OTHER SMARANDACHE TYPE FUNCTIONS

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- 1) Let $f: N \longrightarrow N$ be a strictly increasing function and x an element in N. Then:
 - a) Inferior Smarandache f-Part of x,

ISf(x) is the smallest k such that $f(k) \le x \le f(k+1)$.

b) Superior Smarandache f-Part of x,

SSf(x) is the smallest k such that $f(k) < x \le f(k+1)$.

Particular Cases:

- a) Inferior Smarandache Prime Part: For any positive real number n one defines ISp(n) as the largest prime number less than or equal to n. The first values of this function are (Smarandache[6] and Sloane[5]):
 - 2,3,3,5,5,7,7,7,7,11,11,13,13,13,13,17,17,19,19,19,19,23,23.
- b) Superior Smarandache Prime Part: For any positive real number n one defines SSp(n) as the smallest prime number greater than or equal to n. The first values of this function are (Smarandache[6] and Sloane[5]): 2,2,2,3,5,5,7,7,11,11,11,11,13,13,17,17,17,17,19,19,23,23,23.
- c) Inferior Smarandache Square Part: For any positive real number n one defines ISs(n) as the largest square less than or equal to n. The first values of this function are (Smarandache[6] and Sloane[5]):
- 0,1,1,1,4,4,4,4,4,9,9,9,9,9,9,9,16,16,16,16,16,16,16,16,16,25,25.
 b) Superior Smarandache Square Part:
 For any positive real number n one defines SSs(n) as the smallest square greater than or equal to n.
 The first values of this function are (Smarandache[6] and Sloane[5]):
- 0,1,4,4,4,9,9,9,9,16,16,16,16,16,16,16,25,25,25,25,25,25,25,25,25,36.

 - e) Superior Smarandache Cube Part:
 For any positive real number n one defines SSs(n) as the smallest cube greater than or equal to n.
 The first values of this function are (Smarandache[6] and Sloane[5]):

- - f) Inferior Smarandache Factorial Part: For any positive real number n one defines ISf(n) as the largest factorial less than or equal to n. The first values of this function are (Smarandache[6] and Sloane[5]):

Particular Cases:

- a) Smarandache Square Complementary Function:
 f: N ---> N, f(x) = the smallest k such that xk is a
 perfect square.
 The first values of this function are (Smarandache[6] and
 Sloane[5]):
 1,2,3,1,5,6,7,2,1,10,11,3,14,15,1,17,2,19,5,21,22,23,6,1,26,3,7.
- b) Smarandache Cubic Complementary Function:
 f: N ---> N, f(x) = the smallest k such that xk is a
 perfect cube.
 The first values of this function are (Smarandache[6] and
 Sloane[5]):
 1,4,9,2,25,36,49,1,3,100,121,18,169,196,225,4,289,12,361,50.
 More generally:
- c) Smarandache m-power Complementary Function:
 f: N ---> N, f(x) = the smallest k such that xk is a
 perfect m-power.
- d) Smarandache Prime Complementary Function:
 f: N ---> N, f(x) = the smallest k such that x+k is a prime.
 The first values of this function are (Smarandache[6] and Sloane[5]):
 1,0,0,1,0,3,2,1,0,1,0,3,2,1,0,1,0,3,2,1,0,5,4,3,2,1,0,1,0,5.

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 - (Carol Moore & Marilyn Wurzburger: librarians).