

Contents

Introduction by Charles Ashbacher	4
Tribute to Joseph S. Madachy by Charles Ashbacher	5
Mathematical Cartoons by Caytie Ribble	15
Here's the Scoop: Ground Balls Win Lacrosse Games by Peter R. Smith, Russell K. Banker and Paul M. Sommers	17
An Example of a Smarandache Geometry by Ion Patrascu	28
Smarandache's Concurrent Lines Theorem edited by Dr. M. Khoshnevisan	31
The Career Save Percentage Profile of NHL Goalies by Douglas A. Raeder and Paul M. Sommers	35
Some Unsolved Problems in Number Theory by Florentin Smarandache	40
Alternating Iterations of the Sum of Divisors Function and the Pseudo-Smarandache Function by Henry Ibstedt	42
Alternating Iterations of the Euler φ Function and the Pseudo-Smarandache Function by Henry Ibstedt	52
Book Reviews Edited by Charles Ashbacher	70
Alphametics contributed by Paul Boymel	76
Problems and Conjectures contributed by Lamarr Widmer	79

Solutions To Problems And Conjectures From Journal Of Recreational Mathematics 37(3) edited by Lamarr Widmer	82
Solutions to Alphametics Appearing in This Issue	91
Solutions to Alphametics in Journal of Recreational Mathematics 37(3)	92
Project Euler	96
Map Coloring with Combinatorics by Kate Jones	98
Mathematical Spectrum	101
Neutrosphic Sets and Systems	102
Topics in Recreational Mathematics 1/2015	104
Alphametics as Expressed in Recreational Mathematics Magazine	105

SMARANDACHE'S CONCURRENT LINES THEOREM

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Abstract

In this paper we present the Smarandache's Concurrent Lines Theorem in the geometry of the polygon. The theorem states that if a polygon having any number of sides greater than 3 is circumscribed around a circle then the set of lines connecting vertices of the polygon in combination with the set of lines connecting points of tangency to the circle has at least three of the lines are concurrent.

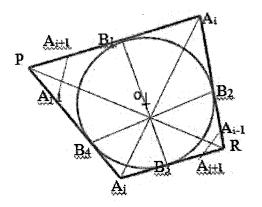
31

Let's consider a polygon (which has at least four sides) circumscribed to a circle, and D the set of its diagonals and the lines joining the points of contact of two non-adjacent sides. Then the set D contains at least three concurrent lines.

Proof:

Let n be the number of sides. If n = 4, then the two diagonals and the two lines joining the points of contact of two adjacent sides are concurrent (according to Newton's Theorem).

The case n > 4 is reduced to the previous case: we consider any polygon $A_1...A_n$ (see the figure)



circumscribed to the circle and we choose two vertices A_i , A_j $(i \neq j)$ such that

$$A_j A_{j-1} \cap A_i A_{i+1} = P$$

and

$$A_j A_{j+1} \cap A_i A_{i-1} = R$$

Let B_h , $h \in \{1, 2, 3, 4\}$, be the contact points of the quadrilateral PA_jRA_i with the circle of center O. Because of the Newton's theorem, the lines A_i , A_j , B_1B_3 and B_2B_4 are concurrent.

Open Problems related to the Smarandache Concurrent Lines Theorem

- 1) In what conditions are there more than three concurrent lines?
- 2) What is the maximum number of concurrent lines that can exist (and in what conditions)?
- 3) What about an alternative of this problem: to consider instead of a circle an ellipse, and then a polygon *ellipsoscribed* (let's invent this word, *ellipso-scribed*, meaning a polygon whose all sides are tangent to an ellipse which inside of it): how many concurrent lines we can find among its diagonals and the lines connecting the point of contact of two non-adjacent sides?
- 4) What about generalizing this problem in a 3D-space: a sphere and a polyhedron circumscribed to it?
- 5) Or instead of a sphere to consider an ellipsoid and a polyhedron ellipsoido-scribed to it?
- 6) What about considering the lines that connect a vertex with a non-adjunct point of contact? Are there three or more such lines that intersect in the same point? (Consider all previous five questions.)

Comments

Of course, we can go by construction reversely: take a point inside a circle (similarly for an ellipse, a sphere, or ellipsoid), then draw secants passing through this point that intersect the circle (ellipse, sphere, ellipsoid) into two points, and then draw tangents to the circle (or ellipse), or tangent planes to the sphere or ellipsoid) and try to construct a polygon (or polyhedron) from the intersections of the tangent lines (or of tangent planes) if possible.

For example, a regular polygon (or polyhedron) has a higher chance to have more concurrent such lines.

In the 3D space, we may consider, as alternative to this problem, the intersection of planes (instead of lines).

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