Dynamic Quantum Vacuum and Relativity

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Abstract

A model of a three-dimensional quantum vacuum with variable energy density is proposed. In this model, time we measure with clocks is only a mathematical parameter of material changes, i.e. motion in quantum vacuum. Inertial mass and gravitational mass have origin in dynamics between a given particle or massive body and diminished energy density of quantum vacuum. Each elementary particle is a structure of quantum vacuum and diminishes quantum vacuum energy density. Symmetry "particle – diminished energy density of quantum vacuum" is the fundamental symmetry of the universe which gives origin to mass and gravity. Special relativity's Sagnac effect in GPS system and important predictions of general relativity such as precessions of the planets, the Shapiro time delay of light signals in a gravitational field and the geodetic and frame-dragging effects recently tested by Gravity Probe B, have origin in the dynamics of the quantum vacuum which rotates with the earth. Gravitational constant G_N and velocity of light *c* have small deviations of their value which are related to the variable energy density of quantum vacuum.

Key words: energy density of quantum vacuum, Sagnac effect, relativity, dark energy, Mercury precession, symmetry, gravitational constant.

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1. Introduction

The idea of 19th century physics that space is filled with "ether" did not get experimental prove in order to remain a valid concept of today physics. The concept of ether was expelled from physics in the light of the null result of Michelson-Morley experiment, which led to the prevailing opinion, during 20th century, that photons can move in an empty space which has no physical origin. However, the idea that material objects can exist in some empty space has created some unsolvable problems regarding the description of Sagnac effect in Global Positioning System (GPS), as well as the interpretation of mass and gravity.

On the other hand, 20th century theoretical physics brought the idea of a quantum vacuum as a fundamental medium subtending the observable forms of matter, energy and space-time. According to the Standard Model, the total vacuum energy density has at least the following three contributions: the fluctuations characterizing the zero-point field, the fluctuations characterizing the quantum chromodynamic level of sub-nuclear physics and the fluctuations linked with the Higgs field. Moreover, one can speculate that there are also contributions from possible existing sources outside the Standard Model (for instance, grand unification theories, string theories, etc…). The missing point inside the physics of 20th century is that a region of universal space which theoretically is void of all fields, elementary particles and massive objects still exists on its own and so must have some concrete physical origin. The so called "empty space" is a type of energy that is "full" of itself, has its independent physical existence. We do not suggest the necessity to "resurrect" the idea of ether here, we just point out that the concept of "empty space" deprived of physical properties represents an a-priory accepted concept in the physics of 20^{th} century.

The existence of a fundamental medium, able to reproduce the dynamical features of a concrete universal space and, in reality, constituting the deepest essence of universal space itself, is an ontological necessity in order to obtain General Relativity as the mathematical description, in the low energy – long wavelength limit, of the space elementary structure and to create the bridge between Quantum Mechanics and General Relativity. This could finally lead to a consistent theory of quantum gravity, in which the quantization will be made on a field function describing the quantum vacuum and not on collective macroscopic variables constructed from it, as in all the proposed and commonly accepted alternative theories of quantum gravity.

As regards the role of the different contributions to the vacuum energy density, Timashev examined the possibility of considering the physical vacuum as a unified system governing the processes taking place in microphysics and macrophysics [1]. We have explored recently this possibility by introducing, on the basis of the Planckian metric emerging, for example, from loop quantum gravity [2, 3, 4], a model of a three-dimensional (3D) dynamic quantum vacuum (DQV) whose energy density is derived from Planck units. In our model DQV is a fundamental energy of the universe which cannot be created and cannot be destroyed. All different particles are different "structures" of DQV. A given particle diminishes energy density of DQV with respect to its energy. Symmetry between a given particle or massive body as a "structured DQV" and the region of diminished energy density around it is a fundamental symmetry of the universe which generates inertial and gravitational mass in microphysics and in macrophysics. In our model time is a fundamental quantity of the universe which has only a mathematical existence, namely numerical order of changes [5, 6]. Moreover, on the basis of this model, the curvature of space-time in general relativity emerges, in the hydrodynamic limit of some underlying theory of a microscopic structure of space-time, as a mathematical value of a more fundamental actual energy density of quantum vacuum. The fluctuations of the quantum vacuum energy density generate a curvature of space-time similar to the curvature produced by a "dark energy" density and produce a shadowing of the gravitational space which determines the motion of other material objects present in the region under consideration [6]. In other words, one can say that, in this model, dark energy is energy of quantum vacuum itself. It is not that some unknown energy exists in universal space. Energy of universal space which originates from fluctuations of quantum vacuum is dark energy.

According to the view suggested in this paper, a three-dimensional DQV (characterized by a symmetry between particles and variations of DQV energy density) can be considered as the fundamental arena of the universe. In particular, here we will show that both special relativity's Sagnac effect and significant general relativistic predictions (such as precession of the planets, the Shapiro time delay of light signals in a gravitational field, the geodetic and frame-dragging effect recently tested by Gravity Probe B) have origin in a "dragging" effect of DQV with the rotating earth, which allows us to obtain results in complete agreement with those of Einstein.

In GPS relativity of clocks rate (associated to a special relativistic effect and a general relativistic effect) also has origin in variable energy density of DQV. Less DQV energy is dense slower is rate of clocks, namely slower is the speed of material changes. Relativistic mass of a given particle is also a result of additional lower energy density of DVQ and additional absorption of quantum vacuum energy due to its high velocity. In this model velocity of light all over universe is constant with a minimal variation which depends of the variable energy density of DQV (in agreement with Shapiro effect).

A given material object, stellar object or particle cannot be examined separately from the region of diminished quantum vacuum energy density which is moving with it. An extended region of diminished energy density of quantum vacuum around the earth is moving with the earth. In this picture, the null result of Michelson-Morley experiment is determined by the motion effect of the region of diminished quantum vacuum energy density around the earth with the earth.

According to the research of Mosanori Sato GPS system functions because Earth rotates in the fixed ether. GPS experiment showed that the ether-wind was not observed at least up to 20,000 km from the ground level. The GPS experiments show that if there is ether-dragging, it will be observed as an ether-wind more than 20,000 km from the ground level [7]. In our model DQV is the medium of light propagation, which Mosanori names "ether". We suppose Michelson-Morley experiment will not give null result on the satellite which is more than 20.000 km distant from the earth (see figure 1).

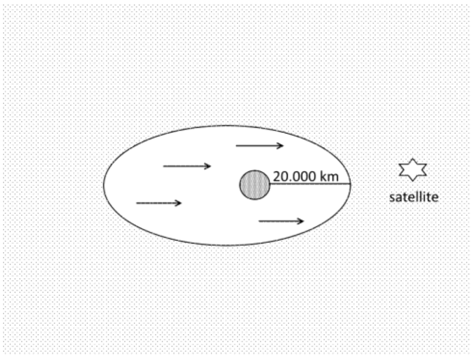
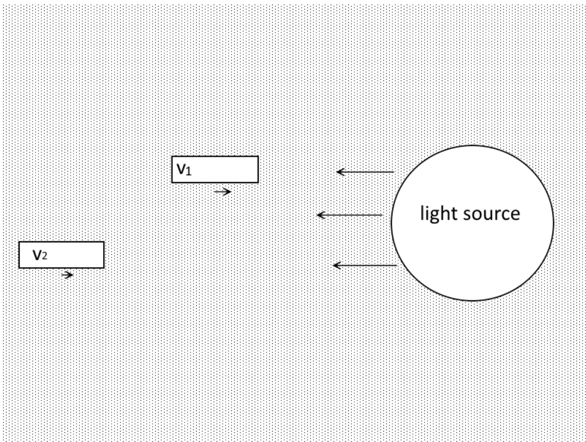


Figure 1.: Region of diminished energy density of DQV is moving with the earth.

In special relativity light has a constant velocity in all inertial systems regardless their motion because light is a vibration (excitation) of DQV and all inertial systems move in DQV. Frequency of light from a given source is variable in inertial systems with different velocity because of Doppler effect (see figure 2):



$c_1 = c_2$

$v_1 \succ v_2 \rightarrow \gamma_1 \succ \gamma_2$

Figure 2: Constancy of *c* and variability of light frequency in Special Relativity.

The paper is structured in the following manner. In chapter 2 we will review the interpretation of mass and gravity in the 3D quantum vacuum model proposed by the authors in the papers [5, 6], focusing the attention on the equivalence between the fluctuations of the quantum vacuum energy density and the curvature produced by the dark energy density and, then, we will introduce the concept of the "dragging" phenomenon of a region of 3D quantum vacuum determined by the changes of its energy density. In chapter 3 we will analyse the Sagnac effect in the context of the 3D quantum vacuum model. In chapter 4 we will explore the role of the "dragging" effect of the quantum vacuum as regards precessions of the planets. In chapter 5 we will analyse the re-reading provided by the 3D quantum vacuum model of the Shapiro time delay of light signals in a gravitational field, as well as of the geodetic and frame-dragging effects recently tested by Gravity Probe B. In chapter 6 we will introduce a possible link between quantum vacuum energy density and relative velocity of clocks. In chapter 7 we will analyze the variability of gravitational constant in the dynamic quantum vacuum model. Finally, in chapter 8 we will make some cosmologic considerations in the dynamic quantum vacuum model.

2. Inertial mass, gravitational mass, energy density of quantum vacuum and dark energy

In a given physical system, energy has a tendency for homogeneous distribution. In a given volume *V* of universal space the total sum of the different forms of energies tends to be constant:

$$\frac{E_{qv}+E_{el}+E_m}{V}=K \quad (1)$$

where E_{qv} is energy of quantum vacuum, E_m is energy of matter and E_{el} is electromagnetic energy [8]. Quantum vacuum is *dynamic* in the sense that presence of a given stellar object or elementary particle reduces the amount of the quantum vacuum energy.

In the absence of elementary particles, atoms and massive objects, energy density of quantum vacuum is defined by the following relation:

$$\rho_{pE}=\frac{m_p \cdot c^2}{l_p^3} \quad (2),$$

where m_p is Planck mass, and l_p is Planck length. The quantity (2) is the maximum value of the quantum vacuum energy density and physically corresponds to the total average volumetric energy density, owed to all the frequency modes possible within the visible size of the universe, expressed by

$$\rho_{pE}=\sqrt{\frac{c^{14}}{\hbar^2 G^4}} \approx 4{,}641266\cdot 10^{113} J/m^3 \cong 10^{97} Kg/m^3 \quad (3).$$

The quantum vacuum energy density (3) is usually considered as the origin of the dark energy and thus of a cosmological constant, if the dark energy is supposed to be owed to an interplay between quantum mechanics and gravity. However the observations are compatible with a dark energy density

$$\rho_{DE} \cong 10^{-26} Kg/m^3 \quad (4)$$

and thus equations (3) and (4) give rise to the so-called "cosmological constant problem" because the dark energy (4) is 123 orders of magnitude larger than (3). In order to solve this problem, Santos proposed an explanation for the actual value (4) which invokes the fluctuations of the quantum vacuum [9]. In Santos' approach ρ_{DE} is the effect of the quantum vacuum fluctuations on the curvature of space-time according to equations

$$\rho_{DE} \cong 70G\int_0^\infty C(s)s\,ds \quad (5)$$

where $C(s)$ is a two-point correlation function of vacuum density fluctuations. In analogy with a suggestion of Zeldovich [10], the observed value of the dark energy density (4) may also be reproduced by proposing that an elementary particle with frequency $\omega = Gm^3c/\hbar^2$ determines a gravitational energy density due to dark matter given by

$\rho_{DE}c^2 \cong \hbar\omega / r_c^3$ (6)
where $r_c = \hbar / mc$ is its Compton's radius.

Moreover, in the picture of Rueda's and Haisch's interpretation of the inertial mass as an effect of the electromagnetic quantum vacuum [11], the presence of a particle with a volume V_0 expels from the vacuum energy within this volume exactly the same amount of energy as is the particle's internal energy (equivalent to its rest mass) according to relation

$$m_0 = \frac{V_0}{c^2}\int \eta(\omega)\frac{\hbar\omega^3}{2\pi^2 c^3}d\omega \quad (7)$$

where the dimensionless parameter $\eta(\omega)$ represents the frequency dependent part of the scattering of the energy flux (namely the gauge factor).

Taking account of Santos' results and of Rueda's and Haisch's results, one can consider that each elementary particle is associated with fluctuations of the quantum vacuum which determine a diminishing of the quantum vacuum energy density. The physical property of mass derives from an opportune change of the energy density of quantum vacuum: each material object endowed with a mass *m* is produced by a change of the quantum vacuum energy density on the basis of equation

$$m = \frac{V \cdot \Delta\rho_{qvE}}{c^2} \quad (8),$$

where $\Delta\rho_{qvE} = \rho_{pE} - \rho_{qvE}$,

$$\rho_{qvE} = \rho_{pE} - \frac{m \cdot c^2}{V} = \rho_{pE} - \frac{3m \cdot c^2}{4\pi \cdot r^3} \quad (9),$$

where *m* is the mass of the object and *r* is the radius of the object.

Formalism 9 expresses energy density of quantum vacuum in the centre of the material object under consideration. On the basis of equation (9), energy density of quantum vacuum constitutes an ontologically primary physical reality with respect to mass.

Going away from the centre of a given material object energy density of quantum vacuum increases according to the following formalism:

$$\rho_{qvE} = \rho_{pE} - \frac{3m \cdot c^2}{4\pi(r+d)^3} \quad (10),$$

where m is the mass of the material object, r is radius of material object and d is the distance from the centre of the material object to a given point T (see figure 3). When $d = 0$ one gets energy density of QDV in the centre. When $d = r$ one gets energy density of DQV on the surface of the stellar object. When $d \to \infty$ one gets energy density of QDV in intergalactic empty space far away from stellar objects.

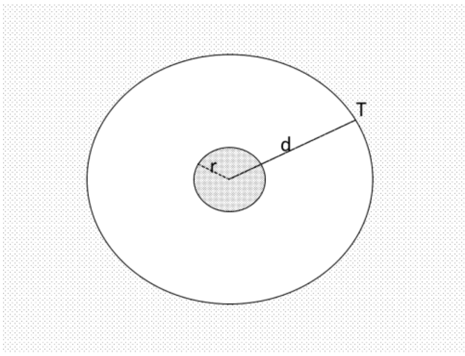


Figure 3: Density of DQV in the centre, on the surface and distant from a stellar object.

Inside the Schwarzschild radius

$r_s = \frac{2Gm}{c^2}$ (11),

where G is the gravitational constant and m is the mass of a stellar object, the energy density of quantum vacuum is at the minimum and constant. Combining equations (9) and (11) we get the following expression for the energy density of quantum vacuum inside Schwarzschild radius:

$$\rho_{qvE} = \rho_{pE} - \frac{c^8}{8\pi G^3 m^2} \quad (12).$$

In black holes energy density of quantum vacuum is at its minimum and under its value which is required for stability of elementary particles. Each particle is un-dividedly related to its region of diminished energy density of DQV. Inside Schwarzschild radius low energy density of quantum vacuum does not provide a necessary quantum vacuum "background" for stability of elementary particles and stability of atoms. That is why inside Schwarzschild radius matter transforms back in electromagnetic energy and this back to energy of quantum vacuum.

In outer intergalactic space energy density of quantum vacuum is at its maximum. Energy of quantum vacuum is forming in electromagnetic waves, called "cosmic radiation" [12] and this further in elementary particles. This circulation of energy in the universe is in permanent dynamic equilibrium. In this picture, universe is not a created system and will not have an end. It is an utter misunderstanding to compare universe and life with man-made machines which are ruled by second law of thermodynamics. Energy of DQV is not created and cannot be destroyed.

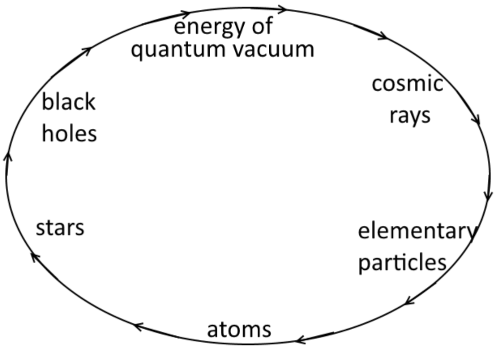


Figure 4: Permanent circulation of energy in the universe.

The presence of a material object diminishes the energy density of quantum vacuum. Energy density of quantum vacuum is increasing with a distance from a given material object. The higher energy density of quantum vacuum around is pushing towards lower energy density and this pressure is the origin of the inertial and gravitational mass and their equality (see figure 5).

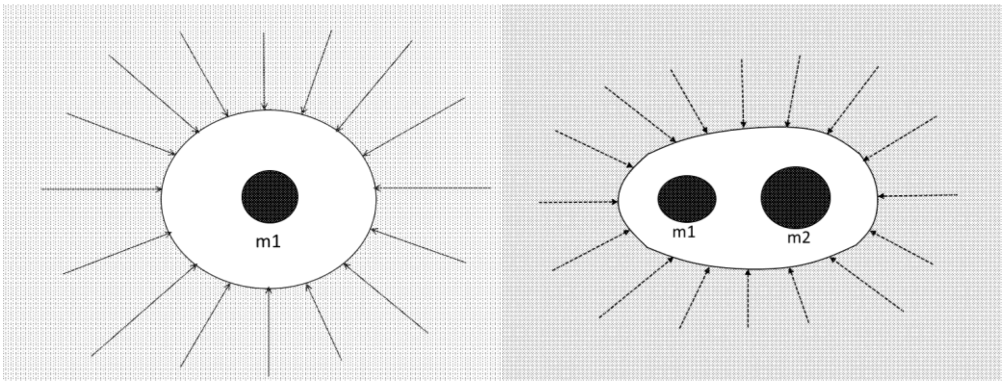


Figure 5: Presence of a given material object diminishes energy density of quantum vacuum and this generates inertial mass and gravitational mass.

The presence of two or several material objects, namely elementary particles, atoms, massive objects or stellar objects diminishes the energy density of quantum vacuum which generates gravitational mass and gravity. Gravity is pushing from the outer higher energy density of quantum vacuum around a given material object towards the lower energy density of quantum vacuum around a given material object.

The changes and fluctuations of the quantum vacuum energy density determine a curvature of space-time similar to the curvature produced by a "dark energy" density, through a quantized metric characterizing the underlying microscopic geometry of the 3D quantum vacuum [6]. The quantized metric of the 3D quantum vacuum condensate is

$$d\hat{s}^2 = \hat{g}_{\mu\nu} dx^\mu dx^\nu \quad (13)$$

whose coefficients (in polar coordinates) are defined by equations

$$\hat{g}_{00} = -1 + \hat{h}_{00},\ \hat{g}_{11} = 1 + \hat{h}_{11},\ \hat{g}_{22} = r^2\left(1 + \hat{h}_{22}\right),\ \hat{g}_{33} = r^2 \sin^2 \vartheta \left(1 + \hat{h}_{33}\right),\ \hat{g}_{\mu\nu} = \hat{h}_{\mu\nu} \text{ for } \mu \neq \nu \quad (14)$$

where multiplication of every term times the unit operator is implicit and, at the order $O\left(r^2\right)$, one has

$$\left\langle \hat{h}_{\mu\nu} \right\rangle = 0 \quad \text{except} \quad \left\langle \hat{h}_{00} \right\rangle = \frac{8\pi G}{3}\left(\frac{\Delta\rho_{qvE}}{c^2} + \frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE} \right)^6 \right) r^2 \quad \text{and}$$

$$\left\langle \hat{h}_{11} \right\rangle = \frac{8\pi G}{3}\left(-\frac{\Delta\rho_{qvE}}{2c^2} + \frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE} \right)^6 \right) r^2 \quad (15).$$

In equations (15) $\Delta\rho_{qvE}^{DE}$ are opportune fluctuations of the quantum vacuum energy density which determine the dark energy density on the basis of relation

$$\rho_{DE} \cong 70 \frac{G}{4\pi} \left(\frac{V}{c^2} \Delta\rho_{qvE}^{DE} \right)^2 \frac{1}{l} \cdot \frac{1}{l^3} \quad (16)$$

where

$$l = \frac{\hbar}{\left(\frac{V}{c^2} \Delta\rho_{qvE}^{DE} \right) c} \quad (17).$$

The quantized metric (13) is associated with an underlying microscopic geometry expressed by equations

$$\Delta x \geq \frac{\hbar}{2\Delta p} + \frac{\Delta p}{2\hbar} \left(2\pi^2 / 3 \right)^{2/3} l^{2/3} l_P^{4/3} \quad (18),$$

which is the uncertainty in the measure of the position,

$$\Delta t \geq \frac{\hbar}{2\Delta E} + \frac{\Delta E T_0^2}{2\hbar} \quad (19)$$

which is the time uncertainty and

$$\Delta L \cong \frac{\left(2\pi^2 / 3 \right)^{1/3} l^{1/3} l_p^{2/3} T_0 E}{2\hbar} \quad (20)$$

which indicates in what sense the curvature of a region of size *L* can be related to the presence of energy and momentum in it. Equations (18)-(20) are derived from the quantum uncertainty principle [13] and from the hypotheses of space-time discreteness at the Planck scale by following Ng's treatment [14-17] in which the structure of the space-time foam can be inferred from the accuracy in the measurement of a distance *l* – in a spherical geometry over the amount of time $T = 2l/c$ it takes light to cross the volume – given by

$$\delta l \geq \left(2\pi^2 / 3 \right)^{1/3} l^{1/3} l_P^{2/3} \quad (21)).$$

The quantized metric (13) allows the quantum Einstein equations

$$\hat{G}_{\mu\nu} = \frac{8\pi G}{c^4} \hat{T}_{\mu\nu} \quad (22)$$

(where the quantum Einstein tensor operator $\hat{G}_{\mu\nu}$ is expressed in terms in terms of the operators $\hat{h}_{\mu\nu}$) to be obtained directly: this means that the curvature of space-time characteristic of general relativity may be considered as a mathematical value which emerges from the quantized metric (13) and thus from the changes and fluctuations of the quantum vacuum energy density (on the basis of equations (14) and (15)) [6].

Moreover, by introducing the concept of energy density of quantum vacuum, the gravitational field existing in the points situated at distance *r* from the centre of a given material object of mass (8) assumes the form

$$\vec{g} = \frac{G\left(\frac{V}{c^2} \cdot \Delta\rho_{qvE} \right)}{r^2} \hat{r} \quad (23)$$

where $\hat{r}$ is the unitary vector indicating direction and orientation of $\vec{r}$. According to equation (23), the gravitational field is a property of space which is derived directly from the change of the energy density of quantum vacuum in the volume under consideration, and that gravity increases with the diminishing of the energy density of quantum vacuum. On the basis of the gravitational field (23) generated by a given change of the quantum vacuum energy density, the 3D quantum vacuum is characterized in each region by a dragging, pushing effect. In particular, as regards the motion of a planet in the solar system, the dragging effect of the 3D quantum vacuum is defined by a velocity given by relation:

$$v_{qv} = \frac{G\left(\frac{V}{c^2} \cdot \Delta\rho_{qvE}\right)}{r_p^{\ 2}} t \quad (24)$$

where r_p is the distance of the planet from the sun and *t* is time, namely the numerical order of the planet motion in the quantum vacuum [18].

3. Sagnac effect and dynamic quantum vacuum

Sagnac effect lies in the different velocities of different light signals relative to an interferometer. Light signals from a source S are split by the half-silvered-mirror HSM into two beams which follow clockwise or counter-clockwise paths, of equal length, back to HSM where they are recombined and detected at a final mirror D; when the interferometer is rotated with a given angular velocity, a phase shift develops between clockwise-and counter-clockwise-rotating beams due to different times-of-passage of the light signals, which is linked to the different velocities of clockwise- and counter-clockwise-rotating light beams relative to the interferometer (see figure 4). Sagnac published the results of his rotating interferometer experiment in 1913 [19]. When the whole apparatus, including the light source and the detector (which in Sagnac's original experiment was a photographic plate) is rotated a fringe shift ΔZ is observed, corresponding, at lowest order in the angular velocity, to a phase difference between the counter-rotating beams of: $\Delta\varphi = 2\pi\Delta Z = 8\pi\vec{\Omega}\cdot\vec{A}/(\lambda_0 c)$ (25)

where $\vec{\Omega}$ is the angular velocity vector, λ_0 is the vacuum wavelength of the light, $|\vec{A}|$ is the area enclosed by the circulating light beams and $\vec{A}$ is perpendicular to the plane of the interferometer. The fundamental space-time effect underlying the phase shift is a different transit time from beam-splitter to beam-splitter for clockwise- and counter clockwise-rotating beams, when the interferometer is rotating.

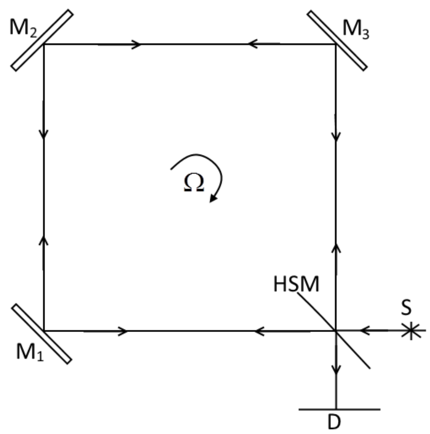


Figure 6: a Sagnac interferometer.

In the approach of the 3D quantum vacuum suggested here, we assume that the angular speed has two contributions, one linked to the orbital velocity of the earth v_p, the other linked to the velocity of the quantum vacuum in the region into consideration v_{qv}:

$$\Omega = \frac{v_p + v_{qv}}{L} \quad (26).$$

where 2L is the length of the path of the light signal between successive mirrors when the interferometer is at rest. In Galilean relativity, neglecting the displacement of the mirrors in the laboratory frame, the phase shift due to rotation of the interferometer, determined by the angular speed (26) is:

$$\Delta\phi_{GR} = \frac{8\pi\left(v_p + v_{qv}\right)A}{\lambda_0 Lc} + O\left(\beta\left(v_{qv}\right)^3\right) \quad (27)$$

where

$$\beta\left(v_{qv}\right) = \frac{v_p + v_{qv}}{c} \quad (28),$$

$$\gamma\left(v_{qv}\right) = \frac{1}{\sqrt{1 - \left(\frac{v_p + v_{qv}}{c}\right)^2}} \quad (29)$$

and $A = 4L^2$ is the area enclosed by the circulating light beams.

The Sagnac interference phase is a consequence of different times of arrival of the counter-rotating signals back at the HSM. The appropriate time interval is therefore that recorded by a clock co-moving with the HSM. In the laboratory frame the HSM has a velocity of constant magnitude $\sqrt{2}\left(v_p + v_{qv}\right)$, corresponding to the time dilation effect:

$$\Delta T = \frac{1}{\sqrt{1 - 2\left(\frac{v_p + v_{qv}}{c}\right)^2}} \Delta T' \quad (30)$$

which leads to

$$\Delta\phi_{SR} = \frac{8\pi\left(v_p + v_{qv}\right)A}{\lambda_0 Lc}\left[1 - \frac{13\beta\left(v_{qv}\right)^2}{24}\right] + O\left(\beta\left(v_{qv}\right)^5\right) \quad (31).$$

On the basis of equation (31), special relativity therefore contributes only an order $\beta\left(v_{qv}\right)^2$ correction to the Sagnac phase difference as calculated in Galilean relativity. These results obtained in the context of the 3D quantum vacuum model are in agreement with the treatment previously made by Post [20].

It is interesting also to consider a Sagnac circular interferometer of radius R rotating with uniform angular velocity in the clockwise direction. The angular velocity is determined by the motion of quantum vacuum on the basis of relation

$$\Omega = \frac{v_p + v_{qv}}{R} \quad (32).$$

Co-rotating (LS+) and counter-rotating (LS−) light signals depart simultaneously from a beam splitter (BS) when it is positioned at BS0 (see figure 5). The signals LS− (LS+) arrive back at BS when it is in the laboratory frame positions BS− (BS+). In the laboratory frame both light signals move with speed *c*. The different arrival times result from different laboratory frame path lengths followed by the signals.

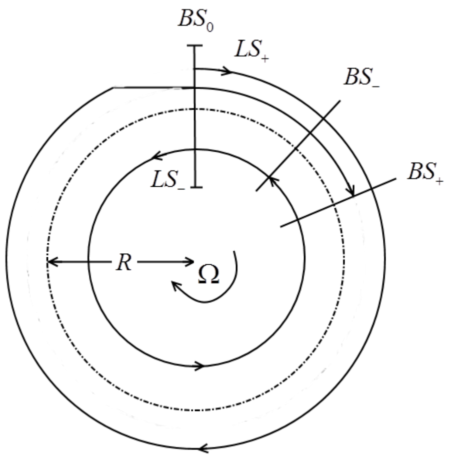


Figure 7: A circular Sagnac interferometer of radius *R* rotating with uniform angular velocity Ω in the clockwise direction.

In this case, the relative velocities of the light signals and the interferometer, determined by the dragging effect of the quantum vacuum, are given by:

$$c_r^{\pm} = c \mp \left(v_p + v_{qv}\right) \quad (33),$$

where c_r^+ (c_r^-) are the velocities of clockwise (counter clockwise) rotating light signals, relative to an adjacent point on the interferometer, in the laboratory system. The times-of-passage of the light signals from beam-splitter to beam-splitter in the laboratory system for the counter-rotating signals are:

$$T_{\pm} = \frac{2\pi R}{c \mp \left(v_p + v_q\right)} \quad (34).$$

In Galilean relativity $T_{\pm} = T_{\pm}'$ where $T_{\pm}'$ are the times of passage in the co-rotating frame of the interferometer, so the corresponding Sagnac phase shift is:

$$\Delta\phi_{GR} = \frac{8\pi\left(v_p + v_{qv}\right)A}{\lambda_0 Rc}\left[1 + \beta\left(v_{qv}\right)^2\right] + O\left(\beta\left(v_{qv}\right)^5\right) \quad (35)$$

where $A = \pi R^2$.

In a special relativistic picture, by using the differential Lorentz transformations from the laboratory system into the instantaneous co-moving frame of the beam splitter BS, one obtains the time dilation effect

$$T_{\pm}' = \frac{T_{\pm}}{\gamma\left(v_{qv}\right)} \quad (36)$$

so that the phase shift becomes

$$\Delta\phi_{SR} = \frac{8\pi\left(v_p + v_{qv}\right)A}{\lambda_0 Rc}\left[1 + \beta\left(v_{qv}\right)^2 / 2\right] + O\left(\beta\left(v_{qv}\right)^5\right) \quad (37)$$

In the light of the time dilation relations (36), the relative velocities of the light signals and the interferometer are not the same in the laboratory and co-rotating systems in the special relativistic case:

$$T_{\pm}' = \frac{2\pi R}{\gamma\left(v_{qv}\right)c_r^{\pm}} \quad (38).$$

Relations (38), which indicate that the times of signal flight in the co-rotating frame are determined by the motion of the quantum vacuum, are in agreement with calculations previously performed by Tartaglia [21]. Moreover, equations (38) show that the relative velocities of the light signals and the interferometer transform between the laboratory and co-rotating frames as

$$\left(c_r^{\pm}\right)=\gamma\left(v_{qv}\right)\left[c\mp\left(v_p+v_{qv}\right)\right] \quad (39)$$

which is compatible with previous results by Klauber [22]. From equations (39) follows also

$$\frac{\left(c_r^{+}\right)}{\left(c_r^{-}\right)}=\frac{c-\left(v_p+v_{qv}\right)}{c+\left(v_p+v_{qv}\right)} \quad (40)$$

which is in agreement with Selleri's inertial transformations

$$\begin{cases} x'=\dfrac{x_0-vt_0}{\sqrt{1-\beta^2}} \\ y'=y_0 \\ z'=z_0 \\ t'=\sqrt{1-\beta^2}\,t_0 \end{cases} \quad (41)$$

which determines an arena of Special Relativity in which the temporal coordinate must be clearly considered as a different entity with respect to the spatial coordinates just because the transformation of clocks' run between the two inertial systems does not depend on the spatial coordinates.

On the light of the treatment of Sagnac effect based on equations (26)-(40), one can say that the different velocities of clockwise- and counter-clockwise-rotating light beams relative to the Sagnac interferometer is really due to the motion of the quantum vacuum. Quantum vacuum around the earth is turning with it and – as equations (27), (30), (31), (34)-(39) explicitly demonstrate – this causes that the light signal between two clocks moves with higher velocity in the direction of earth rotation and with lower velocity in the opposite direction of earth rotation. A turning quantum vacuum in which photon moves influences its velocity (see figure 8).

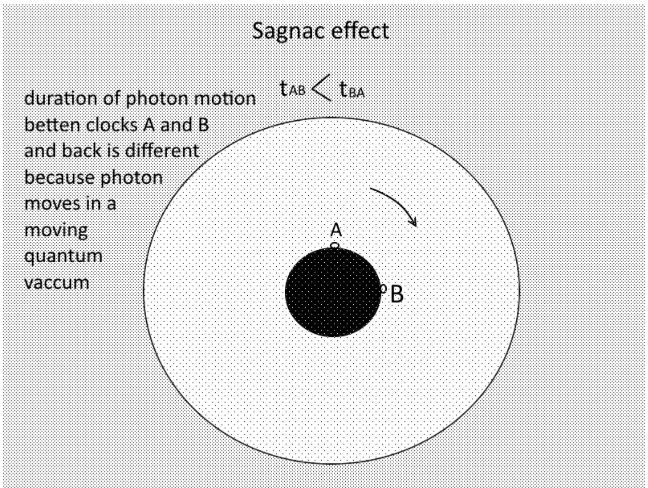


Figure 8: Sagnac effect by measuring light signal velocity.

As described in the papers [23, 24] Sagnac effect is routine in the operations involved in the Global Positioning System (GPS) providing accurate worldwide clock synchronization and timing system. As is well known, in a rotating reference frame, the Sagnac effect prevents a network of self-consistently synchronized clocks from being established by transmission of electromagnetic signals that propagate with the universally constant speed *c* (this is called Einstein synchronization), or by slow transport of portable atomic clocks [25]. This is a significant issue in using timing signals to determine position in the GPS. The Sagnac effect can amount to hundreds of nanoseconds; a timing error of one nanosecond can lead to a navigational error of 30 cm. The velocity of GPS microwave signals in the rest frame of a GPS receiver can be calculated according to the formula (27) above. In the GPS navigation the Sagnac correction term, which arises when one accounts for motion of the receiver while the signal propagates from transmitter to receiver may be expressed as

$$\Delta t_{Sagnac} = \frac{2(\vec{v}_p + \vec{v}_q)}{Rc^2} \cdot \left(\frac{1}{2} \vec{r}_R \times \vec{R} \right) \quad (42)$$

where $\vec{r}_R$ is the receiver position (namely the vector from earth's centre to the receiver position) of a signal transmitted from the satellite position $\vec{r}_T$ at GPS time t_T, $\vec{R} = \vec{r}_R - \vec{r}_T$.

The quantity $\frac{2(v_p + v_q)}{Rc^2}$ has the value

$$\frac{2(v_p + v_q)}{Rc^2} = 1{,}6227 \cdot 10^{-21} s/m^2 \quad (43).$$

In agreement with equations (27), (31), (35), (37), the last factor in equation (42) can be interpreted as a vector area $\vec{A}$:

$$\vec{A} = \left(\frac{1}{2} \vec{r}_R \times \vec{R} \right) \quad (44).$$

The only component of $\vec{A}$ which contributes to the Sagnac correction is along earth's angular velocity vector

$$\vec{\Omega} = \frac{\vec{v}_p + \vec{v}_{qv}}{R} \quad (45)$$

due to the motion of the quantum vacuum and the orbital velocity of the earth, because of the dot product that appears in the expression. This component is the projection of the area onto a plane normal to earth's angular velocity vector associated with the dragging of the quantum vacuum. This leads to a simple description of the Sagnac correction (which turns out to be in agreement, for example, with Ashby's treatment [23]): Δt_{Sagnac} is $\frac{2(\vec{v}_p + \vec{v}_q)}{Rc^2}$ time the area swept out by the electromagnetic pulse – determined by the motion of the quantum vacuum – as it travels from the GPS transmitter to the receiver, projected onto earth's equatorial plane.

Similar corrections are also applied in tests, using the GPS, of the isotropy of the speed of light [26]. In this case, as also in the Michelson-Gale experiment, the 'laboratory frame', in which the speed of light is assumed [23, 24] or measured [26] to be *c*, is the Earth-Centered-Inertial (ECI) frame which is the co-moving inertial frame of the centroid of the Earth with axes pointing to fixed directions on the celestial sphere. It is in this frame that the Earth's gravitational field is given by the Schwarzschild metric [27, 28] and which effectively contains the 'aether', relative to which, 'winds' were observed by Sagnac, and Michelson and Gale. It is indeed a prediction of general relativity that, in just this frame, the speed of light is (very nearly) equal to *c*. 'Very nearly' because of the Shapiro delay [29] of light signals crossing the Earth's gravitational field. For signals from the GPS satellites such delays are less than 200ps [23] and so give no perceptible effect in GPS operation.

For hypothetical in vacuum light signals circumnavigating the Earth at the Equator at constant distance *R* from the centre of the Earth the velocity of light is given by the Schwarzschild metric equation:

$$0=\left(1-\frac{2G\left(\frac{V}{c^2}\cdot\Delta\rho_{qvE}\right)}{Rc^2}\right)dt^2-\frac{R^2d\phi^2}{c^2} \quad (46).$$

Then the speed of the light signals in the ECI frame is

$$c_E=\left(1-\frac{G\left(\frac{V}{c^2}\cdot\Delta\rho_{qvE}\right)}{Rc^2}\right)c+O\left[\left(-\frac{G\left(\frac{V}{c^2}\cdot\Delta\rho_{qvE}\right)}{Rc^2}\right)^2\right] \quad (47)$$

which yields

$$\frac{c-c_E}{c}=6{,}94\cdot 10^{-10} \quad (48).$$

The ‘Shapiro delay’ for such a light signal is then about 90ps for a round trip time of $\frac{2\pi R}{c_E}=134ms$.

In order to provide an explanation of the experimental data on the propagation of microwaves near to the surface of the Earth [23, 24, 30] and the Shapiro radar echo delay experiments for microwave signals passing close to the Sun [29], in two 2001 papers Su proposed the existence of different ‘effective aethers’ around the Earth and the Sun in the context of a classical electromagnetic wave theory distinct from that given by special relativity [31, 32]. Here, we have shown, however, that the existence of such ‘effective aethers’ is a necessary consequence of general relativity in the picture of a 3D quantum vacuum which determines dragging effects as a consequence of the changes of its energy density, so that no new classical theory of the type proposed by Su is required.

4. Precessions of planets originates in the turning quantum vacuum

Quantum vacuum as the fundamental arena of the universe is in dynamic relation with particles and massive bodies which exist in it. The quantum vacuum around a stellar object which turns around its axis is moving with it. Diminished region of quantum vacuum around a given material object or stellar body is like his “extended body” and is in a dynamic relation with outer region of quantum vacuum with higher density.

The idea about dynamic energy density of universal space which depends on the presence of stellar objects is not new. Already Newton was thinking in a similar way: "Doth not this ethereal medium in passing out of water, glass, crystal, and other compact and dense bodies in empty spaces, grow denser and denser by degrees, and by that means refract the rays of light not in a point, but by bending them gradually in curve lines? ...Is not this medium much rarer within the dense bodies of the Sun, stars, planets and comets, than in the empty celestial space between them? And in passing from them to great distances, does it not grow denser and denser perpetually, and thereby cause the gravity of those great bodies towards one another, and of their parts towards the bodies; every body endeavoring to go from the denser parts of the medium towards the rarer?" [33].

The region of quantum vacuum around the Sun is turning together with the Sun’s turning and is causing precession of planets which is diminishing with the distance from the Sun and is biggest for Mercury. The difference between the velocity of the quantum vacuum and orbital velocity of the planets acts in such a way that it produces the precession of the perihelion of the planets' orbits. It is the motion of the planets owing to the velocity of the quantum vacuum that is the fundamental element that determines the famous test effect of the General Theory of Relativity. In the light of equation (24), we can say that quantum vacuum has a special property, namely a “motion effect” which is linked to the change of its energy density: when the energy density of quantum vacuum decreases, its motion effect on a stellar object is stronger and thus produces a stronger precession of this stellar object (see figure 9). The precession of each planet is caused by a specific value of the motion effect of the quantum vacuum.

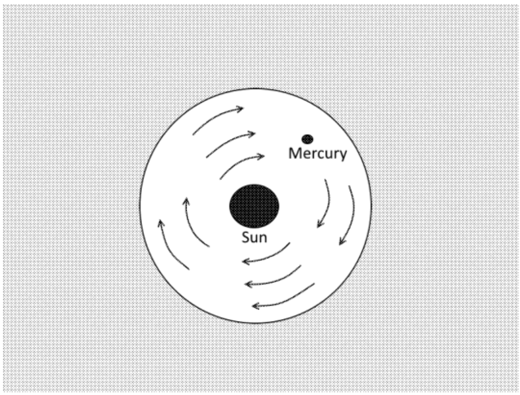


Figure 9: Dragging effect of quantum vacuum causes Mercury's perihelion precession.

In general theory of relativity the anomalous precessions of the planets can be derived by considering the following equation

$$\frac{d^2r}{d\tau^2} = -\frac{r_S}{r^2} + \frac{h^2}{r^3} - \frac{3h^2 r_S}{r^4} \quad (49)$$

where τ is the proper time, r_S is the gravitational radius of the Sun, h is a quantity (having the dimension of an angular momentum) determined by the initial conditions of the planet's orbit and is given by $h = \omega r^2$ where ω is the proper angular speed of the planet. Our Sun's mass is not nearly concentrated enough to permit this kind of orbit, since the Sun's gravitational radius r_S is only 1.475 kilometres, whereas its matter fills a sphere of radius 696,000 kilometres [34].

In the approach of the 3D quantum vacuum suggested here, we assume that the angular speed of each planet has two contributions, one linked to the orbital velocity of the planet v_p, the other linked to the velocity of the quantum vacuum on the planet's orbit v_{qv}:

$$\omega = \frac{v_p + v_{qv}}{r} \quad (50).$$

By substituting (50) into (49) we obtain:

$$\frac{d^2r}{d\tau^2} = -\frac{r_S}{r^2} + \frac{(v_p + v_{qv})^2}{r^2}(r - 3r_S) \quad (51).$$

By resolving equation (51) one arrives at the solution

$$r(\phi) = \left(\frac{h^2 / r_S}{1 + 3(r_S / h)^2}\right)\frac{1}{1 + k\cos(\Omega\phi)} \quad (52)$$

where k is a constant of integration and

$$\Omega = \frac{1}{\sqrt{1+6\left(\frac{r_S}{(v_p+v_{qv})r}\right)^2}} \quad (53).$$

By expanding Ω one can obtain the precession per revolution as

$$\frac{2\pi}{\Omega} - 2\pi = 6\pi\left(\frac{r_S}{(v_p+v_{qv})r}\right)^2 \quad (54)$$

and thus the amount of precession for revolution depends on the velocity of the quantum vacuum that drags the planet under consideration. Moreover, by multiplying the amount of precession for revolution, given by equation (54), for the number of revolutions per century one can obtain the amount of precession for century (that can so be seen itself as a consequence of the velocity of the quantum vacuum).

In our approach, we can say that the precession of each planet is caused by a specific velocity of the quantum vacuum, which derives from its energy density. The velocity of the quantum vacuum at the planet's orbit is determined by the diminishing of the energy density in that region on the basis of equation (24). Moreover, for each planet p we can define a factor of "motion effect of quantum vacuum" e_{mqv} at the planet's orbit by means of the following relation

$$e_{mqv} = \frac{|v_{qv} - v_p|}{r_p^2} \quad (55)$$

where v_{qv} is the velocity of quantum vacuum on the planet's orbit and v_p is the velocity of the planet. Taking into account equation (55), the motion effect of the quantum vacuum increases with time and decreases with the increasing of the distance from the Sun. So, for planets closer to the Sun, the velocity of the quantum vacuum at a planet's orbit turns out to be higher and therefore the motion effect of the quantum vacuum is higher and the amount of precession is higher. Instead, for planets further from the Sun, the velocity of the quantum vacuum at a planet's orbit turns out to be lower and therefore the motion effect of the quantum vacuum is lower and the amount of precession is lower.

On the basis of the elements of planetary orbits we can construct the following table showing the values of relativistic precession, the specific velocity of the quantum vacuum for each planet (in one second), and the motion effect of the quantum vacuum acting on each planet (in one second).

Planet	Velocity v_{qv} of quantum vacuum in one second (Km/s)	Mean orbital velocity v_p of the planet (Km/s)	Mean distance from the Sun ($10^6 Km$)	Mass ($10^{24} Kg$)	Motion effect e_{mqv} of the quantum vacuum in one second ($10^{-16} Km^{-1}s^{-1}$)	Calculation of precession per century ($arcs$)
Mercury	39.3943	47.88	57.9	0.33	25.3122	42.9195
Venus	11.2807	35.02	108.2	4.87	20.2774	8.6186
Earth	5.9010	29.79	149.6	5.98	10.6742	3.8345
Mars	2.5427	24.13	227.9	0.65	4.1563	1.3502

Jupiter	0.2180	13.97	778.3	1900	0.2270	0.0623
Saturn	0.0648	9.67	1427	570	0.0472	0.0137
Uranus	0.0160	6.81	2869.6	87	0.0083	0.0024
Neptune	0.0065	5.45	4496.6	100	0.0027	0.0008
Pluto	0.0038	4.74	5900	0.7	0.0014	0.0004

It is interesting to remark that the calculations on the basis of the model here suggested lead, as regards the amounts of precession per century, to the same results as obtained by Einstein's general theory of relativity. What emerges here is the possibility of introducing a new physical entity as the ultimate source of the precessions of planets, namely the velocity of quantum vacuum (which is related to the change of the energy density of quantum vacuum) and thus to provide a new suggestive key of reading the results of general relativity.

5. About Shapiro experiment, geodetic effect, dragging effect and energy density of dynamic quantum vacuum

Besides perihelion-shift, another classic "test" of general relativity is represented by the time delay of light signals in a gravitational field. In this regard, in 1964 Irwin Shapiro realized that if general relativity was correct, a light signal sent across the solar system past the sun to a planet or satellite would be slowed in the sun's gravitational field by an amount proportional to the light-bending factor, $\frac{1+\gamma}{2}$ (where γ is the Eddington parameter measuring the distortion of space to first order, which, according to various observations, is predicted to satisfy $|\gamma-1|<2{,}3\cdot10^{-5}$) and that it would be possible to measure this effect if the signal were reflected back to earth. Typical time delays are on the order of several hundred microseconds; this is sometimes referred to as the "fourth classical test" of general relativity. Passive radar reflections from Mercury and Mars were consistent with general relativity to an accuracy of about 5%. Use of the Viking Mars lander as an active radar retransmitter in 1976 confirmed Einstein's theory at the 0.1% level. Other targets included artificial satellites such as Mariners 6 and 7 and Voyager 2, but the most precise of all Shapiro time delay experiments involved Doppler tracking of the Cassini spacecraft on its way to Saturn in 2003; this limited any deviations from general relativity to less than 0.002% — the most stringent test of the theory so far.

In our model velocity of light by Shapiro effect is diminished for a minimal amount because of diminished energy density of quantum vacuum near stellar objects. Diminished energy density of DQV ρ_{qv} close to the stellar object with mass diminishes permeability μ_0 and permittivity ε_0 of "free space" and this determines a diminishing of the velocity of light: $\rho_P \to c=\frac{1}{\varepsilon_0\cdot\mu_0}$, $\rho_{qv}\to c=\frac{1}{\sqrt{\varepsilon\cdot\mu}}$. It is valid in general that velocity of changes (rate of clocks and velocity of light included) diminishes with the diminishing of energy density of quantum vacuum.

Furthermore, radio astronomy provided another famous test of general relativity in the form of the binary pulsar. General relativity predicts that a non-spherically-symmetric system (such as a pair of masses in orbit around each other) will lose energy through the emission of gravitational waves. While these waves themselves have not yet been detected directly, the loss of energy has. The evidence comes from binary systems containing at least one pulsar. Pulsars are rapidly rotating neutron stars that emit regular radio pulses from their magnetic poles. These pulses can be used to reconstruct the pulsar's orbital motions. The fact that these objects are neutron stars makes them particularly valuable as experimental probes because their gravitational fields are much stronger than those of the sun (thus providing arguably "moderate-field" tests of general relativity, in the regime of weak fields in the sense that $Gm/c^2r \approx 1$, namely $GV \cdot \Delta\rho_{qvE}/c^4r \approx 1$). The first binary pulsar was discovered by R. A. Hulse and J. H. Taylor in 1974. Timing measurements produce three constraints on the two unknown masses plus one more quantity; when applied to the general-relativistic energy loss formula, the results are consistent at the 0.2% level. Several other relativistic binary systems have since been discovered, including one whose orbital plane is seen almost edge-on and another in which the companion is probably a white dwarf rather than a neutron star. Most compelling is a *double pulsar* system, in which radio pulses are detected from both stars. This imposes six constraints on the two unknown masses and allows for four independent tests of general relativity. The fact that all four are mutually consistent is itself impressive confirmation of the theory. After two and a half years of observation, the most precise of these tests (time delay) verifies Einstein's theory to within 0.05%.

On the other hand, in 1960, Schiff showed that an ideal gyroscope in orbit around Earth would undergo two relativistic precessions with respect to a distant inertial frame: (1) a geodetic drift in the orbit plane due to motion through the space-time curved by Earth's mass and (2) a frame-dragging due to Earth's rotation [35]. This means, in other words, that general relativity predicts two fundamental phenomena: the geodetic effect, according to which the spin axis of a rotating test body precess in a gravitational field (namely a curved spacetime around a massive object causes an orbiting gyroscope to precess about an axis perpendicular to the plane of its motion), and the frame-dragging effect, according to which a rotating object pulls spacetime around with it, twisting the spin axis of a gyroscope along the equatorial plane. In the framework of a gravito-electromagnetic analogy, the geodetic effect can be seen partly as a spin-orbit interaction between the spin of the gyroscope and the "mass current" of the rotating object; the frame-dragging effect is a manifestation of the *spin–spin* interaction between the test body and the central mass. Gravity Probe B, launched 20 April 2004, can be considered as the first space experiment of general relativity to produce direct and unambiguous detections of the geodetic effect and the frame-dragging effect. Data collection started 28 August 2004 and ended 14 August 2005. Analysis of the data from all four gyroscopes of this space experiment results in a geodetic drift rate of $-6601{,}8 \pm 18{,}3 mas/yr$ and a frame-dragging drift rate of $-37{,}2 \pm 7{,}2 mas/yr$, to be compared with the general relativistic predictions of $-6606{,}1 mas/yr$ and $-39{,}2 mas/yr$, respectively (where $1 mas = 4{,}848 \cdot 10^{-9} rad$). Results of the Gravity Probe B experiment are thus in agreement with the predictions of general relativity (GR) for both the geodetic precession and the frame-dragging precession.

The precession due to the geodetic effect and the frame-dragging effect is given by Schiff's formula

$$\vec{\Omega}_{GR} = \vec{\Omega}_g + \vec{\Omega}_{fd} = \frac{3GM}{2c^2r^3}\left(\vec{r} \times \vec{v}\right) + \frac{GI}{c^2r^3}\left[\frac{3\vec{r}}{r^2}\left(\vec{S} \cdot \vec{r}\right) - \vec{S}\right] \quad (56)$$

where M, I and $\vec{S}$ are mass, moment of inertia and angular momentum of the central body while $\vec{r}$ and $\vec{v}$ are the radial position and instantaneous velocity of the test body. The frame-dragging or S-dependent term in equation (56), which reveals clearly the Machian aspect of Einstein's theory, is smaller in magnitude than the geodetic one. For whatever reason, frame-dragging within general relativity was first discussed that same year by Austrian physicists Hans Thirring and Josef Lense; it is often referred to as the Lense-Thirring effect. Thirring originally approached this problem as an experimentalist; he hoped to look for Mach-type dragging effects inside a massive rotating cylinder. Unable to raise the necessary financing, he reluctantly settled down to solve the problem theoretically instead [36]. It is his second calculation (with Lense) involving the field outside a slowly rotating solid sphere that forms the basis for modern gyroscopic tests. But both his results are "Machian" in the sense that the inertial reference frame of the test particle is influenced by the motion of the larger mass (the cylinder or sphere). This is completely unlike Newtonian dynamics, where local inertia arises entirely due to motion with respect to "absolute space" and is not influenced by the distribution of matter.

In terms of the gravito-electromagnetic analogy, frame-dragging is a manifestation of the *spin–spin* interaction between the test body and central mass. In the case of Gravity Probe B, a test body with spin *S* experiences a torque proportional to $\vec{S}\times\vec{H}$, where $\vec{H}$ is the gravitomagnetic field obeying equation

$$\vec{\nabla}\times\vec{H} = -\frac{4\pi G}{c^2}2\vec{j} + \frac{1}{c^2}\frac{\partial\vec{g}}{\partial t} \quad (57),$$

($\vec{g}$ representing the gravitostatic field, namely the "ordinary" Newtonian field and $\vec{j}$ being the ordinary mass current density), which causes the gyroscope spin axes to precess in the east-west direction by 39 milliarcseconds per year – an angle so tiny that it is equivalent to the average angular width of the dwarf planet *Pluto* as seen from earth.

The orbital plane of an artificial satellite is also a kind of "gyroscope" whose nodes (the points where it intersects a reference plane) will exhibit a similar frame-dragging precession (the de Sitter effect). Such an effect has been reported in the case of the earth-orbiting Laser Geodynamic Satellites (LAGEOS and LAGEOS II) by Ignazio Ciufolini and colleagues using laser ranging [37, 38]. Both in the Lageos and in the Gravity Probe B experiments the relevant parameter which determines the angular velocities of the gyroscopes is

$$\frac{GM_E}{c^2R} \approx 10^{-9} \quad (58).$$

In [39] Adler has shown that the predictions of the gyro precession in the Gravity Probe B experiment can be reproduced in a coherent picture in terms of the following three fundamental elements of gravity theory: firstly, that macroscopic gravity is described by a metric theory such as general relativity, secondly that the Lense-Thirring metric provides an approximate description of the gravitational field of the spinning earth, and thirdly that the spin axis of a gyroscope is parallel displaced in spacetime, which gives its equation of motion. On the basis of Adler's treatment, the agreement of Gravity Probe B with theory strengthens the belief that all three elements of gravity theory listed above are correct and constitutes an important proof of the shows the success of general relativity in the description of astrophysical phenomena.

By following Adler [39], in the Lens-Thirring metric

$$ds^2 = (1-2m/r)dt^2 - (1+2m/r)dr^2 + 2\left(\frac{2GJ}{r}\right)\sin^2\theta d\varphi dt \quad (59),$$

(*J* being the angular momentum of the spinning source body), which in the gravito-magnetic approximation may be conveniently expressed as

$$ds^2 = (1-2\phi)dt^2 - (1+2\phi)dr^2 + 2(\vec{H}\cdot d\vec{r})dt \quad (60)$$

ϕ being the Newtonian potential outside the body, the spin equation for Gravity Probe B is

$$\dot{\vec{S}} = \left(\vec{\Omega}_G + \vec{\Omega}_{LT}\right)\times\vec{S} \quad (61)$$

where $\vec{\Omega}_G$ is the geodetic vector field

$\vec{\Omega}_G = (\gamma + \alpha/2)(\nabla\phi \times \vec{v})$ (62),

$\vec{\Omega}_{LT}$ is the gravito-magnetic vector potential

$\vec{\Omega}_{LT} = \frac{1}{4}(\gamma + \alpha)(\nabla \times \vec{H})$ (63),

α being the Eddington parameter measuring the distortion of time due to gravity.

For the Gravity Proce B gyro the precession is extremely slow, so the spin does not change appreciably over the course of many orbits, and we may write the change in $\vec{S}$ in time Δt as

$\Delta\vec{S} = (\vec{\Omega}_G \times \vec{S})\Delta t + (\vec{\Omega}_{LT} \times \vec{S})\Delta t$ (64)

with $\vec{S}$ treated as a constant. As regards the geodetic term of (64) which is by far the larger part, since for a circular orbit the gravitational force and the velocity are perpendicular and thus the geodetic field is perpendicular to the orbit plane, the geodetic vector and its magnitude are

$\vec{\Omega}_G = (\gamma + \alpha/2)\left(\frac{GM}{r^2}\right)(\hat{r} \times \vec{v})$ (65),

$\Omega_G = (\gamma + \alpha/2)\left(\frac{GMv}{r^2}\right)$ (66).

The Lens-Thirring precession depends on the gravito-magnetic field $\vec{\Omega}_{LT}$, which varies with position in the orbit. The gravito-magnetic vector potential $\vec{H}$ of the spinning earth can be calculated in the same way as the vector potential of a spinning ball of charge in electrodynamics. The results are the following

$\vec{H} = \left(\frac{2G}{r^3}\right)(\vec{r} \times \vec{J})$ (67),

$\vec{\Omega}_{LT} = \frac{1}{2}(\gamma + \alpha)G\left(\frac{\vec{J}}{r^3} - \frac{3\vec{r}}{r^5}(\vec{r} \cdot \vec{J})\right)$ (68)

where $\vec{J}$ is the angular momentum of the earth. In this way, according to Adler's results, the Lens-Thirring precession may be obtained directly by only averaging $\vec{\Omega}_{LT}$ over an orbit.

According to our model of 3D DQV, the mass of the central body is determined by a corresponding diminishing of the quantum vacuum energy density, which thus acts on the test body motions; as a consequence, Schiff's formula (56) may be conveniently expressed as

$\vec{\Omega}_{GR} = \vec{\Omega}_g + \vec{\Omega}_{fd} = \frac{3GV \cdot \Delta\rho_{qvE}}{2c^4 r^3}\left(\vec{r} \times (\vec{v}_p + \vec{v}_{qv})\right) + \frac{GI(\Delta\rho_{qvE})}{c^2 r^3}\left[\frac{3\vec{r}}{r^2}(\vec{S} \cdot \vec{r}) - \vec{S}\right]$ (69).

On the basis of equation (69), the geodetic effect of general relativity is directly determined by the motion effect of the quantum vacuum energy density and, because of the indirect dependence of the moment of inertia of the central body of the changes of the quantum vacuum energy density, also the frame-dragging effect implicitly depends of the quantum vacuum energy density. Moreover, taking account of Adler's results, the geodetic vector field (62) may be written as

$\vec{\Omega}_G = (\gamma + \alpha/2)\left(\nabla\phi \times (\vec{v}_p + \vec{v}_{qv})\right)$ (70)

which, in the case of a circular orbit, becomes

$$\vec{\Omega}_G = (\gamma + \alpha/2)\left(\frac{GV \cdot \Delta\rho_{qvE}}{c^2 r^2}\right)\left(\hat{r} \times \left(\vec{v}_p + \vec{v}_{qv}\right)\right) \quad (71)$$

whose magnitude is

$$\Omega_G = (\gamma + \alpha/2)\left(\frac{GV \cdot \Delta\rho_{qvE}\left(v_p + v_{qv}\right)}{c^2 r^2}\right) \quad (72).$$

Finally, also the gravito-magnetic vector potential (68), because of its dependence of the angular momentum of the earth, is linked with the motion effect of the quantum vacuum and the changes of the quantum vacuum energy density. In synthesis, according to our model of 3D DQV, Adler's relations regarding the geodetic effect and the Lens-Thirring precession, namely equations (62)-(68), may be seen as a consequence of more fundamental changes of the quantum vacuum energy density.

6. Energy density of quantum vacuum and relative velocity of clocks

Energy density of dynamic quantum vacuum is at the minimum in the centre of stellar object and increases by distance from the centre according to the formalism (10). Diminished energy density of quantum vacuum causes clocks run slower on the earth surface than on GPS satellites. It is valid in general that velocity of changes (rate of clocks and velocity of light included) diminishes with the diminishing of energy density of quantum vacuum.

Because of the well-known General Relativity effect, rate of clocks is slower on the surface of the earth than on the GPS satellites for 45,7 μs per day. Because of Special Relativity effect rate of clocks is slower on the GPS satellite than on the surface of the earth for 7,1 μs per day [40].

By considering the Schwarzschild metric

$$c^2 d\tau^2 = \left(1 - \frac{r_S}{r}\right)c^2 dt^2 - \left(1 - \frac{r_S}{r}\right)^{-1} dr^2 + r^2 d\vartheta^2 - r^2 \sin^2 \vartheta d\varphi^2 \quad (73)$$

where $r_S = \frac{2GV\Delta\rho_{qvE}}{c^4}$ is the Schwarzschild radius (corresponding to the change of the quantum vacuum energy density $\Delta\rho_{qvE} = \rho_{pE} - \rho_{qvE}$ the gravitational time dilation of general relativity, in the vicinity of a non-rotating massive spherically symmetric object, may be expressed as:

$$\tau_0 = \tau_f \left(1 - \frac{r_S}{r}\right)^{1/2} \quad (74)$$

where τ_0 is the proper time between events A and B for a slow-ticking observer within the gravitational field, τ_f is the coordinate time between two given events A and B for a fast-ticking observer at an arbitrarily large distance from the massive object (this assumes the fast-ticking observer is using Schwarzschild coordinates, a coordinate system where a clock at infinite distance from the massive sphere would tick at one second per second of coordinate time, while closer clocks would tick at less than that rate), *G* is the gravitational constant, *r* is the radial coordinate of the observer (which is analogous to the classical distance from the center of the object, but is actually a Schwarzschild coordinate).

In particular, if we consider the propagation of pulsed signals in a Schwarzschild space-time, which are emitted at events 1 and 2 on radius r_E and received at events 3 and 4 on radius r_R, with $r_R > r_E$, one obtains

$$d\tau_R / d\tau_E = \left(1 - \frac{r_S}{r_R}\right)^{1/2} / \left(1 - \frac{r_S}{r_E}\right)^{1/2} \quad (75)$$

where $d\tau_R / d\tau_E > 1$. Equation (75) indicates that the proper time interval between signal pulses at the receiver is longer than the interval at the emitter; equivalently, the signal frequency at the receiver is lower than at the emitter (this is the well known gravitational red shift, which can be attributed to the different gravitational potentials at the transmitter and receiver and thus to the different behaviours of the quantum vacuum energy density at the transmitter and receiver and is expressed in a proper time ratio).

A moving satellite is diminishing energy density of quantum vacuum ρ_{qvE} in the centre of the satellite according to the following formalism:

$$\rho_{qvE} = \rho_{pE} - \frac{mc^2 + \frac{1}{2}mv^2}{V} \quad (73),$$

where m and *V* are the mass and the volume of the satellite and v is its velocity regarding the earth surface.

We can thus conclude that between an event pair at the receiver the associated clock records a longer velocity of change than the corresponding velocity of change recorded at the emitter. Put another way: according to a given time standard, there is more velocity of change between an event pair at the receiver than there is between the corresponding events at the emitter. In both special relativity and general relativity, we employ time intervals on standard clocks running at the standard rate. On what might be called the usual view in special relativity, clocks are said to be slowed on account of their motion, but no satisfactory explanation, or calculation, has ever been given. In general relativity, a clock in a stronger gravitational field is said to run more slowly – again, a notion exists that the clock is in some way affected.

By considering what we mean by the rate of a clock and the amount of time between given event pairs in the picture of our 3D DQV model, our conclusion is that clocks (and consequently also rods) are not affected in Relativity Theory. Clocks do not go slow and rods do not contract. In Dynamic Quantum Vacuum Relativity (DQVR) changes run in quantum vacuum only and not in time. “Relative” is velocity of change which depends on the energy density of quantum vacuum. Changes (and clocks) do not run in time; duration of changes is time. In DQVR time is a fundamental quantity of the universe which has only a mathematical existence. Dynamic Quantum Vacuum itself is “timeless” in a sense time is not its 4^{th} dimension [41].

7. About the variability of gravitational constant

Variable energy density of DQV has also an influence on the value of gravitational constant G_N. According to our model gravitational constant G_N has not the same value in the entire universe. In the outer space where energy density of DQV is at the maximum gravitational constant G_N is at the minimum and increases minimally into direction of stellar objects where energy density of DQV is diminishing. In interstellar space, far away from material objects, energy density of DQV is the Planck energy density (2), and this implies that in interstellar space the value of gravitational constant G_N is given by relation:

$$G_N = \frac{l_P^3}{m_P \cdot t_P^2} = \frac{1}{\rho_{pE} t_P^2} \qquad (76),$$

where ρ_{pE} is Planck energy density and t_P is Planck time.

The energy density of DQV at a given point T on the surface of a satellite which is at a distance d from the centre of the stellar object density of DQV is given by equation (10) and, as a consequence, at this point gravitational constant G_N is given by the following relation:

$$G_N = \frac{1}{\rho_{qvE} t_P^2} \qquad (77).$$

Using formalism (77) we can calculate value of gravitational constant G_N on the Earth surface, in the earth centre and for example on the satellite which is 20000 km above the surface:

$$G_{earth.surface} = 6{,}746469 \cdot 10^{-11} m^3 Kg^{-1} s^{-2}$$

$$G_{earth.centre} = 6{,}7464714 \cdot 10^{-11} m^3 Kg^{-1} s^{-2}$$

$$G_{satellite} = 6{,}745427 \cdot 10^{-11} m^3 Kg^{-1} s^{-2}.$$

Calculated difference between value of gravitational constant G_N in the centre of the earth and on its surface is:

$$\Delta G_{earth.centre-earth.surface} = 6{,}7464714 \cdot 10^{-11} - 6{,}746469 \cdot 10^{-11} = 0{,}0000024 \cdot 10^{-11} m^3 kg^{-1} s^{-2}.$$

Calculated difference between value of gravitational constant G_N on the surface of the earth and satellite 20000 km above the surface is:

$$\Delta G_{earth.surface-satellite} = 6{,}746469 \cdot 10^{-11} - 6{,}745427 \cdot 10^{-11} = 0{,}001042 \cdot 10^{-11} m^3 kg^{-1} s^{-2}.$$

We see that value of *G* is bigger at the centre of the earth and decreases with the distance from the centre. The difference between gravitational constant G_N on the surface and in the centre is minimal respectively to the difference of G_N between earth surface and on the satellite. This indicates that measured differences of G_N in different places on the earth surface can be ascribed to some "external causes", but not to "internal causes" inside the earth as for example its geological structure. Gravitational constant G_N has been measured by several groups in different places on the globe and the values are variable from 0,1% to 0,7% [42]. Our explanation of the measured variability of gravitational constant G_N is that motion of earth, moon and other planets is affecting density of DQV of a given place on the earth surface where G_N is measured.

In order to confirm influence of moon and planet's motion, G_N should be measured at the same time in different places on the planet earth which are close to the same meridian and have similar geographic length. We chose following places: St. Petersburg in Russia, Minsk in Belorussia, Kiev in Ukraine, Chisinau in Moldova, Istanbul in Turkey, Cairo in Egypt and Johannesburg in South Africa. In all cities one should obtain the same values of G_N because the distance and so influence of the moon and planets on density of quantum vacuum in these cities is almost the same. We plan proposed experiment will be carried out in 2016.

On the other hand, in virtue of the fluctuations of the quantum vacuum energy density, the interesting perspective emerges that, as a consequence of the evolution of the quantum vacuum energy density, a cosmic evolution of all the masses in the universe occurs, both of the nuclei and of the Dark Matter particles, which can be perfectly compatible with general relativity. By using the Friedmann-Lemaitre-Robertson-Walker (FLRW) metric one finds that the most general local conservation law preserving the Bianchi identity (that is satisfied by the Einstein tensor of the gravitational field equations $\nabla^{\mu} G_{\mu\nu} = 0$), corresponding to an isotropic and homogeneous dust matter fluid emerging from a change of quantum vacuum energy density $\Delta\rho_{qvE}$, reads

$$\frac{G'_N}{G_N}\left(\frac{\Delta\rho_{qvE}}{c^2}+\frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE}\right)^6\right)+\left(\frac{\Delta\rho_{qvE}}{c^2}\right)^I\left(\frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE}\right)^6\right)^I+\frac{3}{a}\frac{\Delta\rho_{qvE}}{c^2}=0 \quad (78)$$

where a is the scale factor and the primes denote derivatives of the various quantities with respect to it. Equation (78) means physically that Newton's gravitational constant G_N is strictly related to fundamental variations of the quantum vacuum energy density.

From equation (78) one can understand how in the theory here proposed a general evolution of Newton's coupling G_N in combination with the particle masses can emerge. In this regard, many studies motivated the possibility of having variable fundamental constants of Nature and of a time variation of the particle masses, such as, for example, the one regarding the proton mass [43-45]. For example, in Fritzsch's and Solà's chiral gauge theory of quantum haplodynamics, where the weak bosons, quarks, and leptons are bound states of fundamental constituents, called haplons, and their antiparticles, the predicted time evolution of the particle masses can be parameterized as

$$\rho_m \approx a^{-3(1-\nu)} \quad (79)$$

[46], where the presence of $|\nu| << 1$ denotes a very small departure from the standard conservation law $\approx a^{-3}$. Such a departure is not viewed as a loss or an excess in the number of particles in a commoving volume (beyond the normal dilution law), but rather as a change in the value of their masses. Models with anomalous matter conservation laws of the above type have been carefully confronted with the precise cosmological data on distant supernovae, baryonic acoustic oscillations, structure formation, and one finds the upper bound $|\nu| \le O(10^{-3})$ [47-49].

In our approach, equation (77) may be written as

$$\Delta\rho_{qvE} \approx c^2 a^{-3(1-\nu)} \quad (80)$$

which means that the predicted time evolution of the particle masses corresponds to a more fundamental time evolution of the quantum vacuum energy density. The conservation law (80) together with equation (78) implies that a dynamical response will be generated from the parameters of the gravitational sector, G_N and $\Delta\rho_{qvE}^{DE}$. In other words, on the basis of equations (80) and (78), one can say that the time evolution of all the masses in the universe as well as of the gravitational constant is related to opportune changes of the quantum vacuum energy density. Conversely, dark energy may be seen as an effect of opportune changes of the quantum vacuum energy density triggered by the time evolution of all the masses in the universe.

The time variation of the proton mass (and in general of all masses) within Fritzsch's and Solà's aforementioned parameterization is expressed as follows:

$$\left|\frac{\dot{m}_p}{m_p}\right| \cong 3|v|H \quad (81)$$

and the corresponding change of the vacuum energy density reads

$$\left|\frac{\dot{\rho}_{vac}}{\rho_{vac}}\right| \cong -3|v|\frac{\Omega_m^0}{\Omega_{vac}^0}H \quad (82)$$

where Ω_m^0, Ω_{vac}^0 are the current cosmological parameters associated with matter and vacuum energy. In our model, taking account of equations (15)-(16), equation (82) becomes:

$$\left|\frac{\left(\frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE}\right)^6\right)^I}{\frac{35Gc^2}{2\pi\hbar^4 V}\left(\frac{V}{c^2}\Delta\rho_{qvE}^{DE}\right)^6}\right| \cong -3|v|\frac{\Omega_m^0}{\Omega_{vac}^0}H \quad (83)$$

which indicates that the cosmic evolution of the masses emerges as an effect of a more fundamental evolution of the quantum vacuum energy density. Moreover, as a consequence of the cosmic evolution of the quantum vacuum energy density, one has an analogous evolution of the gravitational constant:

$$\left|\frac{\dot{G}}{G}\right| \le |v|H \quad (84).$$

Using the current value of the Hubble parameter as a reference, $H_0 = 1.0227k \cdot 10^{-10} yr^{-1}$, where $k \cong 0.70$ and the mentioned limit $|v| \le O\left(10^{-3}\right)$, we find that the time variations of the above parameters are at most of the order $\le 10^{-13} yr^{-1}$.

Finally, we should also mention that the approach here developed, which implies that the variable vacuum energy and the gravitational constant can be linked to the variation of the particle masses, are compatible with the primordial nucleosynthesis bounds on the chemical species. The important constraint to be preserved here is that the vacuum energy density remains sufficiently small as compared to the radiation density at the time of nucleosynthesis. At the same time, potential variations of the gravitational constant should also be moderate enough to avoid a significant change in the expansion rate at that time.

8. Dynamic quantum vacuum model and cosmology

In DQV which is the fundamental arena of the universe time is merely a mathematical parameter of change, i.e. motion in DQV. Past, present and future are not physical realities which can be associated to a 4th dimension of space, they are only emergent realities which have a mathematical existence [50]. Universe exists in what Albert Einstein used to call NOW: "…there is something essential about the NOW which is just outside the realm of science. People like us, who believe in physics, know that the distinction between the past, present and future is only a stubbornly persistent illusion" [51].

Our model of DQV has brought Einstein's NOW inside the realm of physics. DQV is always NOW in which past, present, future have only a mathematical existence. Common understanding of the Big bang cosmology where universe is expanding in time as a physical reality is not appropriate any more (see figure 10).

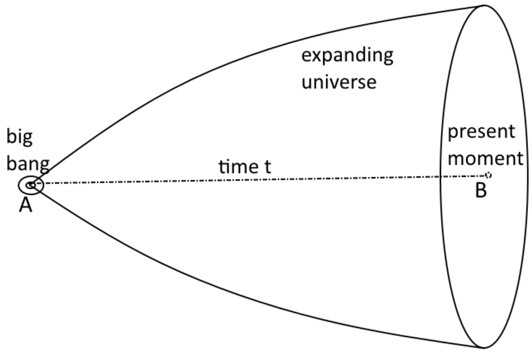


Figure 10: Classical image of Big bang cosmology.

Universe exists in DQV which is NOW. Universe is timeless in a sense that time is not a physical dimension in which universe exists. This view is also confirmed by the research of Kurt Gödel. By 1949, Gödel had produced a remarkable proof: "In any universe described by the Theory of Relativity, time cannot exist" [41]. Gödel discovered that closed "time-lines" in General Relativity allow hypothetical travels in time which leads to contradictions. Considering time has only mathematical existence there are no contradictions, one can travel in dynamic quantum vacuum only and time is duration of its motion.

Model of the universe where time is only a mathematical parameter of change, i.e. motion requires the re-reading of some experimental data. Considering that universe exists in physical time the interpretation that cosmic microwave background radiation (CMB) has a source 380000 years after big bang makes sense because time *t* is a physical dimension which relates big bang (on the Figure 10 point A) with present moment (on the Figure 10 point B) in which we measure CMB, in other words time is a transmitor of CMB. Considering that universe exists in DQV which is NOW, CMB cannot have its source in some hypothetical physical past and time cannot be transmitor of CMB. The source of CMB is present in the actual universe that we observe.

Considering that universe is NOW also existence of one single big bang and eternal expansion of the universe is questionable. The only reasonable cosmological model based on big bang seems a cyclic universe where big bang is followed by expansion which stops at a certain period and universe starts collapsing in a big crunch which explodes in a new big bang. We propose a model of universe in a dynamic equilibrium with no beginning and no end with a permanent energy flow which has origin in variable density of DQV (see Figure 4).

In our model of DQV which is NOW, also BICEP2 model of gravitational waves as ripples of space-time which have origin in big bang becomes questionable [52]. The idea of BICEP2 is that gravitational waves are born at Big bang (on the Figure 10, at the point A) and are expanding in physical time to the present moment (on the figure 10, at the point B). Considering time is not a physical dimension in which universe expands, time cannot transmit gravitational waves or any other signal which can be transmitted only via DQV where time is a duration of its motion from point A to point B. If gravitational waves exist, they should have origin in DQV which is NOW, namely in a source which is present in the universe we observe. On the other hand, the "B-mode" polarizations of the cosmic microwave radiation observed by the BICEP telescope at the South Pole seem most likely to be “local” galactic contamination rather than an imprint left behind by the rapid “inflation” of the early universe [53].

In our model gravity is a result of fundamental symmetry between a given particle or material object and diminished energy density of DQV. In order to describe gravity our model does not require existence of hypothetical graviton nor existence of gravitational waves. According to Newton’s model gravity is not a propagating phenomenon with duration as light is; gravity is immediate. That’s why in Newton’s formalism for gravity time does not appear. Also in General Relativity time is only a mathematical parameter of stress-energy tensor; gravity has origin in curvature of space and is immediate. Our model does not predict existence of hypothetical graviton nor existence of gravitational waves. Gravity is not a propagating phenomenon with duration as light is, gravity is immediate. In this picture, comparing hypothetical graviton with photon does not seem appropriate also because it considers gravity requires motion and so time.

9. Perspectives and conclusions

In this article mass is presented as a result of a dynamics between a given particle or massive body and the quantum vacuum in which particle or massive body exists. The concept of mass presented in this paper answers the question what gives mass to the Higgs boson itself [54]. In our model gravity is a result of the pressure of outer quantum vacuum with higher energy density in the direction of quantum vacuum with lower energy density due to existence of a given particle or massive object. This model is valid from the scale of elementary particles to the scale of stellar objects.

NASA research shows that universal space is flat with only a 0.4% margin of error: “Recent measurements (c. 2001) by a number of ground-based and balloon-based experiments, including MAT/TOCO, Boomerang, Maxima, and DASI, showed that the brightest spots are about 1 degree across. Thus the universe was known to be flat to within about 15% accuracy prior to the WMAP results. WMAP has confirmed this result with very high accuracy and precision. We now know (as of 2013) that the universe is flat with only a 0.4% margin of error. This suggests that the Universe is infinite in extent; however, since the Universe has a finite age, we can only observe a finite volume of the Universe. All we can truly conclude is that the Universe is much larger than the volume we can directly observe” [55].

NASA results strongly indicate that curvature of space in General Theory of Relativity is only a mathematical description of energy density of universal space which originates in energy density of quantum vacuum. The development of a mathematical model which will connect energy density of quantum vacuum, curvature of space in General Theory of Relativity and Higgs field is currently in progress and, in this connection, the geometro–hydrodynamic model of space-time as condensate could give an important contribution in the understanding of quantum vacuum since, if the Universe as a whole should be a quantum object (whose large scale behavior is controlled by a classic–like equation such the Gross–Pitaevsky equation in Bose-Einstein Condensate theory [56]), the existence of vacuum energy density characterizing it as a quantum system could be immediately explained, unlike what happens in the generally accepted point of view in which it remains substantially mysterious. Obviously further researches and developments are necessary and in progress in this direction, above all as regards the formulation of a complete dynamical model of quantum vacuum energy density.

The general concept of the Standard Model is to describe the four fundamental forces with elementary particles and to explain the mass of the elementary particles with the Higgs boson. As this model does not give completely satisfying results yet, on the basis of the treatment of this paper, according to the authors it seems plausible and legitimate to suggest that mass and gravity originate from the diminishing of the energy density of a quantum vacuum condensate characterized by a quantized metric, caused by a given material object or particle. Physical phenomena of inertial mass, gravitational mass and gravity have origin in the dynamics between the underlying arena of the universe represented by the 3D dynamic quantum vacuum and existing particle or massive object. This model can be applied from the scale of the photon to the scale of a centre of the galaxy and has the merit to describe the mass of every elementary particle including the Higgs boson too. Furthermore it is compatible with the dynamic space mathematically described by general relativity in the low energy–long wavelength limit of the behaviour of timeless dynamic quantum vacuum.

References:

1. Timashev, S. F.: “Physical vacuum as a system manifesting itself on various scales – from nuclear physics to cosmology”, arXiv:1107.pdf [gr-qc] (2011).
2. Rovelli, C.: “Loop quantum gravity”, *Physics World* **7**, 11, 1-5 (2003).
3. Rovelli, C.: “Loop quantum gravity”, <http://relativity.livingreviews.org/Articles/lrr-2008-5/> (2008).
4. Rovelli, C.: “A new look at loop quantum gravity”, <arXiv:1004.1780v1 [gr-qc]> (2010).
5. Fiscaletti, D. and Sorli, A.: “Perspectives about quantum mechanics in a model of a three-dimensional quantum vacuum where time is a mathematical dimension”, *SOP Transactions on Theoretical Physics* **1**, 3, 11-38 (2014).
6. Fiscaletti D. and Sorli, A.: “Space-time curvature of general relativity and energy density of a three-dimensional quantum vacuum”, *Annales UMCS Sectio AAA: Physics* **69**, 55-81 (2010).
7. Mosanori, S.: "A revisit of the papers on the theory of relativity: Reconsideration of the hypothesis of ether-dragging", http://arxiv.org/abs/0704.1942 (2009).
8. Sorli, A., Fiscaletti, D. and Gregl, T.: “New insights into Gödel’s universe without time”, *Physics Essays* **26**, 1, 113-115 (2013).
9. Santos, E.: “Space-time curvature induced by quantum vacuum fluctuations as an alternative to dark energy”, *International Journal of Theoretical Physics* **50**, 7, 2125-2133, DOI 10.1007/s10773-010-0633-6 (2010).
10. Zeldovich, Yu B.: “Cosmological constant and elementary particles”, *Zh. Eksp. & Teor. Fiz. Pis’ma* **6**, 883-884 (1967).
11. Rueda, A. and Haisch, B.: “Gravity and the quantum vacuum inertia hypothesis”, arXiv:gr-qc0504061v3 (2005).
12. Friedlander, M. W.: *A Thin Cosmic Rain: Particles from Outer Space*, Harvard University Press, Harvard (2002).
13. Ghao, S.: “Why gravity is fundamental,” arXiv:1001-3029v3 (2010).

14. Ng, Y. Jack: “Holographic Foam, Dark Energy and Infinite Statistics”, *Physics Letters B* **657**, 1, 10-14 (2007).

15. Ng, Y. Jack: “Spacetime foam: from entropy and holography to infinite statistics and non-locality”, *Entropy* **10**, 441-461 (2008).

16. Ng, Y. Jack: “Holographic quantum foam”, arXiv:1001.0411v1 [gr-qc] (2010).

17. Ng, Y. Jack: “Various facets of spacetime foam”, arXiv:1102.4109.v1 [gr-qc] (2011).

18. Sorli, A. and Fiscaletti, D.: “Special theory of relativity in a three dimensional Euclid space”, *Physics Essays* **25**, 1, 141-143 (2012).
19. Sagnac, G.: “L'ether lumineux demonstre par l’effet du vent relatif d’ether dans un interferometre en rotation uniforme”, *Comptes Rendus* **157**, 708-710; “Sur la preuve de la réalité de l'éther lumineux par l'expérience de l'interférographe tournant”, *Comptes Rendus* **157**, 1410-1413 (1913).
20. Post, E. J.: “Sagnac effect”, *Reviews of Modern Physics* **39**, 2, 475-493 (1967).
21. Tartaglia, A. in: ‘Relativity in Rotating Frames’, G. Rizzi and M.L. Ruggiero (Eds.), Kluwer Academuc Publishers, Dordrecht (2004).
22. Klauber, R.D.: “Derivation of the general case Sagnac result using non-time-orthogonal analysis”, *Found. Phys. Lett.* **16**, 5, 447-463 (2003).
23. Ashby, N.: “Relativity and the global positioning system”, *Physics Today* **55**, 5, 41-47 (2002).
24. Allan, D. W., Weiss, M. A. and Ashby, N.: *Science* **228**, 64-70 (1985).
25. Landau, L. and Lifshitz, E.: *The Classical Theory of Fields*, 4th ed., Pergamon, New York (1997).
26. Wolf, P. and Petit, G.: “Satellite Test of Special Relativity Using the Global Positioning System”, *Physical Review A* **56**, 4405-4409 (1997).
27. Schwartzschild, K.: Sitzungberichte Prüssiche Akademie der Wissenschaften, p. 198 (1916).
28. Weinberg, S.: *Gravitation and Cosmology, Principles and Applications of the General Theory of Relativity*, John Wiley, New York (1972).
29. Shapiro, I. et al.: “Fourth test of general relativity: New radar results”, *Physical Review Letters* **26**, 18, 1132-1135 (1971).
30. Saburi, Y., Yamamoto, M. and Harada, K.: “High-precision Time Comparison via Satellite and Observed Discrepancy of Synchronization”, *IEEE Trans. Instr. Meas.* **25**, 4, 473-477 (1976).
31. Su, C.-C.: Reinterpretation of the Michelson-Morley experiment based on the GPS Sagnac correction, *Europhysics Letters* **56**, 2, 170-174 (2001).
32. Su, C.-C.: “A local-ether model of propagation of electromagnetic wave”, *European Journal of Physics C* **21**, 4, 701-715 (2001).
33. Newton, I.: *The Third Book of Optics*, http://www.newtonproject.sussex.ac.uk (1718).
34. Brown, K.: *Reflections on relativity*, Amazon (2011), pp. 421-431.
35. Schiff, L. I.: “Possible new experimental test of general relativity theory,” *Physical Review* **4**, 5, 215-217 (1960).
36. Pfister, H.: “Dragging effects near rotating bodies and in cosmological models,” in Barbour, J. B. and Pfister, H. (eds.), *From Newton’s bucket to quantum gravity*, Birkhäuser, Boston (1995), p. 315.
37. Ciufolini, I. et al.: “Test of general relativity and measurement of the Lense-Thirring effect with two earth satellites,” *Science* **279**, 5359, 2100-2103 (1998).

38. Ciufolini, I. and Pavlis, E.C.: “A confirmation of the general relativistic prediction of the Lense-Thirring effect,” *Nature* **431**, 7011, 958-960 (2004).
39. Adler, R. J.: “The three-fold theoretical basis of the Gravity Probe B gyro precession calculation”, arXiv:1405.5511v1 [gr-qc] (2014).
40. Mosanori, S.: "Interpretation of the slight periodic displacement in the Michelson-Morley experiments", http://arxiv.org/abs/physics/0605067 (2006).
41. Fiscaletti, D. and Sorli, A.: “Bijective epistemology and space-time”, *Foundations of Science*, in course of publication (2014).
42. Gundlach, J. H. Adelberger, E. G., Heckel, B. R. and Swanson, H. E.: *Physical Review D* **54**, 1256R (1996).
43. E. Reinhold, R. Buning, U. Hollenstein, A. Ivanchik, P. Petitjean, and W. Ubachs, “Indication of a cosmological variation of the proton-electron mass ratio based on laboratory measurement and reanalysis of H_2 spectra”, *Physical Review Letters* **96**, 15, Article ID 151101 (2006).
44. W. Ubachs and E. Reinhold, “Highly accurate H_2 Lyman and Werner Band Laboratory measurements and an improved constraint on a cosmological variation of the proton-to-electron mass ratio”, *Physical Review Letters* **92**, 101302 (2004).
45. A. Ivanchik, P. Petitjean, D. Varshalovich et al., “A new constraint on the time dependence of the proton-to-electron mass ratio: analysis of the Q 0347-383 and Q 0405-443 spectra”, *Astronomy and Astrophysics* **440**, 1, 45–52 (2005).
46. H. Fritzsch and J. Solà, “Quantum haplodynamics, dark matter, and dark energy”, *Advances in High Energy Physics* Volume 2014, Article ID 361587, 6 pages (2014).
47. S. Basilakos, M. Plionis, and J. Solà, “Hubble expansion and structure formation in time varying vacuum models”, *Physical Review D* **80**, 8, Article ID083511 (2009).
48. J. Grande, J. Solà, S. Basilakos, and M. Plionis, “Hubble expansion and structure formation in the “running FLRW model” of the cosmic evolution”, *Journal of Cosmology and Astroparticle Physics* **1108**, 007 (2011).
49. S. Basilakos, D. Polarski, and J. Solà, “Generalizing the running vacuum energy model and comparing with the entropic-force models”, *Physical Review D* **86**, Article ID 043010 (2012).
50. Fiscaletti, D. and Sorli, A.: “Perspectives of the Numerical Order of Material Changes in Timeless Approaches in Physics”, *Foundations of Physics* **44**, 10 (2014).
51. Sorli, A.: *The Physics of NOW*, Amazon (2014).
52. BICEP 2 http://bicepkeck.org/.
53. http://physicsworld.com/cws/article/news/2014/sep/22/bicep2-gravitational-wave-result-bites-the-dust-thanks-to-new-planck-data (2014).
54. Wilczek, F.: “Origins of Mass”, http://arxiv.org/pdf/1206.7114.pdf (2012).
55. NASA, http://map.gsfc.nasa.gov/universe/uni_shape.html (2013).
56. Pethick, C. and Smith, H.: *Bose – Einstein condensation in diluited gas*, Cambridge University Press, Cambridge (2002).