New finding of number theory

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1. Introduce

To prove a theorem, I have found some new phenomenon in number theory. To explain the phenomenon, I have given my explanation and deduction. Some deduction is surprised and revolutionary, which is unbelievable, but it can be verified by fact and logic.

2. Prime density regularity

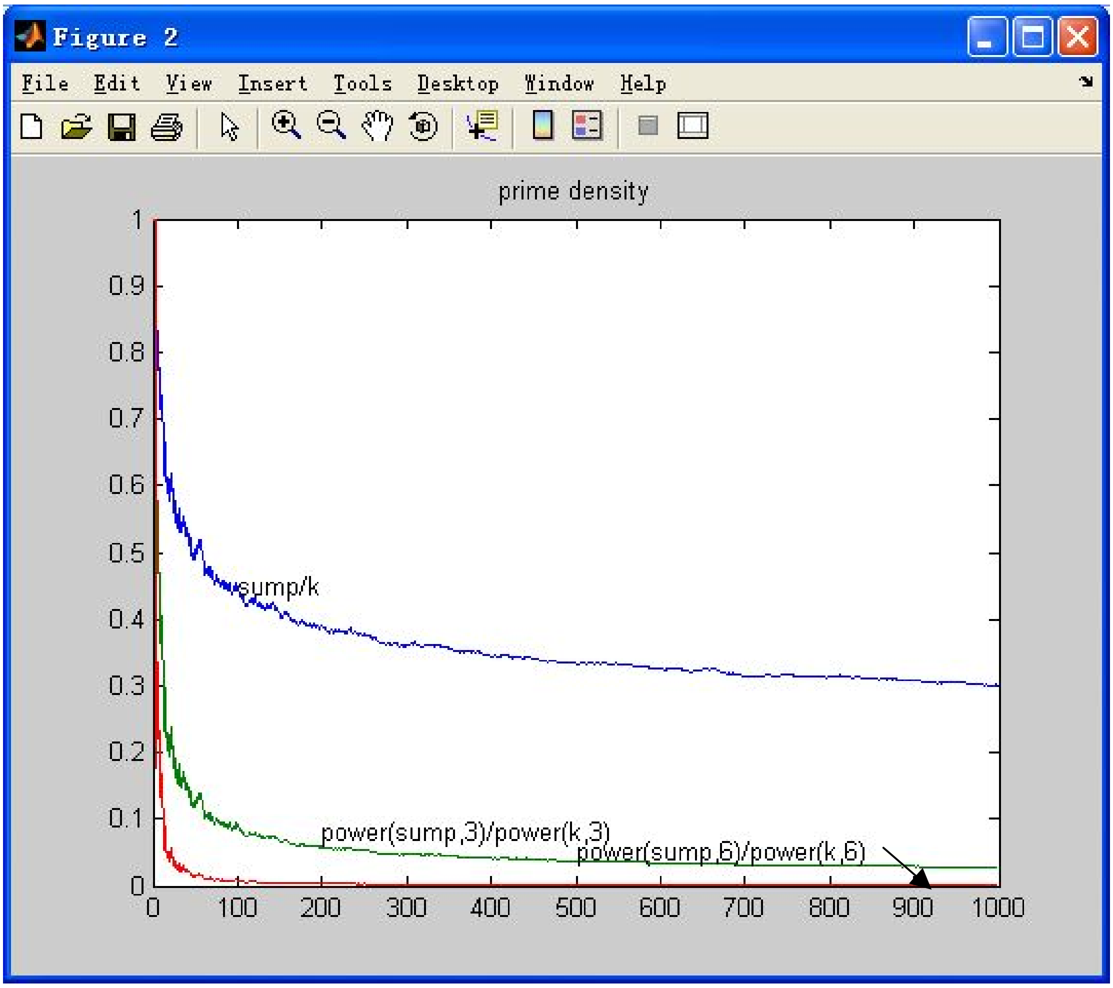
The occurrence of prime is irregular, but the density of prime is more regular.

The density of prime is oscillating to trend to 0 when odd number is increasing.

Prime density data table like below, which displays the regularity very clearly.

2K+1	*sum(prime)/K*	$sum(p)^3 / K^3$	$sum(p)^6 / K^6$
00000003	1.0000	1.0000	1.0000
00000005	1.0000	1.0000	1.0000
00000007	1.0000	1.0000	1.0000
00000011	0.8000	0.5120	0.2621
00000013	0.8333	0.5787	0.3349
…	…	…	…
00000673	0.3601	0.0467	0.0022
00000677	0.3609	0.0470	0.0022
00000683	0.3607	0.0469	0.0022
00000691	0.3594	0.0464	0.0022
00000701	0.3571	0.0456	0.0021
…	…	…	…
00098807	0.1920	0.0071	0.0001
00098809	0.1920	0.0071	0.0001
00098837	0.1919	0.0071	0.0000
00098849	0.1919	0.0071	0.0000
…	…	…	…

The function plot like below.



3. Odd composite number density regularity

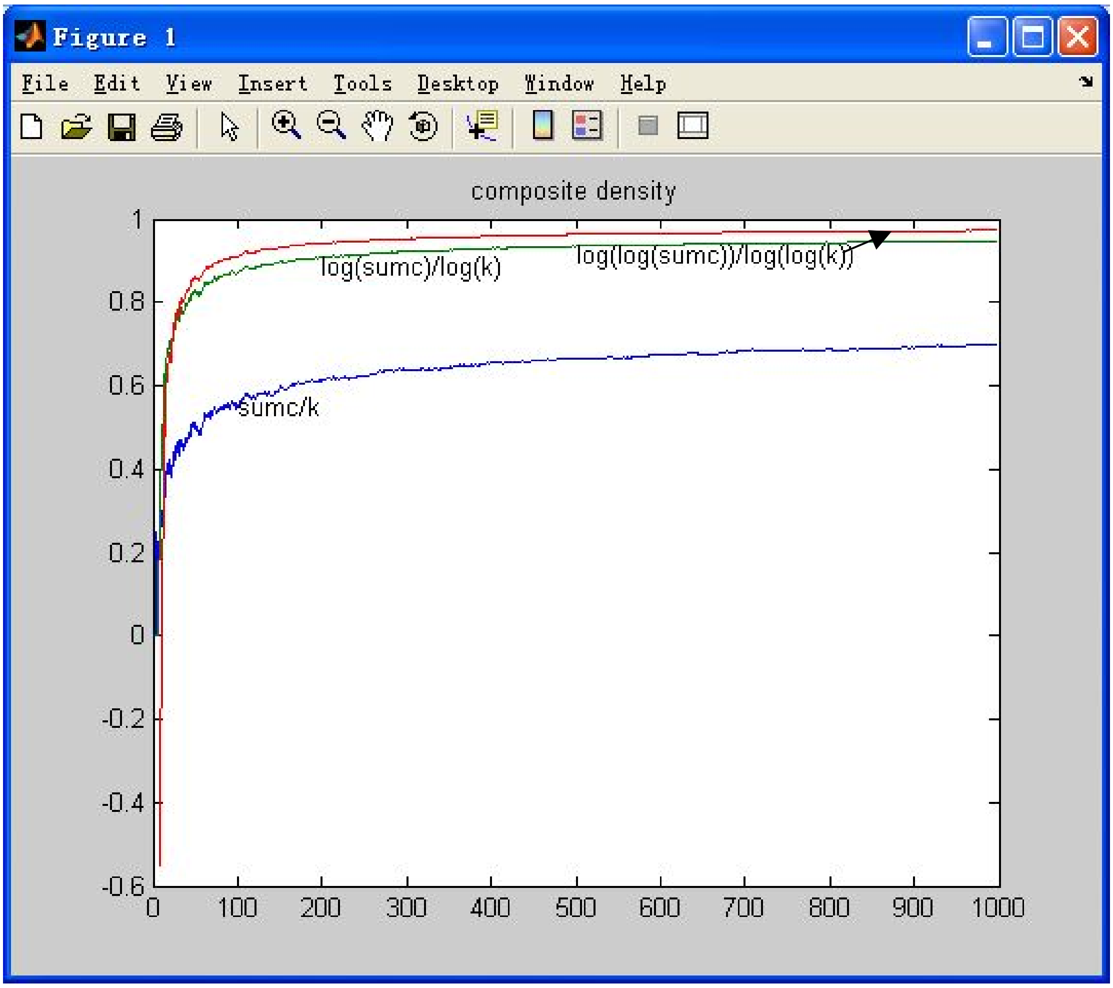
The density of odd composite number is oscillating to trend to 1 when odd number is increasing.

Odd composite number density data table like below,

2K+1	*sum(composite)/K*	*ln(sum(c))/lnK*	*lnln(sum(c))/lnlnK*
00000009	0.2500	0.0000	-INF
00000015	0.2857	0.3562	-0.5505
00000021	0.3000	0.4771	0.1128
00000025	0.3333	0.5579	0.3588
00000027	0.3846	0.6275	0.5052
…	…	…	…
00000671	0.6418	0.9237	0.9549
00000675	0.6409	0.9236	0.9549
00000679	0.6401	0.9234	0.9548
00000681	0.6412	0.9238	0.9550
…	…	…	…
00098805	0.8081	0.9803	0.9916
00098811	0.8080	0.9803	0.9916
00098813	0.8080	0.9803	0.9916
00098815	0.8080	0.9803	0.9916
…	…	…	…
12669203	8691	9910	9967

12669205	8691	9910	9967
12669207	8691	9910	9967
12669209	8691	9910	9967
…	…	…	…

The function plot like below.



4. The limitation of odd number is composite number

Theorem (4.1):

When an odd number trends to infinity, this odd number must be an odd composite number.

First to define a prime set P = {p|p=1×p; {p/(p-k)} $\neq$ 0; [p/(p-k)] $\neq$ 0; p>1,k$\geq$1,k<p; p, k$\in$N}. x = [x]+{x} is Gaussian function. [x] expresses the maximum integer but not above x . Set [X] = {[x]| [x]$\leq$x, [x]>x-1; x$\in$R, [x]$\in$Z}; {x} expresses the non-negative decimal fraction. Set {X} = {{x}| {x}$\geq$0, {x} < 1, {x} = x – [x]; x$\in$R, [x]$\in$Z }

(4.4.1) Suppose when an odd number trends to infinity, there is at least one odd number is prime.

i.e. Exist p1 is an odd number and $\lim_{p1\to\infty} p1 \in$ P

Because p1 is an odd number $\Rightarrow$ $\lim_{p1\to\infty}(p1/(p1-[p1/2]))$ = $\lim_{p1\to\infty}(p1/(p1-(p1-1)/2))$ = $\lim_{p1\to\infty}(p1/(p1/2+1/2))$ = $\lim_{p1\to\infty}(2p1/(p1+1))$ = $2\lim_{p1\to\infty}(1-1/(p1+1))$=2 $\Rightarrow$ {2} = { $\lim_{p1\to\infty}(p1/(p1-[p1/2]))$ } = 0 (4.1.1.1)

Because p1$\in$P and p1 trends to infinity $\Rightarrow${p1/(p1-[p1/2])} $\neq$ 0 and p1 trends to infinity $\Rightarrow${ $\lim_{p1\to\infty}(p1/(p1-[p1/2]))$ } $\neq$ 0.

It’s self-contradictory with (4.1.1.1). So p1 is not a prime, because we have found a divisor p1-[p1/2] beside p1 and 1. According to prime definition (p = 1×p), p1 does not belong to prime set.

Because $\lim_{p1\to\infty} p1 = \infty \Rightarrow \lim_{p1\to\infty} p1 \neq 0$ and $\lim_{p1\to\infty} p1 \neq 1$.

$\lim_{p1\to\infty} p1 \neq 0$, $\lim_{p1\to\infty} p1 \neq 1$ and $\lim_{p1\to\infty} p1 \notin$ P $\Rightarrow$ $\lim_{p1\to\infty} p1$ is an odd composite number. Preliminary theorem (4.1) is true.

Theorem (4.1) is a very key theorem. To explain clearly, let me talk from a Series $X_k = p_k/(p_k-1)$, k∈N, $p_k \in$P. i.e. X_k=2/1, 3/2, 5/4, 7/6, 11/10, 13/12, 17/16,…. It's easy to calculate the limitation of X_k. $\lim_{pk\to\infty} pk/(pk-1)=1$. Similarly, $\lim_{pk\to\infty} pk/(pk-[pk/2])=2$. It's strictly "equal to".

But we have found 2 divisors (p_k-1 and p_k-[p_k/2]) of p_k, according to prime definition (p = 1×p), p_k does not belong to prime set. It has become a composite number.

Just like limitation of polygon becomes a circle, that is a qualitative change. The limitation of prime becomes a composite number that is also a qualitative change.

It's not easy to state clearly preliminary theorem (4.1). I have another statement for theorem (4.1)

Theorem (4.2):

The distribution of odd number serial can divide into 2 parts: a + b.

Serial a is a compound body of primes and odd composite numbers, density of prime become more and more lower;

Serial b is a pure body of odd composite numbers after density of prime being zero;

For example: 1,3,5,7,9,11,13,…,c1,c2,c3,c4,…

c1,c2,c3,c4,… are very big odd composite numbers.

5. Natural number is limited

In ancient times, people can only calculate by hands. The natural number is from 1 to 10. Such as 11, 12, …, 21, 22, …,100, …, 1000, … is recorded as one number 10+.

In 32 bit computer, the biggest number is 2^32 = 4294967296. Any number is more than 4294967296 recorded as 4294967296+. Similarly, In 64 bit computer, the biggest number is 2^64 = 18446744073709551616. Any number being bigger than 2^64 is record as one number 2^64+. The natural number is from 1 to 18446744073709551616 in computer.

Since human invent algebra, any big number can be expressed as one character N. But it has occupied 1 character. N +1 occupied 1 character also. A very very … big number N + … can exhaust all characters finally. It only changes the start number of natural number from 1 to N.

Maybe some people say that we can think a bigger number than limitation. But if the big number has occupied human's entire brain cell, human can't even think a bigger number than limitation.

Any number needs something to store, such as finger, paper, computer memory or brain cell. We can exhaust everything in the world to store a big number, including sun, earth, atom, and particle, everything in the world. Because the matter is limited, the big number is also limited. Any number being bigger than it can't be measured or calculated, because we can't store such a big number. This number should be the biggest number in our world and it's the limitation of natural number.

Theorem (5.1):

Natural number is limited.

We can exhaust everything in the world to store a big number record as INF.

INF + 1 $\geq$ INF for algebra calculating rule;

But we have exhausted everything in the world to store INF, INF + 1 $\leq$ INF for maximum store matter.

Because INF + 1 $\geq$ INF and INF + 1 $\leq$ INF $\Rightarrow$ INF + 1 = INF.

Similarly, INF + k = INF, k$\geq$1, k$\leq$ INF.

Because INF + k = INF, k$\leq$ INF $\Rightarrow$ INF + INF = INF $\Rightarrow$ 2$\times$INF = INF;

Similarly, k$\times$INF = INF, k$\geq$1, k$\leq$ INF.

Because INF $\times$ k = INF, k$\leq$ INF $\Rightarrow$ INF $\times$ INF = INF $\Rightarrow$ INF^2 = INF;

Similarly, INF^k = INF, k$\geq$1, k$\leq$ INF.

Because INF^k = INF, k$\leq$ INF $\Rightarrow$ INF^{INF} = INF.

Summary below:

Theorem (5.2):

INF + k = INF;

INF $\times$ k = INF;

INF^k = *INF*

$k \geq 1, k \leq \ INF$

Because $INF + k = INF \ \Rightarrow$ natural number is limited

6. Prime is limited

It seems that it’s contradictory with the famous Euclid’s proof. Suppose prime is limited, P = {p|2, 3, 5 … p_k }. Constructing a number p_{k+1} = 2×3×5×…×p_k + 1. Either p_{k+1} is a prime or p_{k+1} is a composite number that can resolve a prime being bigger than p_k.

It’s correct in classical number theory.

If p_{k+1} = INF, because of theorem (5.2), INF = p_k × INF $\Rightarrow$ p_{k+1} is a composite number. But p_{k+1} can resolve a divisor of INF, and INF is a composite number. It’s not sure to resolve a prime being bigger than p_k. So the famous proof is not correct when natural number is limited.

Actually, because natural number is limited, prime is natural number $\Rightarrow$ prime is limited.

7. Zeno’s paradox

In the paradox of Achilles and the Tortoise, Achilles is in a footrace with the tortoise. Achilles allows the tortoise a head start of 100 meters, for example. If we suppose that each racer starts running at some constant speed (one very fast and one very slow), then after some finite time, Achilles will have run 100 meters, bringing him to the tortoise's starting point. During this time, the tortoise has run a much shorter distance, say, 10 meters. It will then take Achilles some further time to run that distance, by which time the tortoise will have advanced farther; and then more time still to reach this third point, while the tortoise moves ahead. Thus, whenever Achilles reaches somewhere the tortoise has been, he still has farther to go. Therefore, because there are an infinite number of points Achilles must reach where the tortoise has already been, he can never overtake the tortoise.

It’s very interesting. Zeon’s paradox becomes the evidence to verify that natural number is limited.

Infinitesimal can be regarded as 1/infinity. Because infinity is limited, 1/infinity is limited also.

In fact, Achilles has one moment to overtake the tortoise. At this moment, infinitesimal can’t be divided again. If infinitesimal is really infinite small, that can’t explain Zeno’s paradox with satisfaction. But if natural number is limited, it’s so natural to explain Zeno’s paradox.

8. Conclusion

When odd number increases, the density of odd composite number trends to 1 with oscillation; the density of prime trends to 0 with oscillation.

Natural number is really the quantity of world matter.

Number need matter to store, it imply that number map really to the matter quantity.

Theorem (8.1)

The distribution of odd number serial is 1, 3, 5, …, INF, INF, …

The distribution of natural number serial is 1, 2, 3, …, INF, INF, …

Theorem (8.2)

Infinitesimal can be regarded as 1/infinity. Because infinity is limited, infinitesimal is limited also.

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