## On a Conjecture of F. Smarandache

Wang Yang 1.2 Zhang Hong Li 1.3

Department of Mathematics, Northwest University;
Department of Mathematics, Nanyang Teacher's College, Henan China 473061;
3.Xi'an Finance and Accounting School, Xi'an Shanxi China 710048)

Abstract: The main purpose of this paper is to solve a problem generated by Professor F.Smarandache.

Key word: Permutation sequence; k-power.

Let n be a positive integer, n is called a k-power if  $n=m^k$ , where k and m are positive integer, and  $k \ge 2$ . Obviously, if n is a k-power, p is a prime, then we have  $p^k|n$ , if p|n.

In his book "Only Problems, not Solutions", Professor F.Smarandache defined a permutation sequence: 12, 1342, 135642, 13578642, 13579108642, 135791112108642, 1357911131412108642,13579111315161412108642,135791113151718161412108642,..., and generated a conjecture: there is no any k-power among these numbers. The main purpose of this paper is to prove that this conjecture is true.

Suppose there is a k-power a(n) among the permutation sequence. Noting the fact:  $12=2^2\times3$ , we may immediately get:  $a(n)\geq 1342>10000$ . For the last two digits of a(n) is 42, so we have  $a(n)\equiv 42 \pmod{100}$ 

Noting that 4|100, we may immediately deduce :  $a(n) \equiv 42 \equiv 2 \pmod{4}$ .

So we get 2|a(n), 4|a(n). However, 2 is a prime, then 4|a(n) contradicts with 4|a(n). So a(n) is not a k-power.

This complete the proof of the conjecture.

## REFERENCES

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