

Pi-Theory of the fundamental physical constants Copyright © V.B. Smolenskiy 2014  
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 of the principal ideas.

## Pi-Theory of the fundamental physical constants: metrological aspects

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The article presents the results of exact analytical calculations of values of fundamental physical constants – given the finite formulas and calculations. Presents comparison of some of the data CODATA 2010 with theoretical calculations.

### 1. Introduction

The author of this article proceed from the famous assumptions John A. Wheeler, that the direction of development of physics can be no physics → pregeometry and pregeometry → physics.

Conceptually, Pi-Theory of the fundamental physical constants (hereinafter Pi-Theory) is constructed in the area of development pregeometry → physics.

PI-Theory is based on the following assumptions:

1. Physical reality – is a single parametric space-time material environment (hereinafter the Environment).
2. Wednesday dwells only in the boundaries of extreme values of its parameters.
3. Each of the parameters of Environment has a finite range of your changes.
4. The maximum rate of change of parameters of the Environment has a limit.

The aim of this article is to present for physical community of concrete results PI-Theory in the field of fundamental Metrology - in determining the values of the fundamental physical constants (FPC). Issues related with section PI-Theory “Pregeometry” and subsection “Cosmology” section “Physics”, the article will not considered.

### 2. The final formulas and the calculated results

Clarification: if the designation of the parameter has a lower index of “ $\pi$ ”, that is, first of all, means that it is parameter PI-Theory, and secondly, that this parameter has a theoretical value that can be used instead the true value of the parameter.

**Table 1.** Presents the calculation formulas for determining the values of the dimensionless FPC.

N	Name of parameter	Symbol	Calculation formula
1	scalar parameter of structure of space - time	$f_{\pi s}$	$f_{\pi s} = \sqrt[3]{\frac{f_{\pi se}^4}{f_{\pi s0}}}$
2	scalar parameter of structure of space - time	$\tilde{f}_{\pi s}$	$\tilde{f}_{\pi s} = \sqrt[4]{f_{\pi s0} \cdot f_{\pi se}^3}$
3	coefficient of asymmetry	$k_{\pi}$	$k_{\pi} = \sqrt[4]{\frac{\tilde{f}_{\pi s}}{f_{\pi s}}}$
4	coefficient of absolute stability	$k_{\pi st}$	$k_{\pi st} = k_{\pi}^9$
5	scalar parameter of elementary charge*	$\alpha_{\pi}$	$\alpha_{\pi} = \alpha_{\pi e} / k_{\pi}$
6	constant of scale invariance	$\psi_{\pi}$	$\psi_{\pi} = \frac{8\pi^6}{\sqrt{\pi}} \cdot f_{\pi s}^3 \cdot \alpha_{\pi}^6$
7	the constant of parametric communication	$\beta_{\pi}$	$\beta_{\pi} = f_{\pi s} / \alpha_{\pi}$

N	Name of parameter	Symbol	Calculation formula
8	scalar parameter of the strong charge	$\alpha_{\pi s}$	$(\sqrt{2\pi})^3 \cdot \pi^2 \cdot \alpha_{\pi x} \cdot \beta_\pi = (1 + \Delta y_\pi \cdot \alpha_{\pi x})^3$
9	the coefficient of electroweak asymmetry	$k_{\pi w}$	$k_{\pi w} = k_\pi \cdot \frac{\alpha_{\pi e} \cdot \beta_{\pi e}}{f_{\pi s}} \cdot \frac{(1 + \Delta y_\pi \cdot \alpha_\pi)^3}{(1 + \Delta y_{\pi e} \cdot \alpha_\pi)^3}$
10	scalar parameter the weak charge	$\alpha_{\pi w}$	$\alpha_{\pi w} = k_{\pi w}^3 - 1$
11	electromagnetic constant asymmetry	$\Delta_{\pi a}$	$\Delta_{\pi a} = \alpha_{\pi e} - a_{\pi ex}$
12	electron magnetic moment anomaly	$a_{\pi e}$	$a_{\pi e} = \alpha_{\pi e} \left( 1 - \frac{1}{k_\pi} \right) + a_{\pi ex}$
13	electron-proton mass ratio	$r_{\pi ep}$	$r_{\pi ep} = \frac{f_{\pi s} \cdot (1 + \Delta y_\pi \cdot \alpha_\pi)^3}{\sqrt[3]{\pi^2}} \cdot \left( 1 - \frac{\alpha_\pi}{\alpha_{\pi s}} \right) \cdot k_{\pi st}$
14	electron-neutron mass ratio	$r_{\pi en}$	$r_{\pi en} = \frac{f_{\pi s} \cdot (1 + \Delta y_\pi \cdot \alpha_\pi)^3}{\sqrt[3]{\pi^2}} \cdot \frac{a_{\pi e} + \alpha_{\pi w}}{a_{\pi e} + \Delta_{\pi a}}$
15	neutron-proton mass ratio	$r_{\pi np}$	$r_{\pi np} = \left( 1 - \frac{\alpha_\pi}{\alpha_{\pi s}} \right) \cdot \frac{a_{\pi e} + \Delta_{\pi a}}{a_{\pi e} + \alpha_{\pi w}} \cdot k_{\pi st}$
16	proton-neutron magnetic moment ratio	$r_{\pi \mu, pn}$	$r_{\pi \mu, pn} = -\frac{(\pi - 1)^2}{\pi} \cdot \frac{(1 + \alpha_{\pi w})^2}{(1 + \Delta_{\pi a})^2}$
17	scalar parameter of substance quantity**	$p_{\pi s}$	

\* – at the same time, the parameter is the root of the cubic equation (line 8).

\*\* – the cosmological parameter. The formula is not given.

**Table 2.** Presents the results of theoretical calculations dimensionless FPC of Table 1.

N	Name of parameter	Symbol	The numerical value
1	scalar parameter of structure of space - time	$f_{\pi s}$	$1.161\ 712\ 977\ 019\ 596\ 928\ 970\ 254\ 552\ 9785 \times 10^{-3}$
2	scalar parameter of structure of space - time	$\tilde{f}_{\pi s}$	$1.161\ 713\ 355\ 141\ 817\ 542\ 167\ 276\ 310\ 5792 \times 10^{-3}$
3	coefficient of asymmetry	$k_\pi$	$1.000\ 000\ 081\ 371\ 686\ 023\ 215\ 889\ 742\ 4093$
4	coefficient of absolute stability	$k_{\pi st}$	$1.000\ 000\ 732\ 345\ 412\ 577\ 634\ 571\ 480\ 5245$
5	scalar parameter of elementary charge	$\alpha_\pi$	$1.161\ 409\ 733\ 400\ 893\ 939\ 488\ 207\ 987\ 9548 \times 10^{-3}$
6	constant of scale invariance	$\psi_\pi$	$1.669\ 642\ 831\ 928\ 813\ 892\ 580\ 472\ 149\ 4893 \times 10^{-23}$
7	the constant of parametric communication	$\beta_\pi$	$1.000\ 261\ 099\ 601\ 615\ 200\ 373\ 179\ 794\ 6565$
8	scalar parameter of the strong charge	$\alpha_{\pi s}$	$15.711\ 152\ 080\ 759\ 781\ 419\ 544\ 767\ 260\ 121$
9	the coefficient of electroweak asymmetry	$k_{\pi w}$	$1.000\ 000\ 081\ 819\ 691\ 595\ 185\ 909\ 818\ 4577$
10	scalar parameter the weak charge	$\alpha_{\pi w}$	$2.454\ 590\ 948\ 689\ 440\ 753\ 881\ 892 \times 10^{-7}$
11	electromagnetic constant asymmetry	$\Delta_{\pi a}$	$1.757\ 552\ 613\ 321\ 940\ 865\ 158\ 064 \times 10^{-6}$
12	electron magnetic moment anomaly	$a_{\pi e}$	$1.159\ 652\ 180\ 787\ 571\ 998\ 623\ 049\ 923\ 493 \times 10^{-3}$
13	electron-proton mass ratio	$r_{\pi ep}$	$5.446\ 170\ 218\ 699\ 090\ 667\ 403\ 109\ 649\ 777 \times 10^{-4}$
14	electron-neutron mass ratio	$r_{\pi en}$	$5.438\ 673\ 446\ 906\ 118\ 561\ 918\ 007\ 850\ 167 \times 10^{-4}$
15	neutron-proton mass ratio	$r_{\pi np}$	$1.001\ 378\ 419\ 180\ 000\ 000\ 000\ 000\ 000\ 000$
16	proton-neutron magnetic moment ratio	$r_{\pi \mu, pn}$	$-1.459\ 898\ 124\ 622\ 977\ 783\ 495\ 815\ 120$
17	scalar parameter of substance quantity	$p_{\pi s}$	$0.999\ 778\ 555\ 773\ 040\ 424\ 750\ 928\ 133\ 967$

**Table 3.** Presents the calculation formulas for determining the values of the dimensional of FPC.

N	Name of parameter	Symbol	Calculation formula	Unit SGS
1	Compton wavelength	$\lambda_{\pi C0}$	$\lambda_{\pi C0} = 2 \cdot \sqrt{\frac{\psi_\pi}{\alpha_\pi \cdot \beta_\pi}}$	sm
2	Rydberg constant	$R_{\pi^\infty 0}$	$R_{\pi^\infty 0} = \frac{2\pi^2 \cdot \alpha_\pi^2}{\lambda_{\pi C0}}$	$\text{sm}^{-1}$
3	the coefficient of concordance	$\kappa_{\pi R}$	$\kappa_{\pi R} = \frac{R_{\pi^\infty 0}}{R_\infty}$	
4	Rydberg constant	$R_{\pi^\infty}$	$R_{\pi^\infty} = \frac{R_{\pi^\infty 0}}{\kappa_{\pi R}}$	$\text{sm}^{-1}$
5	Compton wavelength	$\lambda_{\pi C}$	$\lambda_{\pi C} = 2\pi^2 \cdot \alpha_\pi^2 / R_{\pi^\infty}$	sm
6	electron mass	$m_{\pi e}$	$m_{\pi e} = \pi^2 \cdot f_{\pi s}^3 \cdot \lambda_{\pi C}^2 \cdot \rho_{\pi Se}$	g
7	proton mass	$m_{\pi p}$	$m_{\pi p} = m_{\pi e} / r_{ep}$	g
8	proton Compton wavelength	$\lambda_{\pi C,p}$	$\lambda_{\pi C,p} = r_{ep} \cdot \lambda_{\pi C}$	sm
9	neutron mass	$m_{\pi n}$	$m_{\pi n} = m_{\pi e} / r_{en}$	g
10	neutron Compton wavelength	$\lambda_{\pi C,n}$	$\lambda_{\pi C,n} = r_{en} \cdot \lambda_{\pi C}$	sm
11	Planck mass	$m_{\pi P}$	$m_{\pi P} = m_{\pi e} / \psi_\pi$	g
12	Planck length	$l_{\pi P}$	$l_{\pi P} = \lambda_{\pi C} \cdot \psi_\pi$	sm
13	Planck time	$t_{\pi P}$	$t_{\pi P} = l_{\pi P} / c$	s
14	Planck constant	$h_\pi$	$h_\pi = m_{\pi P} \cdot l_{\pi P} \cdot c$	$\text{g sm}^2 \text{s}^{-1}$
15	Newtonian constant of gravitation	$G_\pi$	$G_\pi = h_\pi \cdot c / m_{\pi P}^2$	$\text{g}^{-1} \text{sm}^3 \text{s}^{-2}$
16	atomic mass constant	$m_{\pi u}$	$m_{\pi u} = \frac{8\pi^4 \cdot p_{\pi s}}{(2\pi - 1)^4 \cdot (1 + 2\pi \cdot f_{\pi s})} \cdot m_{\pi p}$	g

**Table 4.** Presents the results of theoretical calculations the values of the dimensional of FPC of Table 3. In the calculations we used: data of the table 2; the Rydberg's constant  $R_\infty = 1,097\ 373\ 156\ 8539(55) \cdot 10^5 [\text{sm}^{-1}]$  (CODATA 2010); the speed of light  $2,99792458 \cdot 10^{10} [\text{sm} \cdot \text{s}^{-1}]$ ; surface density of the mass of the electron  $\rho_{\pi Se}$ , the numerical value of the which in Pi-Theory is set to unity:  $\rho_{\pi Se} = 1 [\text{g} \cdot \text{sm}^{-2}]$ .

N	Name of parameter	Symbol	The numerical value (SGS)	Unit SGS
1	Compton wavelength	$\lambda_{\pi C0}$	$2.397\ 686\ 311\ 973\ 620\ 014\ 643 \times 10^{-10}$	sm
2	Rydberg constant	$R_{\pi^\infty 0}$	$1.110\ 473\ 757\ 591\ 524\ 062\ 283 \times 10^5$	$\text{sm}^{-1}$
3	The coefficient of concordance	$\kappa_{\pi R}$	1.011 938 145 7946	
4	Rydberg constant	$R_{\pi^\infty}$	$1.097\ 373\ 156\ 8539 \times 10^5$	$\text{sm}^{-1}$
5	Compton wavelength	$\lambda_{\pi C}$	$2.426\ 310\ 240\ 7357 \times 10^{-10}$	sm
6	electron mass	$m_{\pi e}$	$9.109\ 382\ 325\ 3402 \times 10^{-28}$	g
7	proton mass	$m_{\pi p}$	$1.672\ 621\ 669\ 8229 \times 10^{-24}$	g
8	proton Compton wavelength	$\lambda_{\pi C,p}$	$1.321\ 409\ 857\ 4420 \times 10^{-13}$	sm

N	Name of parameter	Symbol	The numerical value (SGS)	Unit SGS
9	neutron mass	$m_{\pi n}$	$1.674\ 927\ 243\ 6135 \times 10^{-24}$	g
10	neutron Compton wavelength	$\lambda_{\pi C,n}$	$1.319\ 590\ 908\ 0246 \times 10^{-13}$	sm
11	Planck mass	$m_{\pi P}$	$5.455\ 886\ 822\ 7026 \times 10^{-5}$	g
12	Planck length	$l_{\pi P}$	$4.051\ 071\ 501\ 4798 \times 10^{-33}$	sm
13	Planck time	$t_{\pi P}$	$1.351\ 291\ 999\ 9741 \times 10^{-43}$	s
14	Planck constant	$h_{\pi}$	$6.626\ 069\ 154\ 6014 \times 10^{-27}$	$\text{g sm}^2 \text{s}^{-1}$
15	Newtonian constant of gravitation	$G_{\pi}$	$6.673\ 381\ 632\ 9142 \times 10^{-8}$	$\text{g}^{-1} \text{sm}^3 \text{s}^{-2}$
16	atomic mass constant	$m_{\pi u}$	$1.660\ 539\ 172\ 2265 \times 10^{-24}$	g

### 3. A table comparing the data CODATA 2010 with theoretical calculations

In accordance with the list of parameters of the tables 1 and 3, see: values FPC recommended CODATA (2010) for international use - of publication on the NIST website by address <http://physics.nist.gov/cuu/Constants/index.html>; the calculation results from tables 2 and 4; the results of data comparison (column 6),  $\delta_r$  – the relative uncertainty.

Parameter $a$ , CODATA	The numerical value SGS, CODATA 2010	Relative std. uncert. $u_r$	Parameter $a^*$ , Pi-Theory	The numerical value SGS, Pi-Theory	$\delta_r = \frac{\bar{a} - a^*}{a^*}$
1	2	3	4	5	6
$\alpha$	$7.297\ 352\ 5698(24) \times 10^{-3}$	$3.2 \times 10^{-10}$	$\alpha_{\pi} \cdot 2\pi$	$7.297\ 352\ 572\ 519\ 857 \times 10^{-3}$	$-3.7 \times 10^{-10}$
$a_e$	$1.159\ 652\ 180\ 76(27) \times 10^{-3}$	$2.3 \times 10^{-10}$	$a_{\pi e}$	$1.159\ 652\ 180\ 787\ 572 \times 10^{-3}$	$-0.2 \times 10^{-10}$
$m_e / m_p$	$5.446\ 170\ 2178(22) \times 10^{-4}$	$4.1 \times 10^{-10}$	$r_{\pi ep}$	$5.446\ 170\ 218\ 699\ 091 \times 10^{-4}$	$-1.6 \times 10^{-10}$
$m_e / m_n$	$5.438\ 673\ 4461(32) \times 10^{-4}$	$5.8 \times 10^{-10}$	$r_{\pi en}$	$5.438\ 673\ 446\ 906\ 119 \times 10^{-4}$	$-1.4 \times 10^{-10}$
$m_n / m_p$	$1.001\ 378\ 419\ 17(45)$	$4.5 \times 10^{-10}$	$r_{\pi np}$	$1.001\ 378\ 419\ 179\ 999$	$-0.1 \times 10^{-10}$
$\mu_p / \mu_n$	$-1.459\ 898\ 06(34)$	$2.4 \times 10^{-7}$	$r_{\pi \mu, pn}$	$-1.459\ 898\ 124\ 622\ 978$	$-0.4 \times 10^{-7}$
$R_{\infty}$	$1.097\ 373\ 156\ 8539(55) \times 10^5$	$5.0 \times 10^{-12}$	$R_{\pi \infty}$	$1.097\ 373\ 156\ 8539 \times 10^5$	0
$\lambda_C$	$2.426\ 310\ 2389(16) \times 10^{-10}$	$6.5 \times 10^{-10}$	$\lambda_{\pi C}$	$2.426\ 310\ 240\ 7357 \times 10^{-10}$	$-7.5 \times 10^{-10}$
$m_e$	$9.109\ 382\ 91(40) \times 10^{-28}$	$4.4 \times 10^{-8}$	$m_{\pi e}$	$9.109\ 382\ 325\ 3402 \times 10^{-28}$	$-6.4 \times 10^{-8}$
$m_p$	$1.672\ 621\ 777(74) \times 10^{-24}$	$4.4 \times 10^{-8}$	$m_{\pi p}$	$1.672\ 621\ 669\ 8229 \times 10^{-24}$	$6.4 \times 10^{-8}$
$\lambda_{C,p}$	$1.321\ 409\ 856\ 23(94) \times 10^{-13}$	$7.1 \times 10^{-10}$	$\lambda_{\pi C,p}$	$1.321\ 409\ 857\ 4420 \times 10^{-13}$	$-9.1 \times 10^{-10}$
$m_n$	$1.674\ 927\ 351(74) \times 10^{-24}$	$4.4 \times 10^{-8}$	$m_{\pi n}$	$1.674\ 927\ 243\ 6135 \times 10^{-24}$	$6.4 \times 10^{-8}$
$\lambda_{C,n}$	$1.319\ 590\ 9068(11) \times 10^{-13}$	$8.2 \times 10^{-10}$	$\lambda_{\pi C,n}$	$1.319\ 590\ 908\ 0246 \times 10^{-13}$	$-9.2 \times 10^{-10}$
$m_p$	$2.176\ 51(13) \times 10^{-5}$	$6.0 \times 10^{-5}$	$m_{\pi p} / \sqrt{2\pi}$	$2.176\ 583\ 930\ 6611 \times 10^{-5}$	$-3.4 \times 10^{-5}$
$l_p$	$1.616\ 199(97) \times 10^{-33}$	$6.0 \times 10^{-5}$	$l_{\pi p} / \sqrt{2\pi}$	$1.616\ 143\ 702\ 8696 \times 10^{-33}$	$3.4 \times 10^{-5}$
$t_p$	$5.391\ 06(32) \times 10^{-44}$	$6.0 \times 10^{-5}$	$t_{\pi p} / \sqrt{2\pi}$	$5.390\ 875\ 119\ 5788 \times 10^{-44}$	$3.4 \times 10^{-5}$
$h$	$6.626\ 069\ 57(29) \times 10^{-27}$	$4.4 \times 10^{-8}$	$h_{\pi}$	$6.626\ 069\ 154\ 6014 \times 10^{-27}$	$6.2 \times 10^{-8}$
$G$	$6.673\ 384(80) \times 10^{-8}$	$1.2 \times 10^{-4}$	$G_{\pi}$	$6.673\ 381\ 632\ 9142 \times 10^{-8}$	$0.6 \times 10^{-4}$
$m_u$	$1.660\ 538\ 921(73) \times 10^{-24}$	$4.4 \times 10^{-8}$	$m_{\pi u}$	$1.660\ 539\ 172\ 2265 \times 10^{-24}$	$-15.1 \times 10^{-8}$