Proof of the Last Theorem of Fermat

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1]	Definition of the Last Theorem of Fermat	
.	Definition of the East Theorem of Fermat	
Defini	tion: $x^n + y^n \neq z^n$, where $x \in \mathbb{N}$, $y \in \mathbb{N}$, $z \in \mathbb{N}$, $n \in \mathbb{N}$, $n > 2$.	
9	Almonithms for Droof by controliction	
2	Algorithm for Proof by contradiction	
2.1	Detailing the Original Formula	
	Detaining the Original Formula	
Let's:		(4)
	$x^n + y^n = z^n.$	(1)
Let's:		
	y < x < z.	(2)
m.		()
Then:	n , n (, $\setminus n$	(0)
	$x^n + y^n = (x + y_n)^n,$	(3)
where:	:	
	$y_n < y$.	(4)

2.2 Original and New Terms of the Formula for n=2

Consider the expressions (1) and (3) for n = 2:

$$x^{2} + y^{2} = z_{2}^{2} = (x + y_{2})^{2}.$$
 (5)

Let's open the brackets in expression (5):

$$y^2 = 2x \cdot y_2 + y_2^2. (6)$$

Let's express x from expression (6):

$$x = \frac{y^2 - y_2^2}{2y_2}. (7)$$

Substitute (7) into (5):

$$\left(\frac{y^2 - y_2^2}{2y_2}\right)^2 + y^2 = \left(\frac{y^2 + y_2^2}{2y_2}\right)^2 = z_2^2.$$
(8)

Let's express z_2 from expression (8):

$$z_2 = \frac{y^2 + y_2^2}{2y_2}. (9)$$

2.3 Conclusion 1

Let's explain the value of z_2 for given x and y, where $x \in \mathbb{N}$ and $y \in \mathbb{N}$. For this let's represent expression (6) as the following expression:

$$y^2 = y_2(2x + y_2). (10)$$

Let's represent the value y^2 under the conditions $y_2 \notin \mathbb{N}$ and $(2x) \in \mathbb{N}$. Let's:

$$y_2 = \frac{l}{m}$$
, where $l \neq p \cdot m$, $l \in \mathbb{N}$, $p \in \mathbb{N}$, $m \in \mathbb{N}$. (11)

Substitute (11) into (10):

$$y^2 = \frac{l(2x \cdot m + l)}{m^2}. (12)$$

Let's transform expression (12), translating m^2 to the left side of the expression:

$$(m \cdot y)^2 = l(2x \cdot m + l). \tag{13}$$

But because of condition (11), the right-hand side of expression (13) can not be a multiple of m. Therefore, in the expression (10) $y \in \mathbb{N}$ only in the case when $y_2 \in \mathbb{N}$. Then $z_2 = (x + y_2) \in \mathbb{N}$. Conclusion 1: Expression (1) will be true if $z_2 \in \mathbb{N}$ for $x \in \mathbb{N}$ and $y \in \mathbb{N}$ in the expression (5).

2.4 Detailing the Formula (5)

Let's consider in detail the values of y, x and z_2 in expression (5), taking into account <u>Conclusion 1</u>. Expression (5) has a number of solutions, but there are patterns that can be determined:

2.4.1 Definition of Parity x

Let's represent solutions of expression (5) in natural numbers with allowance for condition (2):

$$3^2 + 4^2 = 5^2 = (4+1)^2$$
, where $y_2 = 1$ (14)

and the following derivatives of expression (14):

$$(3y_2)^2 + (4y_2)^2 = (4y_2 + y_2)^2$$
, where $y_2 \ge 2$ (15)

$$(3+2n)^2 + \left(\sum_{n=1}^{n+1} 4n\right)^2 = \left(1 + \sum_{n=1}^{n+1} 4n\right)^2, \quad \text{where} \quad n \in \mathbb{N}, \quad y_2 = 1$$
 (16)

$$((3+2n)y_2)^2 + \left(\left(\sum_{n=1}^{n+1} 4n\right)y_2\right)^2 = \left(\left(1 + \sum_{n=1}^{n+1} 4n\right)y_2\right)^2, \quad \text{where} \quad n \in \mathbb{N}, \quad y_2 \ge 2$$
 (17)

It follows from expressions (14), (15), (16), (17) that the larger term x^2 of the expression (5) will always be an even number.

Then:

$$x - \text{always an even number.}$$
 (18)

2.4.2 Definition of Additional Terms of Formula (5)

Let's represent expression (5) as following expression:

$$(y_2x_o)^2 + (y_2y_o)^2 = (y_2z_{2o})^2 = (y_2x_o + y_2)^2$$
, where $y_o \in \mathbb{N}$, $x_o \in \mathbb{N}$, $z_{2o} \in \mathbb{N}$. (19)

In the expression (19) $y_o \ge 3$, $z_{2o} = (x_o + 1)$ – always odd numbers (see the (14) and (17)). (20)

2.4.3 New Expressions for the Terms of Formula (5)

Substitute (7) and (9) into (19) and transform the expression by representing $y = y_2 y_0$:

$$\left(\frac{y_2^2 y_o^2 - y_2^2}{2y_2}\right)^2 + (y_2 y_o)^2 = \left(\frac{y_2^2 y_o^2 + y_2^2}{2y_2}\right)^2.$$
(21)

Let's make visible cuts in the expression (21):

$$\frac{y_2^2(y_o^2-1)^2}{4} + (y_2y_o)^2 = \frac{y_2^2(y_o^2+1)^2}{4}. (22)$$

Let's derive new expressions for x and z_2 from the expression (22):

$$x = \frac{y_2(y_o^2 - 1)}{2},\tag{23}$$

$$z_2 = \frac{y_2(y_o^2 + 1)}{2}. (24)$$

2.5 Transformation of the Original Formula

If expression (1) is true, then:

$$x < z < z_2. \tag{25}$$

Then:

$$y_2 \ge 2. \tag{26}$$

If expression (1) is true, then taking into account <u>Conclusion 1</u>, it can be represented as follows:

$$x^{n} + y^{n} = (z_{2} - k)^{n} = ((x + y_{2}) - k)^{n}, \text{ where } k \in \mathbb{N}, k < y_{2}.$$
 (27)

Substitute (23), (24) and the value of y from expression (19) into (27):

$$\left(\frac{y_2(y_o^2-1)}{2}\right)^n + (y_2y_o)^n = \left(\frac{y_2(y_o^2+1)}{2} - k\right)^n.$$
(28)

From condition (26) it follows that expression (28) can be represented as the following expression:

$$y_2^n \left(\left(\frac{y_o^2 - 1}{2} \right)^n + y_o^n \right) = \left(\frac{y_2(y_o^2 + 1)}{2} - k \right)^n. \tag{29}$$

Let's:

$$\left(\left(\frac{y_o^2 - 1}{2}\right)^n + y_o^n\right) = w, \quad \text{where} \quad w \in \mathbb{N}.$$
(30)

2.6 Proof of the Theorem

Let's transform expression (29), taking into account expression (30):

$$y_2^n w = z^n = \left(\frac{y_2(y_o^2 + 1)}{2} - k\right)^n. (31)$$

Let's take y_2^n out of the brackets in the right side of expression (31):

$$y_2^n w = z^n = y_2^n \left(\frac{y_o^2 + 1}{2} - \frac{k}{y_2}\right)^n = y_2^n v^n.$$
(32)

According to the conditions (20) and (27):

$$v \notin \mathbb{N}.$$
 (33)

Then:

$$w \neq v^n \quad \text{or} \quad \frac{z}{y_2} \neq v, \quad \text{where} \quad v \in \mathbb{N}, \quad n > 2.$$
 (34)

Then the expression (32) for natural numbers can be represented as the following expression:

$$y_2^n w = z^n \neq y_2^n v^n. \tag{35}$$

But expression (35) can be represented as the following expression:

$$z^n = y_2^n w = y_2^n + (y_2^n f) = y_2^n (1+f), \text{ where } f \in \mathbb{N}, w = 1+f.$$
 (36)

According to the conditions (36):

$$y_2^n f = z^n - y_2^n = (z - y_2)(z^{n-1} + z^{n-2}y_2 + \dots + z \cdot y_2^{n-2} + y_2^{n-1}).$$
(37)

But according to the expression (34) the right-hand side of expression (37) can not be a multiple of y_2 :

$$y_2^n f \neq z^n - y_2^n = (z - y_2)(z^{n-1} + z^{n-2}y_2 + \dots + z \cdot y_2^{n-2} + y_2^{n-1}).$$
 (38)

If condition (34) is true, then:

$$y_2^n w \neq z^n. (39)$$

According to the conditions (27), (28), (29), (30), (31):

$$x^{n} + y^{n} = \left(\frac{y_{2}(y_{o}^{2} - 1)}{2}\right)^{n} + (y_{2}y_{o})^{n} \neq \left(\frac{y_{2}(y_{o}^{2} + 1)}{2} - k\right)^{n} = z^{n}.$$
 (40)

Then:

$$x^{n} + y^{n} \neq (z_{2} - k)^{n} = z^{n}, \text{ for } n > 2.$$
 (41)

The Last Theorem of Fermat is proved.

Publications: http://samlib.ru/editors/b/bezymjannyj_a/w3.shtml