

Discussion on the Negate and the Proof of ABC Conjecture

Zhang Tianshu

Zhanjiang city, Guangdong province, China
chinazhangtianshu@126.com
china.zhangtianshu@tom.com

Abstract

The ABC conjecture is both likely of the wrong and likely of the right in the face of satisfactory many primes and satisfactory many odd numbers of $6K \pm 1$ from operational results of computer programs. So we find directly a specific equality $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$, then set about analyzing limits of values of ε to discuss the right and the wrong of the ABC conjecture in which case satisfying $2^N-1 > (\text{Rad}(1, 2^N(2^N-2), 2^N-1))^{1+\varepsilon}$. Thereby supply readers to make with a judgment concerning a truth or a falsehood which the ABC conjecture is.

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1. Introduction

The ABC conjecture was proposed by Joseph Oesterle and David Masser in 1985. The conjecture states that if A, B and C are three co-prime positive integers satisfying $A+B=C$, then for any real number $\varepsilon > 0$, there is merely at most a finite number of solutions to the inequality $C > (\text{Rad}(A, B, C))^{1+\varepsilon}$, where $\text{Rad}(A, B, C)$ denote the product of all distinct prime divisors of A, B

and C. Yet it is still both unproved and un-negated a conjecture hitherto, although somebody claiming proved it on the internet.

2. The Proof and the negate coexist

As everyone knows, whether anybody wants to prove thoroughly the ABC conjecture or negate the ABC conjecture once and for all, undoubtedly that is a very difficult thing after all.

Such being the case, and that equality $A+B=C$ needs satisfying $C > (\text{Rad}(A, B, C))^{1+\varepsilon}$, thus we have to find such an equality such that smallest difference of C minus $\text{Rad}(A, B, C)$ is equal to smallest positive integer 1. The reason to do so, noticeably imply that after solve this case once, actually it solves all cases which are covered by it.

So let A or B be equal to 1, and another is equal to O^2-1 , then C is equal to O^2 according to $A+B=C$, where O is an odd number >1 and the same below.

Then, equality $A+B=C$ satisfying $C > (\text{Rad}(A, B, C))^{1+\varepsilon}$ is turned into equality $1+(O^2-1)=O^2$ satisfying $O^2 > (\text{Rad}(1, O^2-1, O^2))^{1+\varepsilon}$ i.e. satisfying $O > (\text{Rad}(O^2-1))^{1+\varepsilon}$ in which case regard ε as an infinitesimal real number > 0 .

When O expresses from small to large positive prime numbers and from small to large positive odd numbers of $6K\pm 1$ with $K \geq 1$, please, see also appendices 1, 2 and 3 at the back of this article.

After you have seen such appendices, we are indeed unable to reach any conclusion from them, but I am sure that they can shake your perspective.

However, to my way of thinking, although the densities of satisfactory prime

numbers and satisfactory odd numbers of $6K\pm 1$ are getting sparser and sparser along with which the values of O are getting greater and greater, but there are infinitely many prime numbers and infinitely many odd numbers of $6K\pm 1$ after all. To say nothing of this conjecture including all positive integers, then satisfactory positive odd numbers and satisfactory positive integers must be even more.

Judging from this, inequalities like $O > (\text{Rad}(O^2 - 1))^{1+\varepsilon}$ seemingly should last forever in which case regard ε as an infinitesimal real number > 0 .

Well then, let us cite a specific equality to expound both affirmative and negative cases thereafter.

From $O^2 - 1 = (O+1)(O-1)$, we know that $O+1$ and $O-1$ are two even numbers, then, both of them have a common prime factor 2.

In the circumstance, we might well let $O+1$ be equal to 2^N , then not only 2 is a common prime factor of $O+1$ and $O-1$, and that 2 is the unique prime factor of $O+1$, where N is a natural number ≥ 2 .

Thus, aforementioned satisfying $O > (\text{Rad}(O^2 - 1))^{1+\varepsilon}$, actually it is exactly satisfying $O > (\text{Rad}(O-1))^{1+\varepsilon}$ here.

After substitute 2^N for $O+1$ and do certain relevant substitutions, equality $1 + (O^2 - 1) = O^2$ satisfying $O > (\text{Rad}(O-1))^{1+\varepsilon}$ is transformed into equality $1 + 2^N(2^N - 2) = (2^N - 1)^2$ satisfying $2^N - 1 > (\text{Rad}(2^N - 2))^{1+\varepsilon}$ in which case regard ε as an infinitesimal real number > 0 .

On the supposition of $2^N - 1 = (\text{Rad}(2^N - 2))^{1+\varepsilon}$, it has $1 + \varepsilon = \log_{\text{rad}(2^N - 2)}(2^N - 1)$, and

$$\varepsilon = [\log_{\text{rad}(2^N-2)}(2^N-1)]-1.$$

Thus it can be seen, if $\varepsilon = [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, then $2^N-1 = (\text{Rad}(2^N-2))^{1+\varepsilon}$;

If $0 < \varepsilon < [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, then $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$, and that there are infinitely many real numbers of ε between 0 and $[\log_{\text{rad}(2^N-2)}(2^N-1)]-1$;

If $\varepsilon > [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, then $2^N-1 < (\text{Rad}(2^N-2))^{1+\varepsilon}$, of course, there are infinitely many real numbers of ε in the case too.

Hereinafter, we will divide limits as compared with requirements which suit the conjecture into four parts in accordance with disparate evaluations of ε to explain the relation inter se, and decide acceptance or rejection for each part.

Firstly, when $\varepsilon=0$, there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$. Evidently, this kind of cases has nothing to do with the conjecture because $\varepsilon=0$ is inconformity to the requirement of the conjecture.

Secondly, when $0 < \varepsilon < [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$. Then, there are both infinitely many natural numbers of N and infinitely many real numbers of ε to satisfy each and every inequality under the circumstance.

Thirdly, when $\varepsilon = [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, there is equality $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 = (\text{Rad}(2^N-2))^{1+\varepsilon}$. This kind of case has nothing to do with the conjecture too because $2^N-1 = (\text{Rad}(2^N-2))^{1+\varepsilon}$ is inconformity to the requirement of the conjecture.

Fourthly, when $\varepsilon > [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, there are infinitely many equalities

like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 < (\text{Rad}(2^N-2))^{1+\varepsilon}$. Likewise this kind of cases has nothing to do with the conjecture because $2^N-1 < (\text{Rad}(2^N-2))^{1+\varepsilon}$ is inconformity to the requirement of the conjecture.

By this token, whether you want to negate the ABC conjecture or prove the ABC conjecture, either can only from secondly part i.e. the circumstance when $0 < \varepsilon < [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$ to consider it.

By now, let us list N and $1+2^N(2^N-2)=(2^N-1)^2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$ after evaluations of headmost N as follows, where $0 < \varepsilon < [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, but real numbers which satisfy ε of each inequality are incomplete alike.

N	2^N	$2^N(2^N-2)$	$2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$	$1+2^N(2^N-2)=(2^N-1)^2$
2,	4,	8,	$3 > 2^{1+\varepsilon}$,	$1+8=9$
3,	8,	48,	$7 > (2*3)^{1+\varepsilon} = 6^{1+\varepsilon}$,	$1+48=49$
4,	16,	224,	$15 > (2*7)^{1+\varepsilon} = 14^{1+\varepsilon}$,	$1+224=225$
5,	32,	960,	$31 > (2*3*5)^{1+\varepsilon} = 30^{1+\varepsilon}$,	$1+960=961$
6,	64,	3968,	$63 > (2*31)^{1+\varepsilon} = 62^{1+\varepsilon}$,	$1+3968=3969$
7,	128,	16128,	$127 > (2*3*7)^{1+\varepsilon} = 42^{1+\varepsilon}$,	$1+16128=16129$
8,	256,	65024,	$255 > (2*127)^{1+\varepsilon} = 254^{1+\varepsilon}$,	$1+65024=65025$
9,	512,	261120,	$511 > (2*3*5*17)^{1+\varepsilon} = 510^{1+\varepsilon}$,	$1+261120=261121$
10,	1024,	1046528,	$1023 > (2*7*73)^{1+\varepsilon} = 1022^{1+\varepsilon}$,	$1+1046528=1046529$
11,	2048,	4190208,	$2047 > (2*3*11*31)^{1+\varepsilon} = 2046^{1+\varepsilon}$,	$1+4190208=4190209$
12,	4096,	16769024,	$4095 > (2*23*89)^{1+\varepsilon} = 4094^{1+\varepsilon}$,	$1+16769024=16769025$
13,	8192,	67092480,	$8191 > (2*3*5*7*13)^{1+\varepsilon} = 2730^{1+\varepsilon}$,	$1+67092480=67092481$
14,	16384,	268402688,	$16383 > (2*8191)^{1+\varepsilon} = 16382^{1+\varepsilon}$,	$1+268402688=268402689$
15,	32768,	1073676288,	$32767 > (2*3*43*127)^{1+\varepsilon} = 32766^{1+\varepsilon}$,	$1+1073676288=1073676289$
...

From listed above inequalities and their extensions, we are not difficult to make out that smallest difference of 2^N-1 minus $\text{Rad}(2^N-2)$ is 1, and that values of ε are getting smaller and smaller up to infinitesimal along with which values of N are getting greater and greater up to infinite.

Since there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$, satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$ where $0 < \varepsilon < [\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, so we are necessary to divide this circumstance into two aspects i.e. the negate and the proof to expound them respectively.

3. Negating the ABC conjecture

Negate the ABC conjecture, undoubtedly, this implies that we must find at least a value of ε between 0 and $[\log_{\text{rad}(2^N-2)}(2^N-1)]-1$ such that both there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ and satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$.

For the point that there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$, this has been no any question due to $N \geq 2$. Problem is to confirm at least a satisfactory real number.

Now that there are infinitely many positive real numbers between 0 and $[\log_{\text{rad}(2^N-2)}(2^N-1)]-1$, then the positive real number which and 0 border on each other is the smallest positive real number certainly.

Suppose that we named the smallest positive real number “ ε_0 ”, then, there is not a real number between 0 and ε_0 . Then again, there are still infinitely many positive real numbers between ε_0 and $\log_{\text{rad}(2^N-2)}(2^N-1)-1$.

Consequently, if N is endowed with infinite many values, then there are still infinitely many values of ε between ε_0 and $\log_{\text{rad}(2^N-2)}(2^N-1)-1$, enable them to form one-to-one correspondence such that $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_0}$.

In other words, when $\varepsilon=\varepsilon_0$, there are infinitely many equalities like

$$1+2^N(2^N-2)=(2^N-1)^2 \text{ with } N \geq 2 \text{ satisfying } 2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_0}.$$

Moreover, start from ε_0 , we named orderly-increasing and orderly-adjacent real numbers $\varepsilon_0, \varepsilon_1, \varepsilon_2 \dots \varepsilon_y$, where y is a concrete natural number which consists of Arabic numerals. Without doubt, for any real number ε_y , there are infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ with $N \geq 2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_y}$ because N forever cannot increase to $\aleph_0(y+1)$ natural number counted-backwards, so ε forever cannot decrease to ε_y . For natural numbers, there exist not any counted-backwards problem radically either.

That is to say, when $\varepsilon=\varepsilon_y$, there are infinitely many equalities like

$$1+2^N(2^N-2)=(2^N-1)^2 \text{ with } N \geq 2 \text{ satisfying } 2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_y} \text{ too.}$$

So far, let us come back to contents of the conjecture to make a comparison with the specific equality: first, three terms 1, $2^N(2^N-2)$ and $(2^N-1)^2$ in the specific equality are co-prime positive integers. Secondly, qualifications of equalities like $1+2^N(2^N-2)=(2^N-1)^2$ are completely in conformity with the requirements of the conjecture.

If you regard ε_0 plus ε_y as a fixed real number because ε_0 can be described by us, then only this and nothing more, the ABC conjecture asserted the argument that if A, B and C are three co-prime positive integers satisfying $A+B=C$, for any real number $\varepsilon>0$, there is merely at most a finite number of solutions to the inequality $C > \text{Rad}(A, B, C)^{1+\varepsilon}$, has to be negated by infinitely many equalities like $1+2^N(2^N-2)=(2^N-1)^2$ satisfying $(2^N-1)^2 > (\text{rad}(1, 2^N(2^N-2)),$

$(2^N - 1)^2))^{1+\varepsilon}$ i.e. satisfying $2^N - 1 > (\text{rad}(2^N - 2))^{1+\varepsilon}$, where $N \geq 2$, $0 < \varepsilon = \varepsilon_0, \varepsilon_1, \varepsilon_2 \dots \varepsilon_y$, and y is a concrete natural number.

As thus, the ABC conjecture can only be regarded as a fallacy.

4. Proving the ABC conjecture

Prove the ABC conjecture, obviously this implies that we are unable to find a fixed real number, such that both there are infinitely many equalities like $1 + 2^N(2^N - 2) = (2^N - 1)^2$ with $N \geq 2$ and satisfying $2^N - 1 > (\text{Rad}(2^N - 2))^{1+\varepsilon}$.

That is to say, for any real number $\varepsilon > 0$, there are merely finitely many equalities like $1 + 2^N(2^N - 2) = (2^N - 1)^2$ satisfying $2^N - 1 > (\text{Rad}(2^N - 2))^{1+\varepsilon}$ in which case regard ε as a fixed value.

Since $N \geq 2$, then, on the one hand, values of N are getting more and more up to infinite many along with which values of N are getting greater and greater up to infinite, accordingly cause that there are infinitely many equalities like $1 + 2^N(2^N - 2) = (2^N - 1)^2$.

On the other hand, greatest value of ε in correspondence with value of N is getting smaller and smaller up to infinitesimal along with which value of N is getting greater and greater up to infinite, so values of ε are getting more and more up to infinite many such that there are infinitely many inequalities $2^N - 1 > (\text{Rad}(2^N - 2))^{1+\varepsilon}$ satisfying one-for-one requirement for all equalities.

So that start from any known real number to lessen continuously one real number by one real number, enable the series of real numbers to reach an infinitesimal fixed value ε_x in finite field, then a value of N in

correspondence with ε_x is still a finite-great natural number, accordingly there are only finitely many equalities like $1+2^N(2^N-2) = (2^N-1)^2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_x}$.

Therefore, although start from arbitrary great a natural number of N upwards or arbitrary small a real number of ε downwards to form more and more equalities like $1+2^N(2^N-2) = (2^N-1)^2$ satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$, but since forever cannot find an infinitesimal fixed real number in finite field such as ε_y to let equalities like $1+2^N(2^N-2) = (2^N-1)^2$ have infinitely many like as satisfying $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon_y}$.

In other words, 1, $2^N(2^N-2)$ and $(2^N-1)^2$ are three co-prime positive integers satisfying $1+2^N(2^N-2) = (2^N-1)^2$, for any real number $\varepsilon > 0$, there is merely at most a finite number of solutions to the inequality $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$.

In addition, since smallest difference of 2^N-1 minus $\text{Rad}(2^N-2)$ is smallest positive integer 1, therefore $2^N-1 > (\text{Rad}(2^N-2))^{1+\varepsilon}$ represented sufficiently any $C > (\text{Rad}(A, B, C))^{1+\varepsilon}$.

Consequently, the ABC conjecture is proven as a truth.

5. Given a Conclusion from the Author

The reason that cause both proving and negating the ABC conjecture, in my opinion, the key to the settlement of the question lies in mathematical circles whether they can admit ε_0 as a fixed real number.

If ε_0 is admitted as a fixed real number, then the ABC conjecture thereupon is negated either.

If ε_0 can not be admitted as a fixed real number, then the ABC conjecture is tenable according to the proof of preceding fourth section.

Nothing but, to my way of thinking, the ABC conjecture should be negated by us because ε_0 adjoins closely acknowledged integer 0, it has the title and the point location, also it and any real number can compare large or tiny.

Discussion on the Negate and the Proof of ABC conjecture was thus brought to a close. Is exactly right the ABC conjecture, or wrong? I am fully convinced of the ability of judgment of readers.

Appendix 1: Prime number P and equality $1 + (P^2 - 1) = P^2$ satisfying $P > (\text{Rad}(P^2 - 1))^{1+\varepsilon}$ after the evaluations of headmost P are listed as follows, but real numbers which satisfy ε of each inequality are incomplete alike.

P,	$P^2 - 1$,	$\text{Rad}(P^2 - 1)$
7,	48,	$2 \cdot 3 = 6$
17,	288,	$2 \cdot 3 = 6$
31,	960,	$2 \cdot 3 \cdot 5 = 30$
97,	9408,	$2 \cdot 3 \cdot 7 = 42$
127,	16128,	$2 \cdot 3 \cdot 7 = 42$
251,	63000,	$2 \cdot 3 \cdot 5 \cdot 7 = 210$
449,	201600,	$2 \cdot 3 \cdot 5 \cdot 7 = 210$
487,	237168,	$2 \cdot 3 \cdot 61 = 366$
577,	332928,	$2 \cdot 3 \cdot 17 = 102$
1151,	1324800,	$2 \cdot 3 \cdot 5 \cdot 23 = 690$
1249,	1560000,	$2 \cdot 3 \cdot 5 \cdot 13 = 390$
1567,	2455488,	$2 \cdot 3 \cdot 7 \cdot 29 = 1218$
1999,	3996000,	$2 \cdot 3 \cdot 5 \cdot 37 = 1110$
2663,	7091568,	$2 \cdot 3 \cdot 11 \cdot 37 = 2442$
4801,	23049600,	$2 \cdot 3 \cdot 5 \cdot 7 = 210$
4999,	24990000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 17 = 3570$
7937,	62995968,	$2 \cdot 3 \cdot 7 \cdot 31 = 1302$
8191,	67092480,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 13 = 2730$
12799,	163814400,	$2 \cdot 3 \cdot 5 \cdot 79 = 2370$
13121,	172160640,	$2 \cdot 3 \cdot 5 \cdot 41 = 1230$

13183,	173791488,	$2 \cdot 3 \cdot 13 \cdot 103 = 8034$
15551,	241833600,	$2 \cdot 3 \cdot 5 \cdot 311 = 9330$
31249,	976500000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 31 = 6510$
31751,	1008126000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 127 = 26670$
32257,	1040514048,	$2 \cdot 3 \cdot 7 \cdot 127 = 5334$
33857,	1146296448,	$2 \cdot 3 \cdot 11 \cdot 19 \cdot 23 = 28842$
35153,	1235733408,	$2 \cdot 3 \cdot 7 \cdot 13 \cdot 31 = 16926$
39367,	1549760688,	$2 \cdot 3 \cdot 7 \cdot 19 \cdot 37 = 29526$
65537,	4295098368,	$2 \cdot 3 \cdot 11 \cdot 331 = 21846$
79201,	6272798400,	$2 \cdot 3 \cdot 5 \cdot 11 \cdot 199 = 65670$
81919,	6710722560,	$2 \cdot 3 \cdot 5 \cdot 37 \cdot 41 = 45510$
85751,	7353234000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 397 = 83370$
115249,	13282332000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 461 = 96810$
117127,	13718734128,	$2 \cdot 3 \cdot 11 \cdot 241 = 15906$
124001,	15376248000,	$2 \cdot 3 \cdot 5 \cdot 31 \cdot 83 = 77190$
126001,	15876252000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 251 = 52710$
131071,	17179607040,	$2 \cdot 3 \cdot 5 \cdot 17 \cdot 257 = 131070$
153089,	23436241920,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 23 = 62790$
160001,	25600320000,	$2 \cdot 3 \cdot 5 \cdot 2963 = 88890$
161839,	26191861920,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 17 \cdot 37 = 132090$
165887,	27518496768,	$2 \cdot 3 \cdot 7 \cdot 17 \cdot 41 = 29274$
196831,	38742442560,	$2 \cdot 3 \cdot 5 \cdot 6151 = 184530$
215297,	46352798208,	$2 \cdot 3 \cdot 29 \cdot 443 = 77082$
281249,	79101000000,	$2 \cdot 3 \cdot 5 \cdot 11 \cdot 17 \cdot 47 = 263670$
442367,	195688562688,	$2 \cdot 3 \cdot 29 \cdot 263 = 45762$
474337,	224995589568,	$2 \cdot 3 \cdot 61 \cdot 487 = 178242$
511757,	261895227048,	$2 \cdot 3 \cdot 7 \cdot 13 \cdot 373 = 203658$
524287,	274876858368,	$2 \cdot 3 \cdot 7 \cdot 19 \cdot 73 = 58254$
538001,	289445076000,	$2 \cdot 3 \cdot 5 \cdot 41 \cdot 269 = 330870$
665857,	443365544448,	$2 \cdot 3 \cdot 17 \cdot 577 = 58854$
715823,	512402567328,	$2 \cdot 3 \cdot 71 \cdot 1657 = 705882$
902501,	814508055000,	$2 \cdot 3 \cdot 5 \cdot 19 \cdot 619 = 352830$
911249,	830374740000,	$2 \cdot 3 \cdot 5 \cdot 13 \cdot 337 = 131430$
988417,	976968165888,	$2 \cdot 3 \cdot 11 \cdot 13 \cdot 19 \cdot 37 = 603174$
1039681,	1080936581760,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 19 \cdot 103 = 410970$
1062881,	1129716020160,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 73 = 199290$
1102249,	1214952858000,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 4409 = 925890$
1179649,	1391571763200,	$2 \cdot 3 \cdot 5 \cdot 23593 = 707790$
1229311,	1511205534720,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 29 \cdot 157 = 956130$
1246589,	1553984134920,	$2 \cdot 3 \cdot 5 \cdot 7 \cdot 19 \cdot 211 = 841890$
1272833,	1620103845888,	$2 \cdot 3 \cdot 11 \cdot 97 \cdot 113 = 723426$

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Appendix 2: Odd number $6K-1$ and equality $1 + ((6K-1)^2 - 1) = (6K-1)^2$ satisfying $6K-1 > (\text{Rad}((6K-1)^2 - 1))^{1+\varepsilon}$ after the evaluations of headmost $6K-1$ are listed as follows, but real numbers which satisfy ε of each inequality are incomplete alike.

$6K-1$	$(6K-1)^2 - 1$	$\text{Rad}((6K-1)^2 - 1)$
17,	288,	$2^*3=6$
161,	25920,	$2^*3^*5=30$
251,	63000,	$2^*3^*5^*7=210$
449,	201600,	$2^*3^*5^*7=210$
485,	235224,	$2^*3^*11=66$
1025,	1050624,	$2^*3^*19=114$
1151,	1324800,	$2^*3^*5^*23=690$
1457,	2122848,	$2^*3^*7^*13=546$
2177,	4739328,	$2^*3^*11^*17=1122$
2663,	7091568,	$2^*3^*11^*37=2442$
4607,	21224448,	$2^*3^*7^*47=1974$
5291,	27994680,	$2^*3^*5^*7^*23=4830$
7775,	60450624,	$2^*3^*13^*23=1794$
7937,	62995968,	$2^*3^*7^*31=1302$
9827,	96569928,	$2^*3^*7^*13^*17=9282$
10751,	115584000,	$2^*3^*5^*7^*43=9030$
11663,	136025568,	$2^*3^*7^*17=714$
13121,	172160640,	$2^*3^*5^*41=1230$
14849,	220492800,	$2^*3^*5^*11^*29=9570$
15551,	241833600,	$2^*3^*5^*311=9330$
19601,	384199200,	$2^*3^*5^*7^*11=2310$
24335,	592192224,	$2^*3^*13^*23=1794$
25001,	625050000,	$2^*3^*5^*463=13890$
28673,	822140928,	$2^*3^*7^*59=2478$
31751,	1008126000,	$2^*3^*5^*7^*127=26670$
33281,	1107624960,	$2^*3^*5^*13^*43=16770$
33857,	1146296448,	$2^*3^*11^*19^*23=28842$
35153,	1235733408,	$2^*3^*7^*13^*31=16926$
36449,	1328529600,	$2^*3^*5^*17^*67=34170$
48599,	2361862800,	$2^*3^*5^*11^*47=15510$

49151,	2415820800,	$2^3 \cdot 3^5 \cdot 983 = 29490$
52001,	2704104000,	$2^3 \cdot 3^5 \cdot 13 \cdot 107 = 41730$
53249,	2835456000,	$2^3 \cdot 3^5 \cdot 13 \cdot 71 = 27690$
58751,	3451680000,	$2^3 \cdot 3^5 \cdot 17 \cdot 47 = 23970$
65537,	4295098368,	$2^3 \cdot 3^5 \cdot 11 \cdot 331 = 21846$
67229,	4519738440,	$2^3 \cdot 3^5 \cdot 7 \cdot 83 = 17430$
73001,	5329146000,	$2^3 \cdot 3^5 \cdot 23 \cdot 73 = 50370$
83105,	6906441024,	$2^3 \cdot 3^5 \cdot 7 \cdot 19 \cdot 53 = 42294$
85751,	7353234000,	$2^3 \cdot 3^5 \cdot 7 \cdot 397 = 83370$
95831,	9183580560,	$2^3 \cdot 3^5 \cdot 7 \cdot 11 \cdot 37 = 85470$
98495,	9701265024,	$2^3 \cdot 3^5 \cdot 11 \cdot 19 \cdot 37 = 46398$
101249,	10251360000,	$2^3 \cdot 3^5 \cdot 7 \cdot 113 = 23730$
118097,	13946901408,	$2^3 \cdot 3^5 \cdot 11 \cdot 61 = 4026$
124001,	15376248000,	$2^3 \cdot 3^5 \cdot 31 \cdot 83 = 77190$
130049,	16912742400,	$2^3 \cdot 3^5 \cdot 17 \cdot 127 = 64770$
145001,	21025290000,	$2^3 \cdot 3^5 \cdot 11 \cdot 13 \cdot 29 = 124410$
153089,	23436241920,	$2^3 \cdot 3^5 \cdot 7 \cdot 13 \cdot 23 = 62790$
160001,	25600320000,	$2^3 \cdot 3^5 \cdot 2963 = 88890$
165887,	27518496768,	$2^3 \cdot 3^5 \cdot 7 \cdot 17 \cdot 41 = 29274$
171395,	29376246024,	$2^3 \cdot 3^5 \cdot 17 \cdot 23 \cdot 71 = 166566$
194399,	37790971200,	$2^3 \cdot 3^5 \cdot 37 \cdot 71 = 78810$
207647,	43117276608,	$2^3 \cdot 3^5 \cdot 7 \cdot 47 \cdot 103 = 203322$
209951,	44079422400,	$2^3 \cdot 3^5 \cdot 13 \cdot 17 \cdot 19 = 125970$
215297,	46352798208,	$2^3 \cdot 3^5 \cdot 29 \cdot 443 = 77082$
246401,	60713452800,	$2^3 \cdot 3^5 \cdot 7 \cdot 11 \cdot 13 = 30030$
258065,	66597544224,	$2^3 \cdot 3^5 \cdot 59 \cdot 127 = 44958$
259199,	67184121600,	$2^3 \cdot 3^5 \cdot 19 \cdot 359 = 204630$
275561,	75933864720,	$2^3 \cdot 3^5 \cdot 7 \cdot 83 = 17430$
281249,	79101000000,	$2^3 \cdot 3^5 \cdot 11 \cdot 17 \cdot 47 = 263670$
297755,	88658040024,	$2^3 \cdot 3^5 \cdot 53 \cdot 919 = 292242$
360449,	129923481600,	$2^3 \cdot 3^5 \cdot 11 \cdot 89 = 29370$
415151,	172350352800,	$2^3 \cdot 3^5 \cdot 19 \cdot 23 \cdot 31 = 406410$
433025,	187510650624,	$2^3 \cdot 3^5 \cdot 11 \cdot 17 \cdot 199 = 223278$
439001,	192721878000,	$2^3 \cdot 3^5 \cdot 29 \cdot 439 = 381930$
442367,	195688562688,	$2^3 \cdot 3^5 \cdot 29 \cdot 263 = 45762$
456191,	208110228480,	$2^3 \cdot 3^5 \cdot 7 \cdot 11 \cdot 19 = 43890$
511757,	261895227048,	$2^3 \cdot 3^5 \cdot 7 \cdot 13 \cdot 373 = 203658$
526337,	277030637568,	$2^3 \cdot 3^5 \cdot 19 \cdot 257 = 29298$

538001,	289445076000,	$2^3 \cdot 3 \cdot 5 \cdot 41 \cdot 269 = 330870$
595349,	354440431800,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 107 = 292110$
628865,	395471188224,	$2^3 \cdot 3 \cdot 7 \cdot 17 \cdot 23 \cdot 31 = 509082$
663551,	440299929600,	$2^3 \cdot 3 \cdot 5 \cdot 23 \cdot 577 = 398130$
672281,	451961742960,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 17 = 46410$
692225,	479175450624,	$2^3 \cdot 3 \cdot 13 \cdot 4273 = 333294$
715823,	512402567328,	$2^3 \cdot 3 \cdot 71 \cdot 1657 = 705882$
778751,	606453120000,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 89 = 242970$
780449,	609100641600,	$2^3 \cdot 3 \cdot 5 \cdot 11 \cdot 29 \cdot 43 = 411510$
795905,	633464769024,	$2^3 \cdot 3 \cdot 17 \cdot 3109 = 317118$
802817,	644515135488,	$2^3 \cdot 3 \cdot 7 \cdot 14867 = 624414$
816641,	666902522880,	$2^3 \cdot 3 \cdot 5 \cdot 11 \cdot 29 \cdot 71 = 679470$
830465,	689672116224,	$2^3 \cdot 3 \cdot 7 \cdot 13 \cdot 811 = 442806$
845153,	714283593408,	$2^3 \cdot 3 \cdot 7 \cdot 11 \cdot 37 \cdot 47 = 803418$
902501,	814508055000,	$2^3 \cdot 3 \cdot 5 \cdot 19 \cdot 619 = 352830$
907925,	824327805624,	$2^3 \cdot 3 \cdot 61 \cdot 389 = 142374$
911249,	830374740000,	$2^3 \cdot 3 \cdot 5 \cdot 13 \cdot 337 = 131430$
943937,	891017059968,	$2^3 \cdot 3 \cdot 7 \cdot 43 \cdot 229 = 413574$
964895,	931022361024,	$2^3 \cdot 3 \cdot 7 \cdot 19 \cdot 23 \cdot 41 = 752514$
983039,	966365675520,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 1433 = 300930$
1024001,	1048578048000,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 43 = 9030$
1062881,	1129716020160,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 13 \cdot 73 = 199290$
1098305,	1206273873024,	$2^3 \cdot 3 \cdot 11 \cdot 43 \cdot 131 = 371778$
1226177,	1503510035328,	$2^3 \cdot 3 \cdot 7 \cdot 17 \cdot 23 \cdot 29 = 476238$
1240577,	1539031292928,	$2^3 \cdot 3 \cdot 41 \cdot 2423 = 596058$
1246589,	1553984134920,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 19 \cdot 211 = 841890$
1272833,	1620103845888,	$2^3 \cdot 3 \cdot 11 \cdot 97 \cdot 113 = 723426$
1283201,	1646604806400,	$2^3 \cdot 3 \cdot 5 \cdot 89 \cdot 401 = 1070670$
1336337,	1785796577568,	$2^3 \cdot 3 \cdot 17 \cdot 73 \cdot 113 = 841398$
1349633,	1821509234688,	$2^3 \cdot 3 \cdot 11 \cdot 13 \cdot 659 = 565422$
1354751,	1835350272000,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 5419 = 1137990$
1376255,	1894077825024,	$2^3 \cdot 3 \cdot 7 \cdot 11 \cdot 47 = 21714$
1431431,	2048994707760,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 11 \cdot 13 \cdot 47 = 1411410$
1524095,	2322865569024,	$2^3 \cdot 3 \cdot 7 \cdot 11 \cdot 13 \cdot 73 = 438438$
1712501,	2932659675000,	$2^3 \cdot 3 \cdot 5 \cdot 11 \cdot 31 \cdot 137 = 1401510$
1714751,	2940370992000,	$2^3 \cdot 3 \cdot 5 \cdot 13 \cdot 19 \cdot 229 = 1696890$
1721249,	2962698120000,	$2^3 \cdot 3 \cdot 5 \cdot 17 \cdot 19 \cdot 149 = 1443810$
1781249,	3172848000000,	$2^3 \cdot 3 \cdot 5 \cdot 7 \cdot 19 \cdot 71 = 283290$

1843199,	3397382553600,	$2^*3^*5^*7^*31^*137=891870$
1850201,	3423243740400,	$2^*3^*5^*11^*29^*47=449790$
1882385,	3543373288224,	$2^*3^*7^*11^*3169=1464078$
1996001,	3984019992000,	$2^*3^*5^*37^*499=553890$
2024999,	4100620950000,	$2^*3^*5^*59^*131=231870$
2093057,	4380887605248,	$2^*3^*7^*11^*31^*73=1045506$
2218751,	4922856000000,	$2^*3^*5^*71^*107=227910$
2261249,	5113247040000,	$2^*3^*5^*11^*67^*73=1614030$
2371841,	5625629729280,	$2^*3^*5^*11^*17^*109=611490$
2426111,	5886014584320,	$2^*3^*5^*13^*19^*113=837330$
2433401,	5921440426800,	$2^*3^*5^*23^*1669=1151610$
2450087,	6002926307568,	$2^*3^*19^*107^*199=2427402$
2550251,	6503780163000,	$2^*3^*5^*101^*461=1396830$
2618999,	6859155762000,	$2^*3^*5^*19^*41^*97=2266890$
2725001,	7425630450000,	$2^*3^*5^*7^*89^*109=2037210$
2834351,	8033545591200,	$2^*3^*5^*56687=1700610$
2862251,	8192480787000,	$2^*3^*5^*43^*107=138030$
2882465,	8308604476224,	$2^*3^*13^*41^*659=2107482$
2952449,	8716955097600,	$2^*3^*5^*19^*607=345990$
3014657,	9088156827648,	$2^*3^*23^*6203=856014$
3130001,	9796906260000,	$2^*3^*5^*139^*313=1305210$
3429215,	11759515516224,	$2^*3^*7^*47^*191=377034$
3512321,	12336398807040,	$2^*3^*5^*7^*11^*73=168630$
3548447,	12591476111808,	$2^*3^*11^*31^*37^*43=3255186$
3694085,	13646263987224,	$2^*3^*11^*31^*691=1413786$
3792257,	14381213154048,	$2^*3^*13^*17^*43^*53=3021954$
3906251,	15258796875000,	$2^*3^*5^*7^*5167=1085070$
4000751,	16006008564000,	$2^*3^*5^*7^*13^*1231=3360630$
4046849,	16376986828800,	$2^*3^*5^*13^*17^*19^*23=2897310$
4194305,	17592194433024,	$2^*3^*43^*5419=1398102$
4687499,	21972646875000,	$2^*3^*5^*47^*1061=1496010$
4691555,	22010688318024,	$2^*3^*7^*19^*977=779646$
4899851,	24008539822200,	$2^*3^*5^*43^*53^*71=4854270$
5458751,	29797962480000,	$2^*3^*5^*11^*13^*397=1703130$
5544449,	30740914713600,	$2^*3^*5^*7^*13^*17^*37=1717170$
5771249,	33307315020000,	$2^*3^*5^*7^*19^*227=905730$
5786801,	33487065813600,	$2^*3^*5^*7^*17^*23^*37=3038070$

5848415, 34203958012224, $2^*3^*7^*11^*13^*967=5807802$

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Appendix 3: Odd number $6K+1$ and equality $1+ ((6K+1)^2 - 1) = (6K+1)^2$ satisfying $6K+1 > (\text{Rad } ((6K+1)^2 - 1))^{1+\varepsilon}$ after the evaluations of headmost $6K+1$ are listed as follows, but real numbers which satisfy ε of each inequality are incomplete alike.

$6K+1$	$(6K+1)^2 - 1,$	$\text{Rad}((6K+1)^2 - 1)$
7,	48,	$2^*3=6$
31,	960,	$2^*3^*5=30$
49,	2400,	$2^*3^*5=30$
55,	3024,	$2^*3^*7=42$
97,	9408,	$2^*3^*7=42$
127,	16128,	$2^*3^*7=42$
487,	237168,	$2^*3^*61=366$
511,	261120,	$2^*3^*5^*17=510$
577,	332928,	$2^*3^*17=102$
649,	421200,	$2^*3^*5^*13=390$
721,	519840,	$2^*3^*5^*19=570$
1249,	1560000,	$2^*3^*5^*13=390$
1351,	1825200,	$2^*3^*5^*13=390$
1567,	2455488,	$2^*3^*7^*29=1218$
1921,	3690240,	$2^*3^*5^*31=930$
1999,	3996000,	$2^*3^*5^*37=1110$
2047,	4190208,	$2^*3^*11^*31=2046$
2431,	5909760,	$2^*3^*5^*19=570$
4375,	19140624,	$2^*3^*547=3282$
4801,	23049600,	$2^*3^*5^*7=210$
4999,	24990000,	$2^*3^*5^*7^*17=3570$
5617,	31550688,	$2^*3^*13^*53=4134$
6049,	36590400,	$2^*3^*5^*7^*11=2310$
6751,	45576000,	$2^*3^*5^*211=6330$
8191,	67092480,	$2^*3^*5^*7^*13=2730$
8449,	71385600,	$2^*3^*5^*11^*13=4290$
8749,	76545000,	$2^*3^*5^*7=210$

12151,	147646800,	$2^*3^*5^*7^*31=6510$
12799,	163814400,	$2^*3^*5^*79=2370$
13183,	173791488,	$2^*3^*13^*103=8034$
18751,	351600000,	$2^*3^*5^*293=8790$
18817,	354079488,	$2^*3^*7^*97=4074$
21295,	453477024,	$2^*3^*7^*11^*13=6006$
27379,	749609640,	$2^*3^*5^*13^*37=14430$
27649,	764467200,	$2^*3^*5^*7^*79=16590$
29281,	857376960,	$2^*3^*5^*11^*61=20130$
31249,	976500000,	$2^*3^*5^*7^*31=6510$
32257,	1040514048,	$2^*3^*7^*127=5334$
32767,	1073676288,	$2^*3^*43^*127=32766$
33535,	1124596224,	$2^*3^*23^*131=18078$
39367,	1549760688,	$2^*3^*7^*19^*37=29526$
43903,	1927473408,	$2^*3^*7^*271=11382$
51841,	2687489280,	$2^*3^*5^*7^*23=4830$
53137,	2823540768,	$2^*3^*41^*163=40098$
56251,	3164175000,	$2^*3^*5^*7^*41=8610$
57121,	3262808640,	$2^*3^*5^*7^*13^*17=46410$
62425,	3896880624,	$2^*3^*7^*13^*17=9282$
74359,	5529260880,	$2^*3^*5^*11^*13^*17=72930$
79201,	6272798400,	$2^*3^*5^*11^*199=65670$
81919,	6710722560,	$2^*3^*5^*37^*41=45510$
100351,	10070323200,	$2^*3^*5^*7^*223=46830$
110593,	12230811648,	$2^*3^*11^*457=30162$
115249,	13282332000,	$2^*3^*5^*7^*461=96810$
116161,	13493377920,	$2^*3^*5^*11^*241=79530$
117127,	13718734128,	$2^*3^*11^*241=15906$
118099,	13947373800,	$2^*3^*5^*1181=35430$
119071,	14177903040,	$2^*3^*5^*7^*61=12810$
126001,	15876252000,	$2^*3^*5^*7^*251=52710$
131071,	17179607040,	$2^*3^*5^*17^*257=131070$
132097,	17449617408,	$2^*3^*43^*257=66306$
137215,	18827956224,	$2^*3^*7^*11^*67=30954$
143749,	20663775000,	$2^*3^*5^*11^*23=7590$
146881,	21574028160,	$2^*3^*5^*17^*271=138210$
161839,	26191861920,	$2^*3^*5^*7^*17^*37=132090$
167041,	27902695680,	$2^*3^*5^*17^*29=14790$

181249,	32851200000,	$2^*3^*5^*29^*59=51330$
189001,	35721378000,	$2^*3^*5^*7^*11^*71=164010$
196831,	38742442560,	$2^*3^*5^*6151=184530$
202501,	41006655000,	$2^*3^*5^*19^*73=41610$
211249,	44626140000,	$2^*3^*5^*13^*163=63570$
220159,	48469985280,	$2^*3^*5^*43^*151=194790$
221185,	48922804224,	$2^*3^*7^*37^*61=94794$
227137,	51591216768,	$2^*3^*7^*13^*337=184002$
235297,	55364678208,	$2^*3^*7^*19^*43=34314$
236671,	56013162240,	$2^*3^*5^*7^*23^*43=207690$
244903,	59977479408,	$2^*3^*7^*11^*17^*23=180642$
260641,	67933730880,	$2^*3^*5^*19^*181=103170$
262087,	68689595568,	$2^*3^*11^*19^*181=226974$
285769,	81663921360,	$2^*3^*5^*7^*17^*41=146370$
302527,	91522585728,	$2^*3^*7^*29^*163=198534$
312499,	97655625000,	$2^*3^*5^*643=19290$
320761,	102887619120,	$2^*3^*5^*11^*13^*73=313170$
330751,	109396224000,	$2^*3^*5^*7^*17^*19=67830$
337501,	113906925000,	$2^*3^*5^*11^*23^*29=220110$
354295,	125524947024,	$2^*3^*67^*661=265722$
373249,	139314816000,	$2^*3^*5^*1493=44790$
403201,	162571046400,	$2^*3^*5^*7^*449=94290$
406783,	165472409088,	$2^*3^*7^*31^*227=295554$
470449,	221322261600,	$2^*3^*5^*11^*97=32010$
474337,	224995589568,	$2^*3^*61^*487=178242$
500095,	250095009024,	$2^*3^*7^*3907=164094$
522241,	272735662080,	$2^*3^*5^*7^*17^*73=260610$
524287,	274876858368,	$2^*3^*7^*19^*73=58254$
546751,	298936656000,	$2^*3^*5^*8543=256290$
559681,	313242821760,	$2^*3^*5^*11^*23^*53=402270$
559873,	313457776128,	$2^*3^*7^*29^*197=239946$
583201,	340123406400,	$2^*3^*5^*17^*1009=514590$
661249,	437250240000,	$2^*3^*5^*7^*23^*41=198030$
665335,	442670662224,	$2^*3^*7^*37^*109=169386$
665857,	443365544448,	$2^*3^*17^*577=58854$
702463,	493454266368,	$2^*3^*7^*47^*53=104622$
781249,	610350000000,	$2^*3^*5^*13^*313=122070$
818749,	670349925000,	$2^*3^*5^*7^*19^*131=522690$

826687,	683411395968,	$2^*3^*7^*12917=542514$
842401,	709639444800,	$2^*3^*5^*11^*13^*59=253110$
907741,	823993723080,	$2^*3^*5^*11^*31^*41=419430$
913951,	835306430400,	$2^*3^*5^*13^*677=264030$
919999,	846398160000,	$2^*3^*5^*23^*631=435390$
938449,	880686525600,	$2^*3^*5^*7^*19^*137=546630$
966655,	934421889024,	$2^*3^*13^*17^*59=78234$
988417,	976968165888,	$2^*3^*11^*13^*19^*37=603174$
1039681,	1080936581760,	$2^*3^*5^*7^*19^*103=410970$
1059967,	1123530041088,	$2^*3^*7^*13^*727=396942$
1102249,	1214952858000,	$2^*3^*5^*7^*4409=925890$
1102735,	1216024480224,	$2^*3^*41^*2269=558174$
1128001,	1272386256000,	$2^*3^*5^*47^*751=1058910$
1179649,	1391571763200,	$2^*3^*5^*23593=707790$
1202851,	1446850528200,	$2^*3^*5^*7^*11^*17^*19=746130$
1229311,	1511205534720,	$2^*3^*5^*7^*29^*157=956130$
1370929,	1879446323040,	$2^*3^*5^*11^*13^*103=441870$
1387777,	1925925001728,	$2^*3^*7^*13^*17^*139=1290198$
1417177,	2008390649328,	$2^*3^*7^*14461=607362$
1434817,	2058699823488,	$2^*3^*7^*11^*47^*53=1150842$
1518751,	2306604600000,	$2^*3^*5^*31^*1531=1423830$
1555849,	2420666110800,	$2^*3^*5^*7^*29^*37=225330$
1581229,	2500285150440,	$2^*3^*5^*7^*11^*461=1064910$
1653751,	2734892370000,	$2^*3^*5^*7^*37^*151=1173270$
1685503,	2840920363008,	$2^*3^*7^*13^*823=449358$
1823509,	3325185073080,	$2^*3^*5^*13^*37^*83=1197690$
1831249,	3353472900000,	$2^*3^*5^*157^*293=1380030$
1847041,	3411560455680,	$2^*3^*5^*13^*31^*37=447330$
1915999,	3671052168000,	$2^*3^*5^*7^*19^*479=1911210$
1999999,	3999996000000,	$2^*3^*5^*7^*11^*13^*37=1111110$
2086399,	4353060787200,	$2^*3^*5^*53^*163=259170$
2097151,	4398042316800,	$2^*3^*5^*11^*31^*41=419430$
2101249,	4415247360000,	$2^*3^*5^*19^*41=23370$
2234497,	4992976843008,	$2^*3^*7^*11^*23^*151=1604526$
2281249,	5204097000000,	$2^*3^*5^*73^*89=194910$
2367487,	5604994695168,	$2^*3^*11^*17^*1087=1219614$
2400001,	5760004800000,	$2^*3^*5^*11^*43^*59=837210$
2456245,	6033139500024,	$2^*3^*7^*13^*19^*43=446082$

2649601,	7020385459200,	$2^*3^*5^*23^*1151=794190$
2655505,	7051706805024,	$2^*3^*7^*79^*683=2266194$
2739199,	7503211161600,	$2^*3^*5^*7^*11^*107=247170$
2898919,	8403731368560,	$2^*3^*5^*11^*23^*137=1039830$
2957311,	8745688350720,	$2^*3^*5^*19^*1217=693690$
2965951,	8796865334400,	$2^*3^*5^*11^*13^*383=1643070$
2970343,	8822937537648,	$2^*3^*13^*17^*571=757146$
3001249,	9007495560000,	$2^*3^*5^*7^*17^*613=2188410$
3114751,	9701673792000,	$2^*3^*5^*23^*4153=2865570$
3120001,	9734406240000,	$2^*3^*5^*13^*1249=487110$
3188647,	10167469690608,	$2^*3^*398581=2391486$
3271681,	10703896565760,	$2^*3^*5^*71^*1279=2724270$
3483649,	12135810355200,	$2^*3^*5^*7^*19^*193=770070$
3529471,	12457165539840,	$2^*3^*5^*7^*17^*811=2895270$
3543121,	12553706420640,	$2^*3^*5^*7^*11^*19^*37=1623930$
3650401,	13325427460800,	$2^*3^*5^*7^*13^*193=526890$
3684751,	13577389932000,	$2^*3^*5^*17^*41^*137=2864670$
3704401,	13722586768800,	$2^*3^*5^*7^*13^*17^*29=1345890$
3748321,	14049910319040,	$2^*3^*5^*19^*37^*137=2889330$
3781249,	14297844000000,	$2^*3^*5^*11^*43^*229=3249510$
3786751,	14339483136000,	$2^*3^*5^*11^*17^*43=241230$
3909631,	15285214556160,	$2^*3^*5^*19^*23^*83=1088130$
4176049,	17439385250400,	$2^*3^*5^*17^*19^*241=2335290$
4218751,	17797860000000,	$2^*3^*5^*23^*1433=988770$
4245697,	18025943015808,	$2^*3^*7^*13^*31^*47=795522$
4257361,	18125122684320,	$2^*3^*5^*73^*1459=3195210$
4605823,	21213605507328,	$2^*3^*13^*35983=2806674$
4620799,	21351783398400,	$2^*3^*5^*7^*13^*19^*31=1607970$
4910977,	24117695094528,	$2^*3^*7^*29^*1567=1908606$
5030911,	25310065489920,	$2^*3^*5^*17^*6211=3167610$
5038849,	25389999244800,	$2^*3^*5^*179^*563=3023310$
5126401,	26279987212800,	$2^*3^*5^*89^*1601=4274670$
5196799,	27006719846400,	$2^*3^*5^*7^*17^*29^*37=3830610$
5353777,	28662928165728,	$2^*3^*17^*59^*769=4627842$
5540833,	30700830333888,	$2^*3^*11^*13^*53^*97=4410978$
5651521,	31939689613440,	$2^*3^*5^*7^*29^*41=249690$
5658247,	32015759113008,	$2^*3^*11^*17^*29^*41=1334058$

5918719, 35031234600960, $2^*3^*5^*13^*17^*449=2976870$

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References

- [1] *Wolfram Math world*: <http://mathworld.wolfram.com/abcConjecture.html>
- [2] Robert, Olivier; Stewart, Cameron L.; Tenenbaum, Gérald (2014), "A refinement of the abc conjecture", *Bull. London Math. Soc.* 46 (6): 1156–1166, doi: 10.1112/blms/bdu069.
- [3] Baker, Alan (1998), "Logarithmic forms and the abc-conjecture", In Győry, Kálmán, *Number theory, Diophantine, computational and algebraic aspects, Proceedings of the international conference, Eger, Hungary, July 29-August 2, 1996*. Berlin: de Gruyter, pp. 37–44, ISBN 3-11-015364-5. Zbl 0973.11047
- [4] Baker, Alan (2004), "Experiments on the abc-conjecture". *Publ. Math. Debrecen* 65: 253–260.
- [5] Browkin, Jerzy (2000), "The abc-conjecture", In Bambah, R. P.; Dumir, V. C.; Hans-Gill, R. J. *Number Theory, Trends in Mathematics*. Basel: Birkhäuser, pp. 75–106, ISBN 3-7643-6259-6
- [6] Goldfeld, Dorian (2002). "Modular forms, elliptic curves and the abc-conjecture", In Wüstholz, Gisbert. *A panorama in number theory or The view from Baker's garden, Based on a conference in honor of Alan Baker's 60th birthday, Zürich, Switzerland, 1999*. Cambridge: Cambridge University Press, pp. 128–147. ISBN 0-521-80799-9. Zbl 1046.11035
- [7] Van Frankenhuysen, Machiel (2002). "The ABC conjecture implies Vojta's height inequality for curves", *J. Number Theory* 95 (2): 289–302, doi: 10.1006/jnth.2001.2769. MR 1924103
- [8] Stewart, C. L.; Yu, Kunrui (2001), "On the abc conjecture, II". *Duke Mathematical Journal* 108 (1): 169–181, doi:10.1215/S0012-7094-01-10815-6 .