

**On the numbers  $(n+1) \cdot p - n \cdot q$  where  $p$  and  $q$  primes,  $p$  having the group of its last digits equal to  $q$**

**Abstract.** In this paper I make the following two conjectures: (I) For any prime  $p$ ,  $p > 5$ , there exist a pair of primes  $(q_1, q_2)$ , both having the group of their last digits equal to  $p$ , and a positive integer  $n$ , such that  $p = (n + 1) \cdot q_1 - n \cdot q_2$  (examples: for  $p = 11$ , there exist the primes  $q_1 = 211$  and  $q_2 = 311$  and also the number  $n = 2$  such that  $11 = 3 \cdot 211 - 2 \cdot 311$ ; for  $p = 29$ , there exist the primes  $q_1 = 829$  and  $q_2 = 929$  and also the number  $n = 8$  such that  $29 = 9 \cdot 829 - 8 \cdot 929$ ); (II) For any  $q_1$  prime,  $q_1 > 5$ , and any  $n$  non-null positive integer, there exist an infinity of primes  $q_2$ , having the group of their last digits equal to  $q_1$ , such that  $p = (n + 1) \cdot q_2 - n \cdot q_1$  is prime; (III) For any  $q_1$  prime,  $q_1 > 5$ , and any  $q_2$  prime having the group of its last digits equal to  $q_1$ , there exist an infinity of positive integers  $n$  such that  $p = (n + 1) \cdot q_2 - n \cdot q_1$  is prime.

**Conjecture 1:**

For any prime  $p$ ,  $p > 5$ , there exist a pair of primes  $(q_1, q_2)$ , both having the group of their last digits equal to  $p$ , and a positive integer  $n$ , such that  $p = (n + 1) \cdot q_1 - n \cdot q_2$  (examples: for  $p = 11$ , there exist the primes  $q_1 = 211$  and  $q_2 = 311$  and also the number  $n = 2$  such that  $11 = 3 \cdot 211 - 2 \cdot 311$ ; for  $p = 29$ , there exist the primes  $q_1 = 829$  and  $q_2 = 929$  and also the number  $n = 8$  such that  $29 = 9 \cdot 829 - 8 \cdot 929$ ).

The pairs of primes  $(q_1, q_2)$  for  $p > 5$ :

- : for  $p = 7$ ,  $(q_1, q_2) = (37, 47)$  because  $4 \cdot 37 - 3 \cdot 47 = 7$ ;
- : for  $p = 11$ ,  $(q_1, q_2) = (211, 311)$  because  $3 \cdot 211 - 2 \cdot 311 = 7$ ;
- : for  $p = 13$ ,  $(q_1, q_2) = (1013, 1213)$  because  $6 \cdot 1013 - 5 \cdot 1213 = 13$ ;
- : for  $p = 17$ ,  $(q_1, q_2) = (1117, 1217)$  because  $12 \cdot 1117 - 11 \cdot 1217 = 17$ ;
- : for  $p = 19$ ,  $(q_1, q_2) = (419, 619)$  because  $3 \cdot 419 - 2 \cdot 619 = 19$ ;
- : for  $p = 23$ ,  $(q_1, q_2) = (1123, 1223)$  because  $12 \cdot 1123 - 11 \cdot 1223 = 23$ ;
- : for  $p = 29$ ,  $(q_1, q_2) = (829, 929)$  because  $9 \cdot 829 - 8 \cdot 929 = 29$ ;
- : for  $p = 31$ ,  $(q_1, q_2) = (331, 431)$  because  $4 \cdot 331 - 3 \cdot 431 = 19$ ;
- (...)

## Conjecture 2:

For any  $q_1$  prime,  $q_1 > 5$ , and any  $n$  non-null positive integer, there exist an infinity of primes  $q_2$ , having the group of their last digits equal to  $q_1$ , such that  $p = (n + 1) \cdot q_2 - n \cdot q_1$  is prime.

The sequence of primes  $p$  for  $q_1 = 7$ ,  $n = 1$ :

: 67 (=  $2 \cdot 37 - 1 \cdot 7$ ), 127 (=  $2 \cdot 67 - 1 \cdot 7$ ), 307 (=  $2 \cdot 157 - 7$ )..., corresponding to  $q_2 = 37, 67, 157$  (...)

The sequence of primes  $p$  for  $q_1 = 7$ ,  $n = 2$ :

: 37 (=  $3 \cdot 17 - 2 \cdot 7$ ), 97 (=  $3 \cdot 37 - 2 \cdot 7$ ), 127 (=  $3 \cdot 47 - 2 \cdot 7$ )..., corresponding to  $q_2 = 17, 37, 47$  (...)

The sequence of primes  $p$  for  $q_1 = 7$ ,  $n = 4$ :

: 47 (=  $4 \cdot 17 - 3 \cdot 7$ ), 127 (=  $4 \cdot 37 - 3 \cdot 7$ ), 167 (=  $4 \cdot 47 - 3 \cdot 7$ ), corresponding to  $q_2 = 17, 37, 47$  (...)

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The sequence of primes  $p$  for  $q_1 = 11$ ,  $n = 1$ :

: 1811 (=  $2 \cdot 911 - 1 \cdot 11$ ), 3011 (=  $2 \cdot 1511 - 1 \cdot 11$ ), 4211 (=  $2 \cdot 2111 - 1 \cdot 11$ )..., corresponding to  $q_2 = 911, 1511, 2111$  (...)

The sequence of primes  $p$  for  $q_1 = 11$ ,  $n = 2$ :

: 911 (=  $3 \cdot 311 - 2 \cdot 11$ ), 2411 (=  $3 \cdot 811 - 2 \cdot 11$ ), 2711 (=  $3 \cdot 911 - 2 \cdot 11$ )..., corresponding to  $q_2 = 311, 811, 911$  (...)

The sequence of primes  $p$  for  $q_1 = 11$ ,  $n = 3$ :

: 811 (=  $4 \cdot 211 - 3 \cdot 11$ ), 6011 (=  $4 \cdot 1511 - 3 \cdot 11$ ), 7211 (=  $4 \cdot 1811 - 3 \cdot 11$ ), corresponding to  $q_2 = 211, 1511, 1811$  (...)

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The sequence of primes  $p$  for  $q_1 = 97$ ,  $n = 3$ :

: 3697 (=  $4 \cdot 997 - 3 \cdot 97$ ), 27697 (=  $4 \cdot 6997 - 3 \cdot 97$ ), 55697 (=  $4 \cdot 13997 - 3 \cdot 97$ ), 79697 (=  $4 \cdot 19997 - 3 \cdot 97$ ), 87697 (=  $4 \cdot 21997 - 3 \cdot 97$ )..., corresponding to  $q_2 = 997, 6997, 13997, 21997$  (...)

**Conjecture 3:**

For any  $q_1$  prime,  $q_1 > 5$ , and any  $q_2$  prime having the group of its last digits equal to  $q_1$ , there exist an infinity of positive integers  $n$  such that  $p = (n + 1) \cdot q_2 - n \cdot q_1$  is prime.

The sequence of primes  $p$  for  $(q_1, q_2) = (11, 211)$ :

: 811 (=  $4 \cdot 211 - 3 \cdot 11$ ), 1811 (=  $9 \cdot 211 - 8 \cdot 11$ ), 2011 (=  $10 \cdot 211 - 9 \cdot 11$ ), 2411 (=  $12 \cdot 211 - 11 \cdot 11$ )...  
corresponding to  $n = 3, 8, 9, 11$  (...)