

Title: Formula to find prime numbers and composite numbers with termination 7  
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**Abstract:** The prime numbers greater than 5 have 4 terminations in their unit to infinity (1,3,7,9) and the composite numbers divisible by numbers greater than 3 have 5 terminations in their unit to infinity, these are (1,3,5,7,9). This paper develops an expression to calculate the prime numbers and composite numbers with ending 7.

**Keywords:** Prime numbers, composite numbers.

## Introduction

The study of the prime numbers is wonderful, But to understand them, first study the composite numbers, in the absence of an expression that involves all of them I have investigated and I have discovered a brilliant expression that contains all the prime numbers greater than 3 and all composite number that are not divisible by 2 and by 3. This expression comes from investigating first how they are distributed the composite numbers with termination 7, this allowed me to explore its order and understand its mechanism. The expression of the prime numbers with termination 7 is its result. This paper has 8 demonstrations.

## Theorem 1

Numbers with termination 7. These numbers are interleaved between prime numbers greater than 3 and composite numbers divisible by numbers greater than 3. These are distributed in two well-known sequences.

### Numbers with termination 7 within the sequence $\beta$

$$\beta = (6 * n \pm 1)$$

$$\beta_a = (6 * n + 1) = 7, 13, 19, 25, 31, 37, 43, 49, 55, 61, 67, 73, 79, 85, \dots$$

$$\beta_b = (6 * n - 1) = 5, 11, 17, 23, 29, 35, 41, 47, 53, 59, 65, 71, 77, 83, 89, \dots$$

Within the beta sequence we find composite numbers and prime numbers. To be able to locate only the numbers that end with 7 we will go to the next point (**Theorem 2**)

## Theorem 2

At point A we will look for numbers with ending 7 within the sequence  $\beta_b = (6 * n - 1)$

At point B we will look for composite numbers with ending 7 within the sequence  $\beta_b = (6 * n - 1)$

$$\beta_b = (6 * n - 1) = 5, 11, 17, 23, 29, 35, 41, 47, 53, 59, 65, 71, 77, 83, 89 \dots\dots$$

$n > 0$

Reference [A007528](#) (The On-line Enciclopedia of integers sequences)

### A) Formula for numbers with termination 7 within the sequence $\beta_b$

$$N_{(b)t7} = (30 * n + 17)$$

$N_{(b)t7}$  = numbers with termination 7 within the sequence  $\beta_b$

$$N_{(b)t7} = 17, 47, 77, 107, 137, 167, 197, 227, 257, 287, 317, 347, 377, 407, \dots\dots$$

$n \geq 0$

Reference [A128468](#) (The On-line Enciclopedia of integers sequences)

## Demonstration 1

### B) Formula for composite numbers with termination 7 within the sequence $\beta_b$

Composite numbers congruent to 17 (mod 30) within the sequence  $\beta_b = (6 * n - 1)$

$$Nc_{(b)t3} = (30 * n + 17) = \beta * (\delta + 30 * z)$$

$$n \geq 0$$

$$z \geq 0$$

### $\beta$ has infinite values

Formed by the sequence  $\beta = (6 * n \pm 1) = 5, 7, 11, 13, 17, 19, 23, 25, 29, 31, \dots$

$$\beta_1 = 5, \beta_2 = 7, \beta_3 = 11, \beta_4 = 13 \dots\dots$$

### $\delta$ has 10 variants

These 10 variables are always ordered in the same way and are repeated simultaneously until infinity as we add more values of  $\beta$ .

5 Nothing	11	7	29	31	23	19	25 Nothing	13	17
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The multiples of 5 are green and carry the word (nothing), these are not calculated since no multiples of 5 generate numbers with termination 7.

## $N_{C(b)t7} = \text{Composite numbers termination 7}$

$$\begin{array}{llll}
 N_{C(b)t7} = (30 * n + 17) & =\beta_1 \text{ Nothing} & = (30 * n + 17) & =5 \text{ Nothing} \\
 & =\beta_2*(11+30*z) & & =7*(11+30*z) \\
 & =\beta_3*(7+30*z) & & =11*(7+30*z) \\
 & =\beta_4*(29+30*z) & & =13*(29+30*z) \\
 & =\beta_5*(31+30*z) & & =17*(31+30*z) \\
 & =\beta_6*(23+30*z) & & =19*(23+30*z) \\
 & =\beta_{b7}*(19+30*z) & & =23*(19+30*z) \\
 & =\beta_8 \text{ Nothing} & & =25 \text{ Nothing} \\
 & =\beta_9*(13+30*z) & & =29*(13+30*z) \\
 & =\beta_{10}*(17+30*z) & & =31*(17+30*z) \\
 & ----- & & ----- \\
 & =\beta_{11} \text{ Nothing} & & =35 \text{ Nothing} \\
 & =\beta_{12}*(11+30*z) & & =37*(11+30*z) \\
 & =\beta_{13}*(7+30*z) & & =41*(7+30*z) \\
 & =\beta_{14}*(29+30*z) & & =43*(29+30*z) \\
 & =\beta_{15}*(31+30*z) & & =47*(31+30*z) \\
 & =\beta_{16}*(23+30*z) & & =49*(23+30*z) \\
 & =\beta_{17}*(19+30*z) & & =53*(19+30*z) \\
 & =\beta_{18} \text{ Nothing} & & =55 \text{ Nothing} \\
 & =\beta_{19}*(13+30*z) & & =59*(13+30*z) \\
 & =\beta_{20}*(17+30*z) & & =61*(17+30*z) \\
 & ----- & & ----- \\
 & \text{continue infinitely} & & \text{continue infinitely}
 \end{array}$$

The series is repeated every 10 blocks, (nothing,11,7,29,31,23,19,nothing,13,17).  
 We can add more  $\beta$  numbers and expand the formula infinitely.

### Demonstration 2

We solve when  $z = 0, z=1, z=2, \dots$

$$\begin{array}{llll}
 N_{C(b)t7} = (30 * n + 17) & =5 \text{ Nothing} & = (30 * n + 17) & = - \\
 & =7*(11+30*z) & & =77,287,497, \dots \\
 & =11*(7+30*z) & & =77,407,737, \dots \\
 & =13*(29+30*z) & & =377,767,1157, \dots \\
 & =17*(31+30*z) & & =527,1037,1547, \dots \\
 & =19*(23+30*z) & & =437,1007,1577, \dots \\
 & =23*(19+30*z) & & =437,1127,1817, \dots \\
 & =25 \text{ Nothing} & & = - \\
 & =29*(13+30*z) & & =377,1247,2117, \dots \\
 & =31*(17+30*z) & & =527,1457,2387, \dots \\
 & \text{continue infinitely} & & \text{continue infinitely}
 \end{array}$$

### Demonstration 3

#### C) Distances between composite numbers with termination 7 in column b.

The distance between composite numbers with termination 7 when we use the same value for  $\beta$  is equal to:

Distance between composite number  $D_7 = 30 * \beta$

$D_7 =$  Distance between composite number (Termination 7).

#### Example

$\beta = 7; \quad D_7 = 30 * 7 = 210$

$\beta = 11; \quad D_7 = 30 * 11 = 330$

$\beta = 13; \quad D_7 = 30 * 13 = 390$

### Theorem 3

At point A we will look for numbers with ending 7 within the sequence  $\beta_a = (6 * n + 1)$

At point B we will look for composite numbers with ending 7 within the sequence  $\beta_a = (6 * n + 1)$

$$\beta_a = (6 * n + 1) = 7, 13, 19, 25, 31, 37, 43, 49, 55, 61, 67, 73, 79, 85, \dots$$

$n > 0$

Reference [A016921](#) (The On-line Enciclopedia of integers sequences)

A) Formula for numbers with termination 7 within the sequence  $\beta_a$

$$N_{(a)t7} = (30 * n + 7)$$

$$N_{(a)t7} = 7, 37, 67, 97, 127, 157, 187, 217, 247, 277, 307, 337, 367, 397, \dots$$

$n \geq 0$   
 $z \geq 0$

Reference [A128471](#) (The On-line Enciclopedia of integers sequences)

### Demonstration 4

B) Formula for composite numbers with termination 7 within the sequence  $\beta_a$

Composite numbers congruent to 7 (mod 30) within the sequence  $\beta_a = (6 * n + 1)$

$$Nc_{(a) t7} = (30 * n + 7) = \beta * (\delta + 30 * z)$$

$n \geq 0$   
 $z \geq 0$

### $\beta$ has infinite values

Formed by the sequence  $\beta = (6 * n \pm 1) = 5, 7, 11, 13, 17, 19, 23, 25, 29, 31, \dots$

$\beta_1 = 5, \beta_2 = 7, \beta_3 = 11, \beta_4 = 13, \dots$

### $\delta$ has 10 variants

These 10 variables are always ordered in the same way and are repeated simultaneously until infinity as we add more values of  $\beta$ .

5 Nothing	31	17	19	11	13	29	25 Nothing	23	7
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The multiples of 5 are green and carry the word (nothing), these are not calculated since no multiples of 5 generate numbers with termination 7.

## $Nc_{(a)t7}$ = Composite numbers termination 7

$$\begin{array}{lcl}
 Nc_{(a)t7} = (30 * n + 7) & \begin{array}{l} =\beta_1 \text{ Nothing} \\ =\beta_2*(31+30*z) \\ =\beta_3*(17+30*z) \\ =\beta_4*(19+30*z) \\ =\beta_5*(11+30*z) \\ =\beta_6*(13+30*z) \\ =\beta_{b7}*(29+30*z) \\ =\beta_8 \text{ Nothing} \\ =\beta_9*(23+30*z) \\ =\beta_{10}*(7+30*z) \\ \hline =\beta_{11} \text{ Nothing} \\ =\beta_{12}*(31+30*z) \\ =\beta_{13}*(17+30*z) \\ =\beta_{14}*(19+30*z) \\ =\beta_{15}*(11+30*z) \\ =\beta_{16}*(13+30*z) \\ =\beta_{17}*(29+30*z) \\ =\beta_{18} \text{ Nothing} \\ =\beta_{19}*(23+30*z) \\ =\beta_{20}*(7+30*z) \\ \hline \end{array} & = (30 * n + 7) & \begin{array}{l} =\beta_5 \text{ Nothing} \\ =7*(31+30*z) \\ =11*(17+30*z) \\ =13*(19+30*z) \\ =17*(11+30*z) \\ =19*(13+30*z) \\ =23*(29+30*z) \\ =\beta_5 \text{ Nothing} \\ =29*(23+30*z) \\ =31*(7+30*z) \\ \hline =\beta_5 \text{ Nothing} \\ =37*(31+30*z) \\ =41*(17+30*z) \\ =43*(19+30*z) \\ =47*(11+30*z) \\ =49*(13+30*z) \\ =53*(29+30*z) \\ =\beta_5 \text{ Nothing} \\ =59*(23+30*z) \\ =61*(7+30*z) \\ \hline \end{array} \\
 & & & \begin{array}{l} \text{continue infinitely} \\ \text{continue infinitely} \end{array}
 \end{array}$$

The series is repeated every 10 blocks (nothing, 31,17,19,11,13,29,nothing ,23,7) to infinity. We can add more  $\beta$  numbers and expand the formula infinitely.

### Demonstration 5

We solve when  $z = 0, z=1, z=2, \dots$

$$\begin{array}{lcl}
 Nc_{(a)t7} = (30 * n + 7) & \begin{array}{l} =\beta_5 \text{ Nothing} \\ =7*(31+30*z) \\ =11*(17+30*z) \\ =13*(19+30*z) \\ =17*(11+30*z) \\ =19*(13+30*z) \\ =23*(29+30*z) \\ =\beta_5 \text{ Nothing} \\ =29*(23+30*z) \\ =31*(7+30*z) \\ \hline \end{array} & = (30 * n + 7) & \begin{array}{l} = - \\ =217,427,637 \dots \\ =187,517,847, \dots \\ =247,637,1027, \dots \\ =187,697,1207, \dots \\ =247,817,1387, \dots \\ =667,1357,2047, \dots \\ \hline =667,1537,2407, \dots \\ =217,1147,2077, \dots \\ \hline \end{array} \\
 & \text{continue infinitely} & & \text{continue infinitely}
 \end{array}$$

### Demonstration 6

A) Distances between composite numbers with termination 7 in column a.

The distance between composite numbers with termination 7 when we use the same value for  $\beta$  is equal to:

Distance between composite number  $D_7 = 30 * \beta$

$D_7$  = Distance between composite number (Termination 7).

#### Example

- A.  $\beta = 7; D_7 = 30 * 7 = 210$
- B.  $\beta = 11; D_7 = 30 * 11 = 330$
- C.  $\beta = 13; D_7 = 30 * 13 = 390$

**Theorem 4** We will use the same information that we obtained to calculate the numbers composed in the theorem 2, but in this occasion we will use the inequality to obtain only results of prime numbers.

At point A we will look for prime numbers with ending 3 within the sequence  $\beta_b = (6 * n - 1)$

$$\beta_b = (6 * n - 1) = 5, 11, 17, 23, 29, 35, 41, 47, 53, 59, 65, 71, 77, 83, 89 \dots\dots$$

$n > 0$

Reference [A007528](#) (The On-line Enciclopedia of integers sequences)

**Demonstration 7**

A) Formula for Prime numbers with termination 7 within the sequence  
 $\beta_b = (6 * n - 1)$

$$P_{(b)t7} = (30 * n + 17) \neq \beta * (\delta + 30 * z)$$

$n \geq 0$   
 $z \geq 0$

$\beta$  has infinite values

Formed by the sequence  $\beta = (6 * n \pm 1) = 5, 7, 11, 13, 17, 19, 23, 25, 29, 31, \dots$

$$\beta_1 = 5, \beta_2 = 7, \beta_3 = 11, \beta_4 = 13 \dots\dots$$

$\delta$  has 10 variants

These 10 variables are always ordered in the same way and are repeated simultaneously until infinity as we add more values of  $\beta$ .

5 Nothing	11	7	29	31	23	19	25 Nothing	13	17
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The multiples of 5 are green and carry the word (nothing), these are not calculated since no multiples of 5 generate numbers with termination 7.

Primes congruent to 17 (mod 30) within the sequence  $\beta_b = (6 * n - 1)$

$$P_{(b)t7} = \text{Prime numbers, termination 7}$$

$$P_{(b)t7} = (30 * n + 17) \neq 5 \text{ Nothing} = (30 * n + 17) \neq -$$

$\neq 7 * (11 + 30 * z)$ $\neq 11 * (7 + 30 * z)$ $\neq 13 * (29 + 30 * z)$ $\neq 17 * (31 + 30 * z)$ $\neq 19 * (23 + 30 * z)$ $\neq 23 * (19 + 30 * z)$ $\neq 25 \text{ Nothing}$ $\neq 29 * (13 + 30 * z)$ $\neq 31 * (17 + 30 * z)$ <i>continue infinitely</i>	$\neq 77, 287, 497, \dots$ $\neq 77, 407, 737, \dots$ $\neq 377, 767, 1157, \dots$ $\neq 527, 1037, 1547, \dots$ $\neq 437, 1007, 1577, \dots$ $\neq 437, 1127, 1817, \dots$ $\neq -$ $\neq 377, 1247, 2117, \dots$ $\neq 527, 1457, 2387, \dots$ <i>continue infinitely</i>
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$P_{(b)t7} = 17, 47, 107, 137, 167, 197, 227, 257, 317, 347, 467, 557, 587, 617, 647, 677, 797, 827, 857, 887, 947, 977, 1097, 1187, 1217, 1277, 1307, 1367, 1427, 1487, 1607, 1637, 1667, 1697, 1787, 1847, 1877, 1907, 1997, 2027, 2087, 2207, 2237, 2267, 2297, 2357, 2417, \dots$

Reference

[A039949](#) (The On-line Encyclopedia of integers sequences)

**Theorem 5** We will use the same information that we obtained to calculate the composite numbers in the theorem 3, but in this occasion we will use the inequality to obtain only results of prime numbers.

At point A we will look for prime numbers with ending 7 within the sequence  $\beta_a = (6 * n + 1)$

$$\beta_a = (6 * n + 1) = 7, 13, 19, 25, 31, 37, 43, 49, 55, 61, 67, 73, 79, 85, \dots$$

$n > 0$

Reference [A016921](#) (The On-line Encyclopedia of integers sequences)

### Demonstration 8

A) Formula for Prime numbers with termination 7 within the sequence

$$\beta_a = (6 * n + 1)$$

$$P_{(a)t7} = (30 * n + 7) \neq \beta * (\delta + 30 * z)$$

$n \geq 0$

$z \geq 0$

### $\beta$ has infinite values

Formed by the sequence  $\beta = (6 * n \pm 1) = 5, 7, 11, 13, 17, 19, 23, 25, 29, 31, \dots$

$\beta_1 = 5, \beta_2 = 7, \beta_3 = 11, \beta_4 = 13, \dots$

### $\delta$ has 10 variants

These 10 variables are always ordered in the same way and are repeated simultaneously until infinity as we add more values of  $\beta$ .

5 Nothing	31	17	19	11	13	29	25 Nothing	23	7
-----------	----	----	----	----	----	----	------------	----	---

The multiples of 5 are green and carry the word (nothing), these are not calculated since no multiples of 5 generate numbers with termination 7.

Primes congruent to 7 (mod 30) within the sequence  $\beta_a = (6 * n + 1)$

$$P_{(a)t7} = \text{Prime numbers termination 7}$$

$$P_{(a)t7} = (30 * n + 7) \quad \neq 5 \text{ Nothing} \quad = (30 * n + 7) \quad \neq -$$

$$\neq 7 * (31 + 30 * z) \quad \neq 217, 427, 637, \dots$$

$$\neq 11 * (17 + 30 * z) \quad \neq 187, 517, 847, \dots$$

$$\neq 13 * (19 + 30 * z) \quad \neq 247, 637, 1027, \dots$$

$$\neq 17 * (11 + 30 * z) \quad \neq 187, 697, 1207, \dots$$

$$\neq 19 * (13 + 30 * z) \quad \neq 247, 817, 1387, \dots$$

$$\neq 23 * (29 + 30 * z) \quad \neq 667, 1357, 2047, \dots$$

$$\neq 25 \text{ Nothing} \quad \neq -$$

$$\neq 29 * (23 + 30 * z) \quad \neq 667, 1537, 2407, \dots$$

$$\neq 31 * (7 + 30 * z) \quad \neq 217, 1147, 2077, \dots$$

*continue infinitely*

$P_{(a)t7} = 7, 37, 67, 97, 127, 157, 277, 307, 337, 367, 397, 457, 487, 547, 577, 607, 727, 757, 787, 877, 907, 937, 967, 997, 1087, 1117, 1237, 1297, 1327, 1447, 1567, 1597, 1627, 1657, 1747, 1777, 1867, 1987, 2017, 2137, 2287, 2347, 2377, 2437, 2467, 2557, 2617, 2647, \dots$

Reference [A132231](#) (The On-line Encyclopedia of integers sequences)

### Theorem 6 Graphic table 1, with termination 7.

In yellow the prime numbers						In red the composite numbers					
Composite number in red Prime numbers with termination 7 in green						Prime number in Yellow Composite numbers with termination 7 in light blue					
A			B			A			B		
$\beta_a$			$\beta_b$			$\beta_a$			$\beta_b$		
1	2	3	4	5	6	1	2	3	4	5	6
7	8	9	10	11	12	7	8	9	10	11	12
13	14	15	16	17	18	13	14	15	16	17	18
19	20	21	22	23	24	19	20	21	22	23	24
25	26	27	28	29	30	25	26	27	28	29	30
31	32	33	34	35	36	31	32	33	34	35	36
37	38	39	40	41	42	37	38	39	40	41	42
43	44	45	46	47	48	43	44	45	46	47	48
49	50	51	52	53	54	49	50	51	52	53	54
55	56	57	58	59	60	55	56	57	58	59	60
61	62	63	64	65	66	61	62	63	64	65	66
67	68	69	70	71	72	67	68	69	70	71	72
73	74	75	76	77	78	73	74	75	76	77	78
79	80	81	82	83	84	79	80	81	82	83	84
85	86	87	88	89	90	85	86	87	88	89	90
91	92	93	94	95	96	91	92	93	94	95	96
97	98	99	100	101	102	97	98	99	100	101	102
103	104	105	106	107	108	103	104	105	106	107	108
109	110	111	112	113	114	109	110	111	112	113	114
115	116	117	118	119	120	115	116	117	118	119	120
121	122	123	124	125	126	121	122	123	124	125	126
127	128	129	130	131	132	127	128	129	130	131	132
133	134	135	136	137	138	133	134	135	136	137	138
139	140	141	142	143	144	139	140	141	142	143	144

## Conclusion

The numbers with ending 7 are ordered every 30 numbers interspersed between composite numbers and prime numbers. These have two variables.

The first variable shows that the numbers of the formula  $N_{(b)t7} = (30 * n + 17)$  are located in the column (B.) The sum of their digits always generates the sequence 2,5,8.

The second variable shows that the numbers of the formula  $N_{(a)t7} = (30 * n + 7)$  are located in another column (A). the sum of its digits always generates the sequence 1,4,7.

By means of equalities and inequalities we can condition these formulas to obtain all prime numbers greater than 3 and all composite numbers divisible by numbers greater than 3 by means of a simple, unique and infinite expression.

By equalities we obtain composite numbers divisible by numbers greater than 3 whit termination 7.

By inequalities we obtain the prime numbers greater than 3 whit termination 7.

The formula developed with the 10 variables of the delta letter allows you to obtain them infinitely.

These 10 variables are the key for the formula to work.

Thanks to this expression we can understand how the prime numbers and the composite numbers with ending 7 are distributed.

The multiples of 5 in beta are excluded since they do not generate numbers with ending 7.

This formula demonstrates that it is possible to calculate and obtain the sequence of prime numbers with ending 7 and also that of the composite numbers.

This model is applied to the other three terminations (1,3,9) although the locations of the delta numbers vary, since these are the same but they are located differently.

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## References

1. Burton, J. (1964). The Theory of Numbers. United States of America. Library of Congress Catalog Card Number: 55-6187. Página 41
2. Dickson L. E., History of the Theory of Numbers.
3. Euclides, Elementorum Libri XV (Lipsiae 1769, books 7,8,9)
4. Hardy, G. H. and Wright, E. M. An Introduction to the Theory of Numbers, 5th ed. Oxford, England: Clarendon Press, pp. 13 and 219, 1979.
5. H. Riesel, Prime Numbers and Computer Methods for Factorization, Birkhaeuser Boston, Cambridge MA 1994.
6. Hua Loo Keng, Introduction to Number theory (1982).
7. M. Dietzfelbinger, Primality Testing in Polynomial Time, Springer NY 2004.
8. Shanks, Solved and unsolved problems in Number theory (3 ed. 1985).
9. T. M. Apostol, Introduction to Analytic Number Theory, Springer-Verlag, 1976, page 2.
10. The On-line Enciclopedia of integers sequences
11. W. & F. Ellison, Prime Numbers, Hermann Paris 1985
12. Zeolla Gabriel M, Formula for Prime Numbers and Composite Numbers. [viXra:1801.0063](https://arxiv.org/abs/1801.0063)
13. Zeolla Gabriel M, Formula to find prime numbers and composite numbers with termination 9 <http://vixra.org/>
14. Zeolla Gabriel M, Formula to find prime numbers and composite numbers with termination 3 <http://vixra.org/abs/1805.0076>
15. Zeolla Gabriel M, Formula to find prime numbers and composite numbers with termination 1 <http://vixra.org/abs/1804.0262>

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