¿ What is a Strange Attractor ?

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abstract
This note presents a Strange Attractor

Introduction

Strange Attractor: an equation or fractal set representing a complex pattern of behaviour in a chaotic system.

- Lorenz system: $\frac{dx}{dt}=\sigma(y-x),\frac{dy}{dt}=rx-y-xz,\frac{dz}{dt}=xy-bz$.

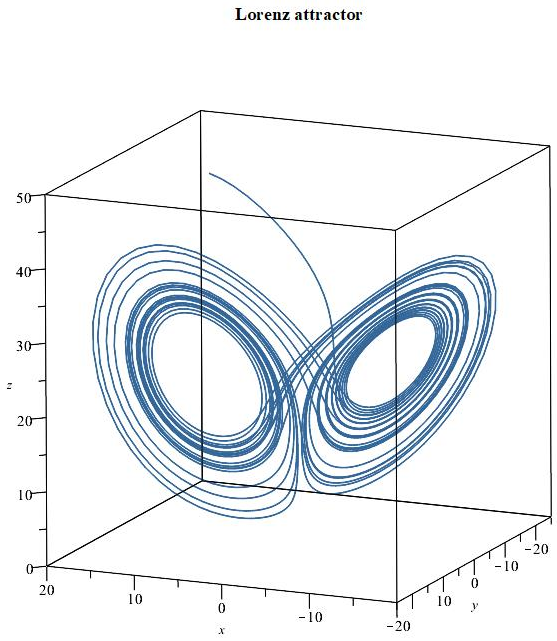

Fig.1: $\sigma=10,b=8/3,r=24.7$.

Strange Attractor

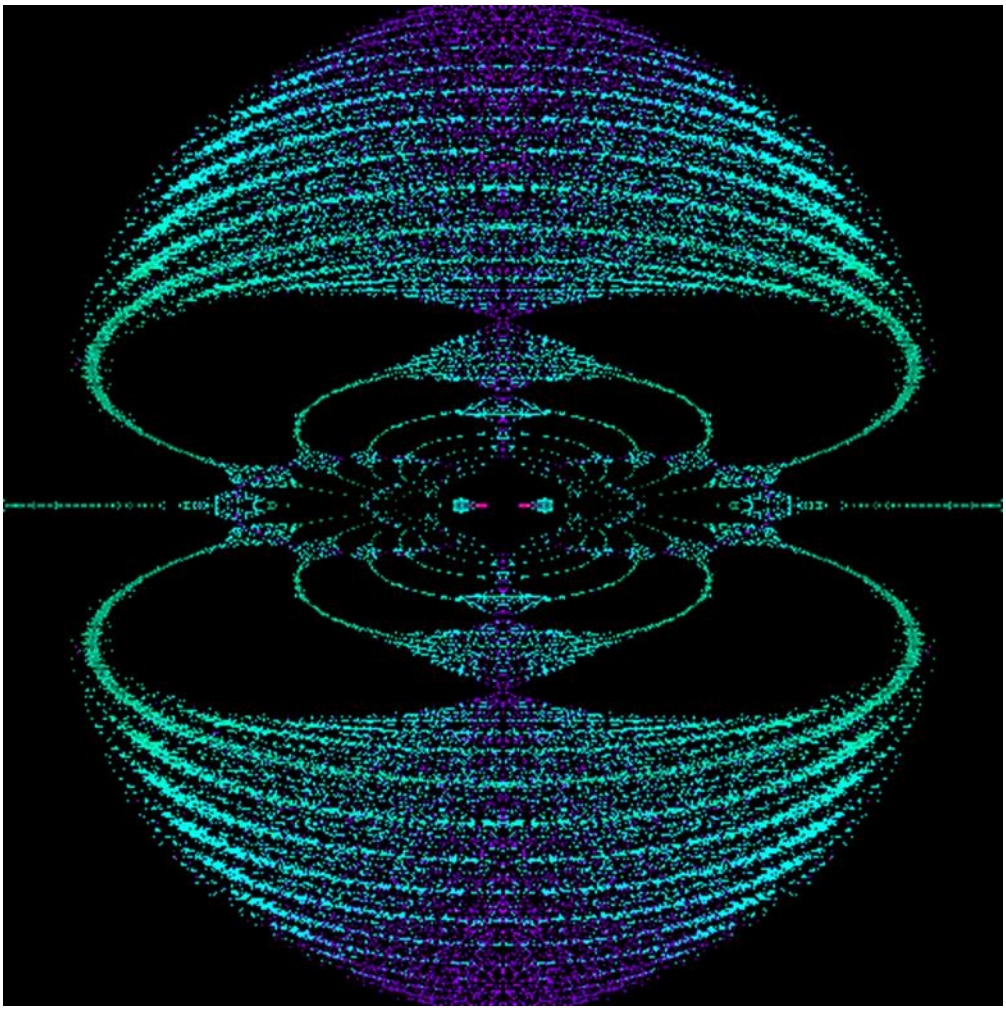

Fig. 2

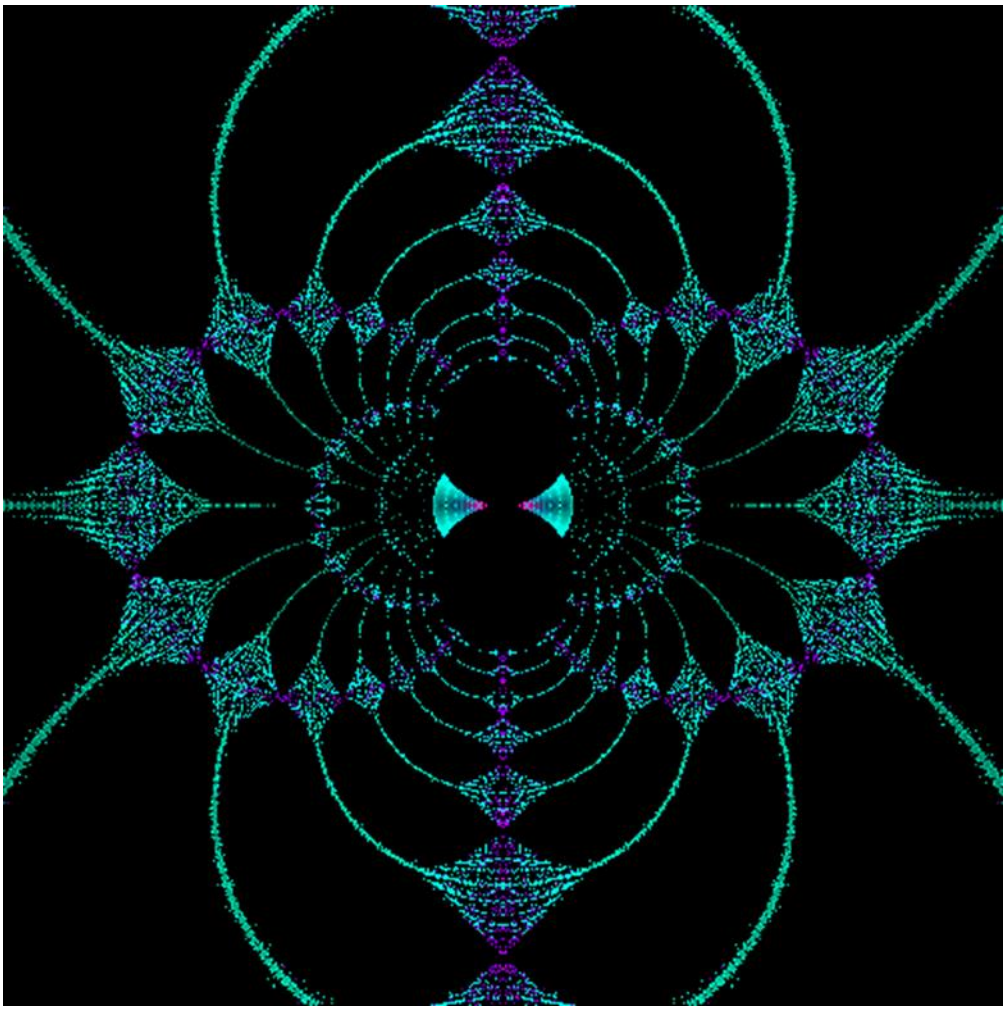

Fig. 3.

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