187)=-0.160201\dots + 0.0351193\dots i$
 $\zeta(0.5+i40.9187)= \text{almost zero}$
 $\zeta(0.6+i40.9187)=0.133452\dots - 0.0261161\dots i$
 $\zeta(0.7+i40.9187)=0.244929\dots - 0.0449756\dots i$
 $\zeta(0.8+i40.9187)=0.338331\dots - 0.0581042\dots i$
 $\zeta(0.9+i40.9187)=0.416856\dots - 0.0667242\dots i$
 $\zeta(1.0+i40.9187)=0.483130\dots - 0.0718298\dots i$

 $\zeta(0.0+i43.3271)=-1.08852\dots - 1.10438\dots i$
 $\zeta(0.1+i43.3271)=-0.801141\dots - 0.767192\dots i$
 $\zeta(0.2+i43.3271)=-0.553912\dots - 0.500228\dots i$
 $\zeta(0.3+i43.3271)=-0.341124\dots - 0.290258\dots i$
 $\zeta(0.4+i43.3271)=-0.157892\dots - 0.126453\dots i$
 $\zeta(0.5+i43.3271)= \text{almost zero}$
 $\zeta(0.6+i43.3271)=0.136045\dots + 0.0964527\dots i$
 $\zeta(0.7+i43.3271)=0.253401\dots + 0.168693\dots i$
 $\zeta(0.8+i43.3271)=0.354666\dots + 0.221574\dots i$
 $\zeta(0.9+i43.3271)=0.442092\dots + 0.259018\dots i$
 $\zeta(1.0+i43.3271)=0.517610\dots + 0.284215\dots i$

 $\zeta(0.0+i48.0052)=-0.669182\dots + 1.21491\dots i$
 $\zeta(0.1+i48.0052)=-0.507917\dots + 0.838705\dots i$
 $\zeta(0.2+i48.0052)=-0.361562\dots + 0.543569\dots i$
 $\zeta(0.3+i48.0052)=-0.228874\dots + 0.313598\dots i$
 $\zeta(0.4+i48.0052)=-0.108693\dots + 0.135903\dots i$
 $\zeta(0.5+i48.0052)= \text{almost zero}$
 $\zeta(0.6+i48.0052)=0.0983814\dots - 0.102400\dots i$
 $\zeta(0.7+i48.0052)=0.187206\dots - 0.178272\dots i$
 $\zeta(0.8+i48.0052)=0.267390\dots - 0.233070\dots i$
 $\zeta(0.9+i48.0052)=0.339725\dots - 0.271237\dots i$
 $\zeta(1.0+i48.0052)=0.404942\dots - 0.296346\dots i$

 $\zeta(0.0+i49.7738)=-1.02525\dots - 0.754450\dots i$
 $\zeta(0.1+i49.7738)=-0.737840\dots - 0.509449\dots i$
 $\zeta(0.2+i49.7738)=-0.499948\dots - 0.322739\dots i$
 $\zeta(0.3+i49.7738)=-0.302406\dots - 0.181875\dots i$
 $\zeta(0.4+i49.7738)=-0.137767\dots - 0.0769389\dots i$
 $\zeta(0.5+i49.7738)= \text{almost zero}$

$\zeta(0.6+i49.7738)=0.115868\dots + 0.0550838\dots i$
 $\zeta(0.7+i49.7738)=0.213762\dots + 0.0933995\dots i$
 $\zeta(0.8+i49.7738)=0.296939\dots + 0.118830\dots i$
 $\zeta(0.9+i49.7738)=0.368023\dots + 0.134469\dots i$
 $\zeta(1.0+i49.7738)=0.429146\dots + 0.142746\dots i$

 $\zeta(0.0+i52.9703)=-2.05299\dots - 0.658562\dots i$
 $\zeta(0.1+i52.9703)=-1.45894\dots - 0.451769\dots i$
 $\zeta(0.2+i52.9703)=-0.975066\dots - 0.291186\dots i$
 $\zeta(0.3+i52.9703)=-0.581125\dots - 0.167209\dots i$
 $\zeta(0.4+i52.9703)=-0.260593\dots - 0.0721938\dots i$
 $\zeta(0.5+i52.9703)= \text{almost zero}$
 $\zeta(0.6+i52.9703)=0.211697\dots + 0.0540653\dots i$
 $\zeta(0.7+i52.9703)=0.383441\dots + 0.0940056\dots i$
 $\zeta(0.8+i52.9703)=0.522579\dots + 0.122832\dots i$
 $\zeta(0.9+i52.9703)=0.635104\dots + 0.142974\dots i$
 $\zeta(1.0+i52.9703)=0.725907\dots + 0.156360\dots i$

 $\zeta(0.0+i56.4462)=-1.95825\dots + 0.879911\dots i$
 $\zeta(0.1+i56.4462)=-1.38812\dots + 0.603511\dots i$
 $\zeta(0.2+i56.4462)=-0.925780\dots + 0.388819\dots i$
 $\zeta(0.3+i56.4462)=-0.550806\dots + 0.223096\dots i$
 $\zeta(0.4+i56.4462)=-0.246681\dots + 0.0961633\dots i$
 $\zeta(0.5+i56.4462)= \text{almost zero}$
 $\zeta(0.6+i56.4462)=0.199940\dots - 0.0721920\dots i$
 $\zeta(0.7+i56.4462)=0.362028\dots - 0.125260\dots i$
 $\zeta(0.8+i56.4462)=0.493332\dots - 0.163419\dots i$
 $\zeta(0.9+i56.4462)=0.599622\dots - 0.189938\dots i$
 $\zeta(1.0+i56.4462)=0.685579\dots - 0.207412\dots i$

 $\zeta(0.0+i59.347)=-1.09043\dots + 0.765162\dots i$
 $\zeta(0.1+i59.347)=-0.772384\dots + 0.506224\dots i$
 $\zeta(0.2+i59.347)=-0.516032\dots + 0.313925\dots i$
 $\zeta(0.3+i59.347)=-0.308319\dots + 0.172993\dots i$
 $\zeta(0.4+i59.347)=-0.138998\dots + 0.0714540\dots i$
 $\zeta(0.5+i59.347)= \text{almost zero}$
 $\zeta(0.6+i59.347)=0.114907\dots - 0.0488387\dots i$
 $\zeta(0.7+i59.347)=0.210750\dots - 0.0805723\dots i$
 $\zeta(0.8+i59.347)=0.291384\dots - 0.0996520\dots i$
 $\zeta(0.9+i59.347)=0.359856\dots - 0.109467\dots i$
 $\zeta(1.0+i59.347)=0.418555\dots - 0.112618\dots i$

 $\zeta(0.0+i60.8318)=-0.390164\dots - 1.53661\dots i$
 $\zeta(0.1+i60.8318)=-0.329826\dots - 1.04894\dots i$
 $\zeta(0.2+i60.8318)=-0.255157\dots - 0.672486\dots i$
 $\zeta(0.3+i60.8318)=-0.172476\dots - 0.383917\dots i$
 $\zeta(0.4+i60.8318)=-0.0863522\dots - 0.164672\dots i$

$\zeta(0.5+i60.8318)$ = almost zero
 $\zeta(0.6+i60.8318)=0.0842443\dots + 0.121898\dots i$
 $\zeta(0.7+i60.8318)=0.164975\dots + 0.210292\dots i$
 $\zeta(0.8+i60.8318)=0.241219\dots + 0.272601\dots i$
 $\zeta(0.9+i60.8318)=0.312443\dots + 0.314688\dots i$
 $\zeta(1.0+i60.8318)=0.378407\dots + 0.341191\dots i$

$\zeta(0.0+i65.1125)=-1.27313\dots + 1.77458\dots i$
 $\zeta(0.1+i65.1125)=-0.929355\dots + 1.20332\dots i$
 $\zeta(0.2+i65.1125)=-0.637674\dots + 0.766403\dots i$
 $\zeta(0.3+i65.1125)=-0.389926\dots + 0.434704\dots i$
 $\zeta(0.4+i65.1125)=-0.179292\dots + 0.185253\dots i$
 $\zeta(0.5+i65.1125)$ = almost zero
 $\zeta(0.6+i65.1125)=0.152527\dots - 0.135550\dots i$
 $\zeta(0.7+i65.1125)=0.282521\dots - 0.232418\dots i$
 $\zeta(0.8+i65.1125)=0.393305\dots - 0.299515\dots i$
 $\zeta(0.9+i65.1125)=0.487740\dots - 0.343780\dots i$
 $\zeta(1.0+i65.1125)=0.568250\dots - 0.370653\dots i$

$\zeta(0.0+i67.0798)=-1.72455\dots - 0.191859\dots i$
 $\zeta(0.1+i67.0798)=-1.19508\dots - 0.121962\dots i$
 $\zeta(0.2+i67.0798)=-0.780696\dots - 0.0722288\dots i$
 $\zeta(0.3+i67.0798)=-0.455914\dots - 0.0377238\dots i$
 $\zeta(0.4+i67.0798)=-0.200847\dots - 0.0146334\dots i$
 $\zeta(0.5+i67.0798)$ = almost zero
 $\zeta(0.6+i67.0798)=0.158698\dots + 0.00837864\dots i$
 $\zeta(0.7+i67.0798)=0.284629\dots + 0.0122881\dots i$
 $\zeta(0.8+i67.0798)=0.385089\dots + 0.0130277\dots i$
 $\zeta(0.9+i67.0798)=0.465744\dots + 0.0115965\dots i$
 $\zeta(1.0+i67.0798)=0.530986\dots + 0.00874614\dots i$

$\zeta(0.0+i370.0509)=2.79835\dots - 6.09129\dots i$
 $\zeta(0.1+i370.0509)=1.35910\dots - 3.86114\dots i$
 $\zeta(0.2+i370.0509)=0.566252\dots - 2.30540\dots i$
 $\zeta(0.3+i370.0509)=0.171720\dots - 1.22933\dots i$
 $\zeta(0.4+i370.0509)=0.0165890\dots - 0.493951\dots$
 $\zeta(0.5+i370.0509)$ = almost zero
 $\zeta(0.6+i370.0509)=0.0591164\dots + 0.323433\dots i$
 $\zeta(0.7+i370.0509)=0.154958\dots + 0.527039\dots i$
 $\zeta(0.8+i370.0509)=0.264407\dots + 0.647001\dots i$
 $\zeta(0.9+i370.0509)=0.374114\dots + 0.709130\dots i$
 $\zeta(1.0+i370.0509)=0.476879\dots + 0.731808\dots i$

$\zeta(0.0+i373.0619)=3.13761\dots + 5.44965\dots i$
 $\zeta(0.1+i373.0619)=1.54354\dots + 3.44413\dots i$
 $\zeta(0.2+i373.0619)=0.657466\dots + 2.05097\dots i$

$\zeta(0.3+i373.0619)=0.209954\dots + 1.09115\dots i$
 $\zeta(0.4+i373.0619)=0.0276074\dots + 0.437580\dots i$
 $\zeta(0.5+i373.0619)= \text{almost zero}$
 $\zeta(0.6+i373.0619)=0.0572810\dots - 0.285763\dots i$
 $\zeta(0.7+i373.0619)=0.156750\dots - 0.465279\dots i$
 $\zeta(0.8+i373.0619)=0.272383\dots - 0.570942\dots i$
 $\zeta(0.9+i373.0619)=0.389127\dots - 0.625732\dots i$
 $\zeta(1.0+i373.0619)=0.498766\dots - 0.645933\dots i$

 $\zeta(0.0+i373.8649)=-4.69228\dots - 1.11954\dots i$
 $\zeta(0.1+i373.8649)=-2.81909\dots - 0.575812\dots i$
 $\zeta(0.2+i373.8649)=-1.61278\dots - 0.260713\dots i$
 $\zeta(0.3+i373.8649)=-0.834547\dots - 0.0932396\dots i$
 $\zeta(0.4+i373.8649)=-0.330066\dots - 0.0185496\dots i$
 $\zeta(0.5+i373.8649)= \text{almost zero}$
 $\zeta(0.6+i373.8649)=0.219307\dots - 0.0131603\dots i$
 $\zeta(0.7+i373.8649)=0.368433\dots - 0.0425648\dots i$
 $\zeta(0.8+i373.8649)=0.473100\dots - 0.0782708\dots i$
 $\zeta(0.9+i373.8649)=0.549508\dots - 0.114299\dots i$
 $\zeta(1.0+i373.8649)=0.607790\dots - 0.147249\dots i$

 $\zeta(0.0+i375.8259)=-0.218830\dots + 3.12037\dots i$
 $\zeta(0.1+i375.8259)=-0.266981\dots + 1.75691\dots i$
 $\zeta(0.2+i375.8259)=-0.241676\dots + 0.928633\dots i$
 $\zeta(0.3+i375.8259)=-0.176271\dots + 0.436800\dots i$
 $\zeta(0.4+i375.8259)=-0.0915171\dots + 0.154224\dots i$
 $\zeta(0.5+i375.8259)= \text{almost zero}$
 $\zeta(0.6+i375.8259)=0.0908625\dots - 0.0770281\dots i$
 $\zeta(0.7+i375.8259)=0.177045\dots - 0.108828\dots i$
 $\zeta(0.8+i375.8259)=0.256527\dots - 0.115212\dots i$
 $\zeta(0.9+i375.8259)=0.328557\dots - 0.108237\dots i$
 $\zeta(1.0+i375.8259)=0.393117\dots - 0.0950879\dots i$

 $\zeta(0.0+i376.3241)=1.34696\dots - 3.00200\dots i$
 $\zeta(0.1+i376.3241)=0.589113\dots - 1.77668\dots i$
 $\zeta(0.2+i376.3241)=0.196119\dots - 0.992622\dots i$
 $\zeta(0.3+i376.3241)=0.0220603\dots - 0.496568\dots i$
 $\zeta(0.4+i376.3241)=-0.0244584\dots - 0.187743\dots i$
 $\zeta(0.5+i376.3241)= \text{almost zero}$
 $\zeta(0.6+i376.3241)=0.0609312\dots + 0.109993\dots i$
 $\zeta(0.7+i376.3241)=0.137822\dots + 0.170510\dots i$
 $\zeta(0.8+i376.3241)=0.218802\dots + 0.199953\dots i$
 $\zeta(0.9+i376.3241)=0.297363\dots + 0.210233\dots i$
 $\zeta(1.0+i376.3241)=0.370234\dots + 0.209009\dots i$

 $\zeta(0.0+i378.4367)=-7.46232\dots - 0.0986345\dots i$
 $\zeta(0.1+i378.4367)=-4.60008\dots - 0.101930\dots i$

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zeta(0.2+i378.4367)=-2.68900... - 0.0872539... i
zeta(0.3+i378.4367)=-1.41405... - 0.0619916... i
zeta(0.4+i378.4367)=-0.564659... - 0.0316043... i
zeta(0.5+i378.4367)= almost zero
zeta(0.6+i378.4367)=0.374144... + 0.0305809... i
zeta(0.7+i378.4367)=0.620883... + 0.0583442... i
zeta(0.8+i378.4367)=0.782475... + 0.0825702... i
zeta(0.9+i378.4367)=0.887243... + 0.102944... i
zeta(1.0+i378.4367)=0.954172... + 0.119477... i
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key words

Riemann zeta function, non-trivial zero point,