

A formula that seems to generate easily big numbers that are primes or products of very few primes

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Abstract. The formula $N = (p^4 - 2p^2 + m)/(m - 1)$, where p is an odd prime and m is a positive integer greater than 1, seems to generate easily primes or products of very few primes.

Observation:

The formula $N = (p^4 - 2p^2 + m)/(m - 1)$, where p is an odd prime and m is a positive integer greater than 1, seems to generate easily primes or products of very few primes.

Examples:

For $m = 2$ the formula becomes $N = p^4 - 2p^2 + 2$ and were obtained the following results for the sequence of the first five consecutive primes of the form $10k + 1$:

- : for $p = 11$, $N = 14401$ prime;
- : for $p = 31$, $N = 921601$ prime;
- : for $p = 41$, $N = 2822401 = 113 \cdot 24977$;
- : for $p = 61$, $N = 13838401 = 3313 \cdot 4177$;
- : for $p = 71$, $N = 25401601 = 101 \cdot 251501$.

For a larger prime of the same form, $p = 961752931$, is obtained $N = 855855567096510789934200845104477377601$, a semiprime with 39 digits.

For $m = 3$ the formula becomes $N = (p^4 - 2p^2 + 3)/2$ and were obtained the following results for the sequence of the first five consecutive primes of the form $20k + 9$:

- : for $p = 29$, $N = 352801 = 17 \cdot 20753$;
- : for $p = 89$, $N = 31363201$ prime;
- : for $p = 109$, $N = 70567201 = 2659 \cdot 26539$;
- : for $p = 149$, $N = 246420001$ prime;
- : for $p = 229$, $N = 1374976801 = 11 \cdot 124997891$.

For $m = 4$ the formula becomes $N = (p^4 - 2p^2 + 4)/3$ and were obtained the following results for the sequence of the first eight consecutive primes of the form $30k + 13$:

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: for p = 13, N = 9409 = 97^2;
: for p = 43, N = 1138369 prime;
: for p = 73, N = 9462529 = 1609*5881;
: for p = 103, N = 37509889 = 43*872323;
: for p = 163, N = 235286209 prime;
: for p = 193, N = 462471169 prime;
: for p = 223, N = 824291329 prime;
: for p = 283, N = 2138029249 prime.

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For two larger primes of the same form is obtained:

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: for p = 1299763, N = 951339271160353903881409 prime;
: for p = 1299853, N = 951602794365121103901889 prime.

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Taking randomly a prime, id est $p = 29$, are obtained the following results:

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: for m = 2, N = 705601, a semiprime;
: for m = 3, N = 352801, a semiprime;
: for m = 4, N = 235201, a semiprime;
: for m = 5, N = 176401, a prime;
: for m = 6, N = 141121, a prime;
: for m = 7, N = 117601, a semiprime;
: for m = 8, N = 100801, a prime;
: for m = 9, N = 88201, a semiprime;
: for m = 10, N = 78401, a prime;
: for m = 11, N = 70561, a semiprime;
: for m = 12, N is not integer;
: for m = 13, N = 58801, a semiprime;
: for m = 14, N is not integer;
: for m = 15, N = 50401, a semiprime;
: for m = 16, N = 47041, a prime;
: for m = 17, N = 44101, a prime (...)

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